



## International GCSE Mathematics

## Formulae sheet – Higher Tier

**Arithmetic series**

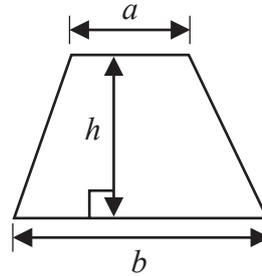
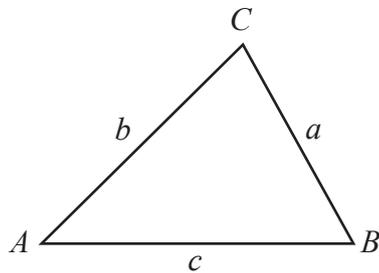
Sum to  $n$  terms,  $S_n = \frac{n}{2} [2a + (n-1)d]$

**The quadratic equation**

The solutions of  $ax^2 + bx + c = 0$  where  $a \neq 0$  are given by:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

**Area of trapezium** =  $\frac{1}{2}(a+b)h$

**Trigonometry**

**In any triangle ABC**

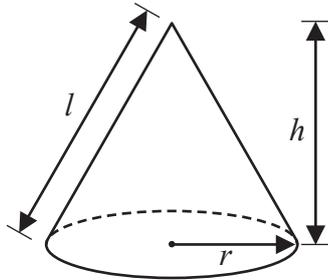
**Sine Rule**  $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

**Cosine Rule**  $a^2 = b^2 + c^2 - 2bc \cos A$

**Area of triangle** =  $\frac{1}{2}ab \sin C$

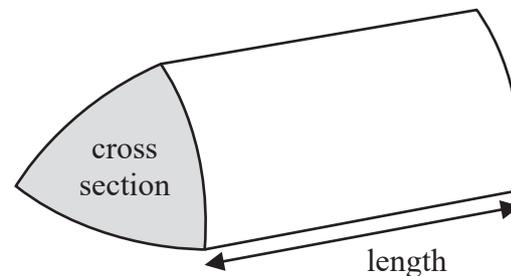
**Volume of cone** =  $\frac{1}{3}\pi r^2 h$

**Curved surface area of cone** =  $\pi r l$



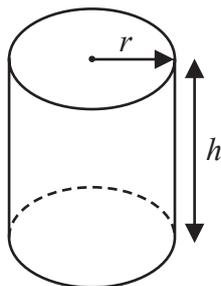
**Volume of prism**

= area of cross section  $\times$  length



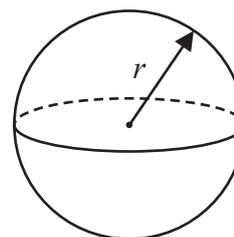
**Volume of cylinder** =  $\pi r^2 h$

**Curved surface area of cylinder** =  $2\pi r h$



**Volume of sphere** =  $\frac{4}{3}\pi r^3$

**Surface area of sphere** =  $4\pi r^2$



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Answer ALL TWENTY FOUR questions.**

**Write your answers in the spaces provided.**

**You must write down all the stages in your working.**

- 1** The table shows information about the lengths, in minutes, of 50 telephone calls.

Length of telephone call ( $m$ minutes)	Frequency
$0 < m \leq 5$	8
$5 < m \leq 10$	2
$10 < m \leq 15$	6
$15 < m \leq 20$	4
$20 < m \leq 25$	12
$25 < m \leq 30$	18

- (a) Write down the modal class.

.....  
(1)

- (b) Work out an estimate for the total length, in minutes, of these telephone calls.

..... minutes  
(3)

**(Total for Question 1 is 4 marks)**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



- 2 The diagram shows triangle  $ABC$  and triangle  $ECD$

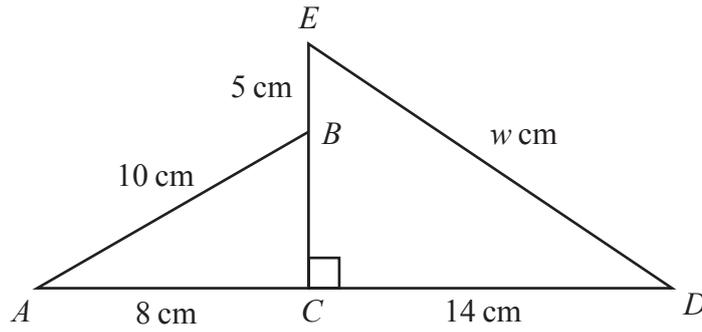


Diagram **NOT**  
accurately drawn

$ACD$  and  $EBC$  are straight lines.

$$AB = 10 \text{ cm} \quad AC = 8 \text{ cm} \quad EB = 5 \text{ cm} \quad CD = 14 \text{ cm} \quad ED = w \text{ cm}$$

Work out the value of  $w$

Give your answer correct to one decimal place.

$$w = \dots\dots\dots$$

(Total for Question 2 is 4 marks)

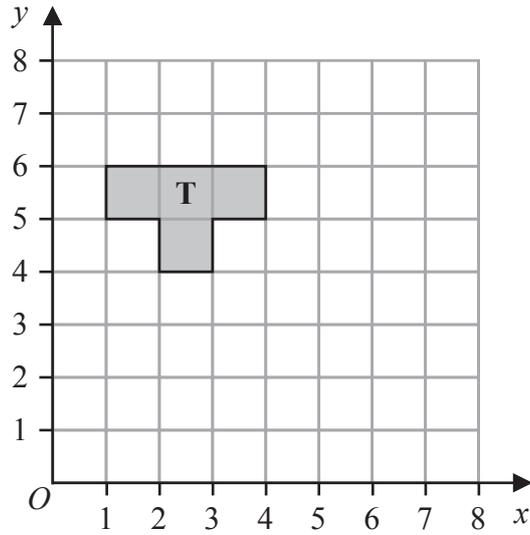
DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

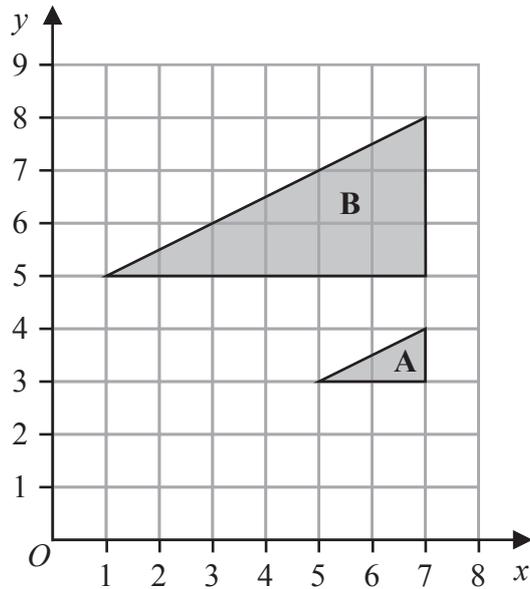


3



(a) Reflect shape **T** in the line  $y = x$

(2)



(b) Describe fully the single transformation that maps triangle **A** onto triangle **B**

(3)

(Total for Question 3 is 5 marks)



4 (a) Solve  $\frac{2x+5}{6} = 2x-5$

Show clear algebraic working.

$x = \dots\dots\dots$   
(3)

(b) Simplify  $h^{15} \div h^3$

$\dots\dots\dots$   
(1)

(c) Simplify fully  $(2g^3k^5)^4$

$\dots\dots\dots$   
(2)

(d) Given that  $\frac{y^5 \times y^n}{y^7} = y^{12}$

work out the value of  $n$

$n = \dots\dots\dots$   
(2)

(Total for Question 4 is 8 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



5 Avril bakes a cake.

She uses flour, butter and sugar such that

$$\text{weight of flour : weight of butter} = 6 : 5$$

$$\text{weight of butter : weight of sugar} = 3 : 2$$

Avril uses 120 grams of sugar.

Work out the weight of flour Avril uses.

..... grams

**(Total for Question 5 is 3 marks)**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



6 Show that  $3\frac{3}{7} \div 2\frac{2}{3} = 1\frac{2}{7}$

(Total for Question 6 is 3 marks)

- 7 Hermione buys a boat for \$26 800  
The value of the boat depreciates by 8% each year.  
Work out the value of the boat at the end of 3 years.  
Give your answer correct to the nearest dollar.

\$.....

(Total for Question 7 is 3 marks)



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- 8 The mean number of goals scored by a hockey team in 8 matches is 6  
The team plays 2 more matches and scores  $k$  goals in each match.  
The mean number of goals scored by the hockey team in the 10 matches is 7

Work out the value of  $k$

$$k = \dots\dots\dots$$

(Total for Question 8 is 3 marks)

- 9 A straight line passes through the points with coordinates  $(0, -3)$  and  $(2, 0)$   
Find an equation of the line.

$$\dots\dots\dots$$

(Total for Question 9 is 2 marks)



10 The diagram shows a hexagon  $ABCDEF$

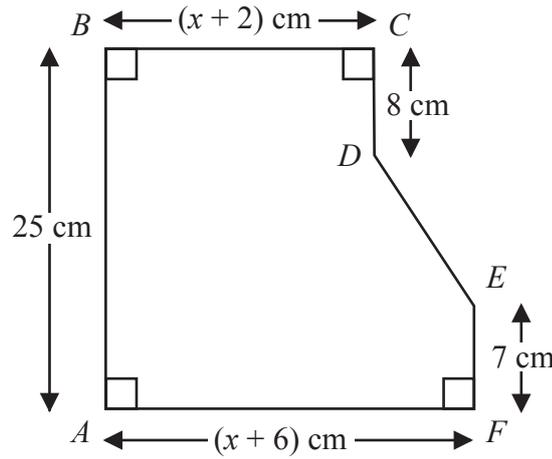


Diagram **NOT**  
accurately drawn

$$AB = 25 \text{ cm} \quad BC = (x + 2) \text{ cm} \quad CD = 8 \text{ cm} \quad EF = 7 \text{ cm} \quad AF = (x + 6) \text{ cm}$$

The area of hexagon  $ABCDEF$  is  $258 \text{ cm}^2$

Work out the value of  $x$

$$x = \dots\dots\dots$$

(Total for Question 10 is 5 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA





12  $2^7 \times 4^5 = 4^x$

(a) Calculate the value of  $x$

$$x = \dots\dots\dots (2)$$

(b) Simplify fully  $(125p^6y^{24})^{\frac{2}{3}}$

.....  
(2)

(Total for Question 12 is 4 marks)

13 Robert asked 11 people how many meetings they attended last week.

Here are the results in numerical order.

1    2    4    6    6    8    11    12    13    14    17

Find the interquartile range of the number of meetings.

.....  
(Total for Question 13 is 2 marks)

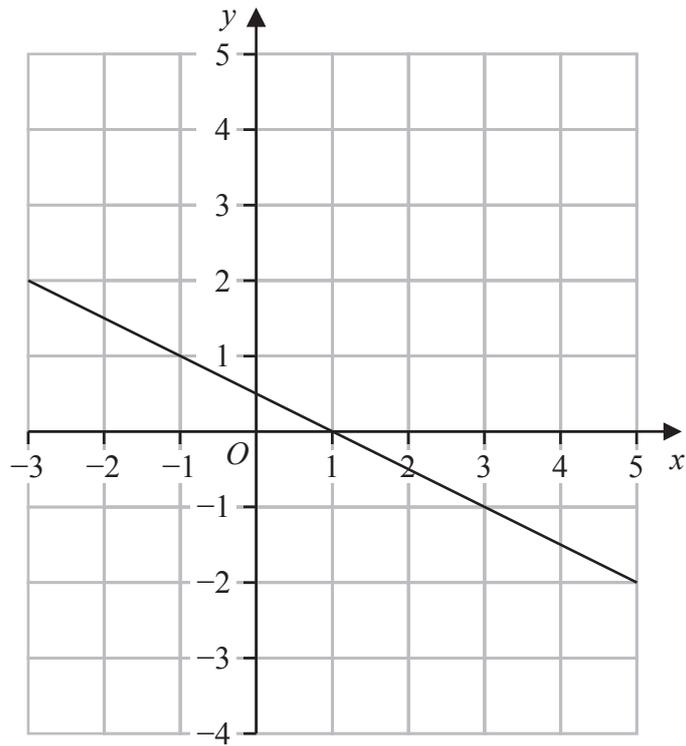
DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



14 Here is the graph of the equation  $2y + x = 1$  drawn on a grid.



By drawing another straight line on the grid, solve the simultaneous equations

$$y - x - 2 = 0$$

$$2y + x = 1$$

$$x = \dots\dots\dots$$

$$y = \dots\dots\dots$$

(Total for Question 14 is 3 marks)



15 (a) Use algebra to show that  $0.\dot{3}\dot{7}\dot{2} = \frac{41}{110}$

(2)

(b) Express  $\frac{\sqrt{125} + \sqrt{80}}{\sqrt{3}}$  in the form  $\sqrt{n}$  where  $n$  is an integer.

Show your working clearly.

(3)

(Total for Question 15 is 5 marks)



16 Expand and simplify  $(2x + 3)(x - 5)(x + 4)$

.....  
(Total for Question 16 is 3 marks)

17  $P = a(c + y)$

$a = 8.3$  correct to 2 significant figures

$c = 2$  correct to 1 significant figure

$y = 15$  correct to the nearest 5

Work out the upper bound for the value of  $P$   
Show your working clearly.

.....  
(Total for Question 17 is 3 marks)



- 18 A particle is moving along a straight line that passes through the fixed point  $O$   
The displacement,  $s$  metres, of the particle from  $O$  at time  $t$  seconds is given by

$$s = 2t^3 - 5t^2 + 6t - 5$$

Find the value of  $t$  when the acceleration of the particle is  $5 \text{ m/s}^2$

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

 $t = \dots\dots\dots$ 

(Total for Question 18 is 4 marks)



19 The functions  $f$  and  $g$  are such that

$$f:x \mapsto 5x + 7$$

$$g:x \mapsto \frac{5}{2x-9}$$

(a) State which value of  $x$  cannot be included in any domain of  $g$

.....  
(1)

(b) Find  $fg(4)$

.....  
(2)

The function  $h$  is such that

$$h:x \mapsto 3x^2 - 12x + 8 \quad \text{where } x > 2$$

(c) Express the inverse function  $h^{-1}$  in the form  $h^{-1}:x \mapsto \dots$

$h^{-1}:x \mapsto \dots$   
(4)

(Total for Question 19 is 7 marks)



P 7 3 4 6 9 A 0 1 7 2 4

- 20 The diagram shows equilateral triangle  $ABC$  with sides of length 10 cm. A circle is drawn inside the triangle.

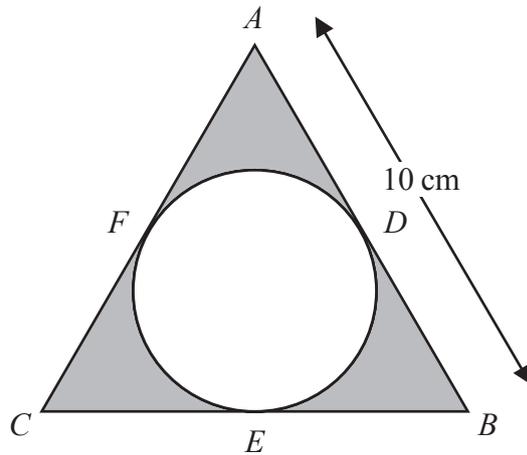


Diagram **NOT** accurately drawn

$D$ ,  $E$  and  $F$  are points on the circle.

$ADB$ ,  $BEC$  and  $CFA$  are tangents to the circle.

Calculate the total area of the regions shown shaded in the diagram.  
Give your answer correct to 3 significant figures.

..... cm<sup>2</sup>

(Total for Question 20 is 4 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



- 21 The line with equation  $x + 2y = 5$  intersects the curve with equation  $x^2 + 3y^2 = 13$  at the points  $A$  and  $B$

Find the coordinates of  $A$  and the coordinates of  $B$   
Show clear algebraic working.

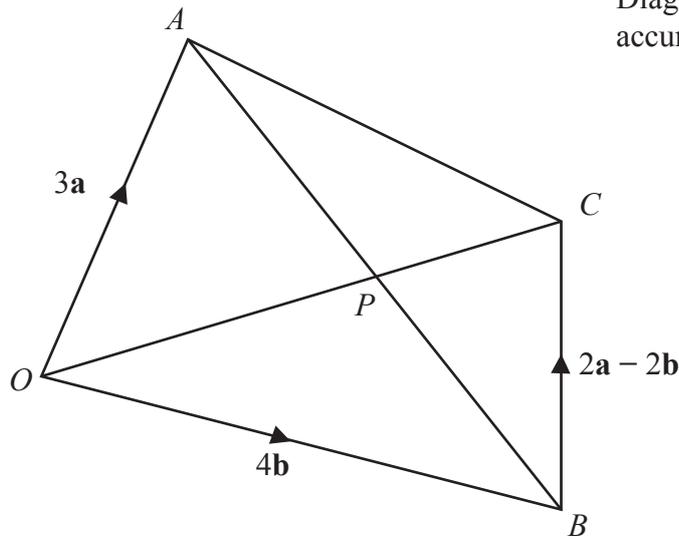
(....., .....) )

(....., .....) )

(Total for Question 21 is 5 marks)



22



$OACB$  is a quadrilateral.

$$\vec{OA} = 3\mathbf{a} \quad \vec{OB} = 4\mathbf{b} \quad \vec{BC} = 2\mathbf{a} - 2\mathbf{b}$$

- (a) (i) Find the vector  $\vec{OC}$  in terms of  $\mathbf{a}$  and  $\mathbf{b}$   
Simplify your answer.

$$\vec{OC} = \dots\dots\dots (1)$$

- (ii) Find the vector  $\vec{AB}$  in terms of  $\mathbf{a}$  and  $\mathbf{b}$

$$\vec{AB} = \dots\dots\dots (1)$$

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

The point  $P$  lies on  $AB$  and on  $OC$

- (b) Using a vector method, find the ratio  $AP : PB$   
Show your working clearly.

.....  
(3)

(Total for Question 22 is 5 marks)



P 7 3 4 6 9 A 0 2 1 2 4

23 Here is a frustum of a cone.

The frustum is made by removing a small cone from a similar large cone.

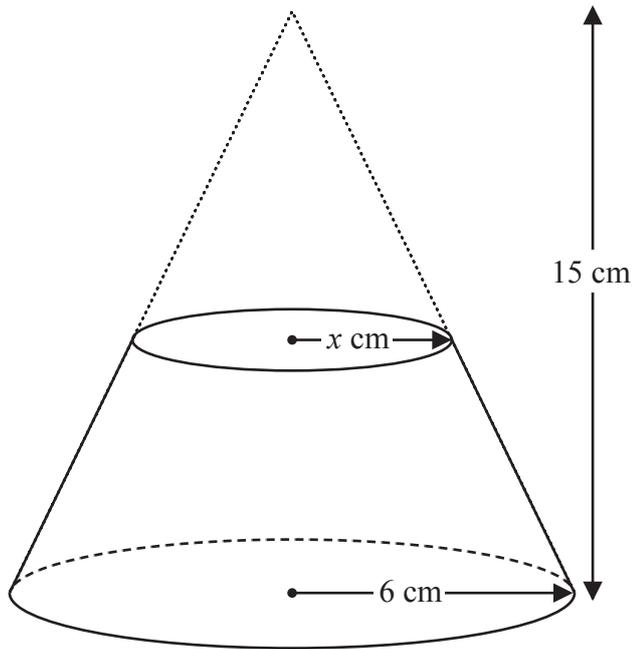


Diagram **NOT**  
accurately drawn

The height of the large cone is 15 cm.

The radius of the base of the large cone is 6 cm.

The radius of the base of the small cone is  $x$  cm.

Given that the volume of the frustum is  $\frac{4212}{25}\pi \text{ cm}^3$

work out the value of  $x$

Show clear algebraic working.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

$$x = \dots\dots\dots$$

**(Total for Question 23 is 5 marks)**

---

**Turn over for Question 24**



24 Solve  $\frac{45x^3 - 80x}{3x^2 + x - 4} \times \left( \frac{1}{3x - 4} + \frac{1}{x} \right) = \frac{4(x + 2)}{5x - 8}$

Show clear algebraic working.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

$x = \dots\dots\dots$

(Total for Question 24 is 5 marks)

TOTAL FOR PAPER IS 100 MARKS

