

**CAMBRIDGE INTERNATIONAL EXAMINATIONS****Cambridge International Advanced Level****MARK SCHEME for the May/June 2015 series****9231 FURTHER MATHEMATICS****9231/23**

Paper 2, maximum raw mark 100

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2015 series for most Cambridge IGCSE<sup>®</sup>, Cambridge International A and AS Level components and some Cambridge O Level components.

® IGCSE is the registered trademark of Cambridge International Examinations.

| Page 2 | Mark Scheme                                     | Syllabus | Paper |
|--------|-------------------------------------------------|----------|-------|
|        | Cambridge International A Level – May/June 2015 | 9231     | 23    |

### **Mark Scheme Notes**

Marks are of the following three types:

**M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

**A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

**B** Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol  $\nabla$  implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.  
B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking  $g$  equal to 9.8 or 9.81 instead of 10.

| Page 3 | Mark Scheme                                     | Syllabus | Paper |
|--------|-------------------------------------------------|----------|-------|
|        | Cambridge International A Level – May/June 2015 | 9231     | 23    |

The following abbreviations may be used in a mark scheme or used on the scripts:

|     |                                                                                                                                                                                         |
|-----|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| AEF | Any Equivalent Form (of answer is equally acceptable)                                                                                                                                   |
| AG  | Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)                                                     |
| BOD | Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)                                                                                                  |
| CAO | Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)                                                                                             |
| CWO | Correct Working Only – often written by a "fortuitous" answer                                                                                                                           |
| ISW | Ignore Subsequent Working                                                                                                                                                               |
| MR  | Misread                                                                                                                                                                                 |
| PA  | Premature Approximation (resulting in basically correct work that is insufficiently accurate)                                                                                           |
| SOS | See Other Solution (the candidate makes a better attempt at the same question)                                                                                                          |
| SR  | Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance) |

### **Penalties**

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR–2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

| Page 4 | Mark Scheme                                     | Syllabus | Paper |
|--------|-------------------------------------------------|----------|-------|
|        | Cambridge International A Level – May/June 2015 | 9231     | 23    |

| Question Number | Mark Scheme Details                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | Part Mark   | Total |
|-----------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------|-------|
| 1               | <p>Find speed <math>u_A</math> [<math>\text{m s}^{-1}</math>] of <math>A</math> after initial impulse: <math>2u_A = 8, u_A = 4</math> B1</p> <p>For <math>A</math> &amp; <math>B</math> use conservation of momentum, e.g.: <math>2v_A + 3v_B = 2u_A</math> [= 8] M1</p> <p>Use Newton's law of restitution (consistent signs): <math>v_B - v_A = eu_A</math> [= <math>4e</math>] M1</p> <p>Combine to find <math>v_A</math> and <math>v_B</math>: <math>v_A = (2-3e)u_A/5, v_B = 2(1+e)u_A/5</math> A1</p> <p>(AEF) <math>v_A = 4(2-3e)/5, v_B = 8(1+e)/5</math> A1</p> <p>Use <math>v_A &lt; 0</math>: <math>2-3e &lt; 0, e &gt; 2/3</math> <b>AG</b> B1</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 5<br>1      | 6     |
| 2               | <p><i>EITHER</i>: Find/ state comps. of speed after 1<sup>st</sup> colln.: <math>u \cos \alpha</math> // to <math>A</math> and <math>eu \sin \alpha \perp</math> to <math>A</math> M1 A1</p> <p>Find/ state comps. of speed after 2<sup>nd</sup> colln.: <math>eu \sin \alpha</math> // to <math>B</math> and <math>eu \cos \alpha \perp</math> to A1</p> <p>Find final angle with barrier <math>B</math>: <b>AG</b> <math>\tan^{-1}(eu \cos \alpha / eu \sin \alpha) = \frac{1}{2}\pi - \alpha</math> A1</p> <p><i>OR</i>: Relate angle <math>\beta_1</math> after 1<sup>st</sup> colln. to <math>\alpha</math>: <math>v_1 \sin \beta_1 = eu \sin \alpha</math></p> <p><math>v_1 \cos \beta_1 = u \cos \alpha</math></p> <p><math>\tan \beta_1 = e \tan \alpha</math> (M1 A1)</p> <p>Relate angle <math>\beta_2</math> after 2<sup>nd</sup> colln. to <math>\beta_1</math>: <math>v_2 \sin \beta_2 = ev_1 \cos \beta_1</math></p> <p><math>v_2 \cos \beta_2 = v_1 \sin \beta_1</math></p> <p><math>\tan \beta_2 = e / \tan \beta_1</math> (A1)</p> <p>Find final angle <math>\beta_2</math> with barrier <math>B</math>: <b>AG</b> <math>\tan^{-1}(e / e \tan \alpha) = \frac{1}{2}\pi - \alpha</math> (A1)</p> <p><i>EITHER</i>: Find total loss or gain in KE, e.g.: <math>\frac{1}{2} m \{u^2 - (eu \sin \alpha)^2 - (eu \cos \alpha)^2\}</math> M1 A1</p> <p>Find total loss in KE (A0 if wrong sign): <math>= \frac{1}{2} m (1 - e^2) u^2</math> A1</p> <p><i>OR</i>: Find or state final speed <math>u_{\text{final}}</math>: <math>u_{\text{final}} = eu</math> (B1)</p> <p>Find total loss in KE (A0 if wrong sign): <math>\frac{1}{2} m (u^2 - u_{\text{final}}^2) = \frac{1}{2} m (1 - e^2) u^2</math> (M1 A1)</p>                                                                                                                                                                                                                                                                                                                                                 | 4<br>3      | 7     |
| 3               | <p>State or imply posn. where max. speed next attained: Centre O M1</p> <p><i>EITHER</i>: Find <math>\omega</math> from SHM eqn. <math>x = a \sin \omega t</math>, e.g.: <math>1 = \omega^{-1} \sin^{-1} \frac{1}{2}, \omega = \pi/6</math> M1 A1</p> <p>Find period <math>T</math> from <math>T = 2\pi/\omega</math>: [ft on <math>\omega</math>] <math>T = 2\pi/(\pi/6) = 12</math> [s] B1✓</p> <p><i>OR</i>: Find <math>\omega</math> from SHM eqn. <math>x = a \cos \omega t</math>, e.g.: <math>1 = \omega^{-1} \cos^{-1} 0 - \omega^{-1} \cos^{-1} \frac{1}{2}</math></p> <p><math>\omega = \pi/2 - \pi/3 = \pi/6</math> M1 A1</p> <p>Find period <math>T</math> from <math>T = 2\pi/\omega</math>: [ft on <math>\omega</math>] <math>T = 2\pi/(\pi/6) = 12</math> [s] B1✓</p> <p><i>OR</i>: Find period <math>T</math> from SHM eqn, e.g.: <math>1 = T/4 - (T/2\pi) \cos^{-1} \frac{1}{2}</math> M1 A1</p> <p><math>= T(1/4 - 1/6), T = 12</math> [s] A1</p> <p>Find distance <math>x</math> from O when speed is half max:</p> <p><math>\omega^2 (a^2 - x^2) = \frac{1}{4} v_{\text{max}}^2</math> M1</p> <p>Use maximum speed: <math>v_{\text{max}} = a\omega</math> [= <math>\pi a/6</math>] M1</p> <p>(note that <math>x</math> is independent of <math>\omega</math>) <math>x^2 = \frac{3}{4} a^2</math></p> <p><math>x = \sqrt{3}a/2</math></p> <p>or <math>a\sqrt{3/4}</math> or <math>0.866a</math> A1</p> <p><i>EITHER</i>: Find <math>a</math> from <math>x = a \sin \omega t</math>: <math>2.5 = \omega^{-1} \sin^{-1}(\sqrt{2}/a) - \omega^{-1} \sin^{-1}(-\frac{1}{2})</math></p> <p>or <math>1.5 = \omega^{-1} \sin^{-1}(\sqrt{2}/a)</math></p> <p><math>\sin^{-1}(\sqrt{2}/a) = \pi/4, a = 2</math> [m] M1 A1</p> <p><i>OR</i>: Find <math>a</math> from <math>x = a \cos \omega t</math>: <math>2.5 = \omega^{-1} \cos^{-1}(-\sqrt{2}/a) - \omega^{-1} \cos^{-1} \frac{1}{2}</math></p> <p>or <math>1.5 = \omega^{-1} \cos^{-1}(-\sqrt{2}/a) - \omega^{-1} \cos^{-1} 0</math></p> <p><math>\cos^{-1}(-\sqrt{2}/a) = 3\pi/4, a = 2</math> [m] M1 A1</p> | 4<br>3<br>2 | 9     |

| Page 5 | Mark Scheme                                     | Syllabus | Paper |
|--------|-------------------------------------------------|----------|-------|
|        | Cambridge International A Level – May/June 2015 | 9231     | 23    |

| Question Number | Mark Scheme Details                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | Part Mark | Total |
|-----------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------|-------|
| 4               | <p>Find reaction at <math>C</math> using moments for rod about <math>A</math>: <math>R_C \times 2a / \sin 30^\circ = W \times 3a \cos 30^\circ</math><br/> <math>R_C = 3\sqrt{3}W / 8</math> M1 A1</p> <p>Find friction <math>F</math> on cube by resolving horizontally: <math>F = R_C \sin 30^\circ [= 3\sqrt{3}W / 16]</math> B1</p> <p>Find reaction <math>R</math> on cube by resolving vertically: <math>R = W + R_C \cos 30^\circ [= 25W / 16]</math> B1</p> <p>Use <math>F \leq \mu R</math> (allow <math>F &lt; \mu R</math> for M1): <b>AG</b> <math>3\sqrt{3}/16 \leq 25\mu/16, \mu \geq 3\sqrt{3}/25</math> M1 A1<br/> (M0 if <math>F = \mu R</math> with no further explanation)</p> <p>Find horizontal force <math>X</math> at <math>A</math> (ignore sign): <math>X = F [= 3\sqrt{3}W / 16]</math> B1</p> <p>Find vertical force <math>Y</math> at <math>A</math> (ignore sign): <math>Y = 2W - R</math> or <math>W - R_C \cos 30^\circ</math><br/> <math>[= 7W/16]</math> B1</p> <p>Find magnitude of force at <math>A</math>: <math>\sqrt{(X^2 + Y^2)} = (\sqrt{19/8}) W</math> or <math>0.545W</math> M1 A1</p>                                                                                                                                                                                                                                                                                               |           | 10    |
| 5               | <p>State or find MI of rod about <math>A</math>: <math>I_{\text{rod}} = (1 + \frac{1}{3}) 3M(2a)^2</math><br/> or <math>\frac{1}{3} 3M(4a)^2 [= 16Ma^2]</math> B1</p> <p>Find MI of disc about <math>A</math>: <math>I_{\text{disc}} = \frac{1}{2} 2M a^2 + 2M(5a)^2</math><br/> <math>[= 51 Ma^2]</math> M1 A1</p> <p>State MI of particle about <math>A</math>: <math>I_{\text{particle}} = M(ka)^2</math> B1</p> <p>Sum to find MI of system about <math>A</math>: <math>I = (16 + 51 + k^2) Ma^2</math><br/> <math>= (67 + k^2) Ma^2</math> <b>AG</b> A1</p> <p>Use eqn of circular motion to find <math>d^2\theta/dt^2</math> where <math>\theta</math> is angle of <math>AO</math> with vertical:<br/> (A0 if <math>\cos \theta</math> used) <math>[-] I d^2\theta/dt^2 = 3Mg \times 2a \sin \theta</math><br/> <math>+ 2Mg \times 5a \sin \theta + Mg \times ka \sin \theta</math><br/> <math>= (16 + k) Mga \sin \theta</math> M1 A1</p> <p>[Approximate <math>\sin \theta</math> by <math>\theta</math> and] find <math>\omega^2</math> in SHM eqn: <math>\omega^2 = (16 + k)g / (67 + k^2) a</math> M1 A1<br/> (A0 if <math>\cos \theta \approx \theta</math> used)</p> <p>Equate <math>2\pi/\omega</math> to <math>4\pi\sqrt{(a/g)}</math> to find possible values of <math>k</math>: <math>\omega^2 = \frac{1}{4} g/a, 16 + k = \frac{1}{4}(67 + k^2)</math><br/> <math>k^2 - 4k + 3 = 0, k = 1, 3</math> M1 A1</p> | 5         | 11    |
| 6               | <p>State (at least) null hypothesis (AEF): <math>H_0</math>: Reliability is independent B1</p> <p>Find expected values (to 1 d.p.):<br/> (lose A1 if rounded to integers) 62.253 57.423 41.323<br/> 53.747 49.577 35.677 M1 A1</p> <p>Calculate value of <math>\chi^2</math>:<br/> <math>\chi^2 = 0.1212 + 0.5416 + 1.6764</math><br/> <math>+ 0.1404 + 0.6274 + 1.9417</math><br/> <math>= 5.05</math> M1 A1<br/> (allow 5.03 if 1 d.p. exp. values used)</p> <p>State or use correct tabular <math>\chi^2</math> value (to 3 s.f.): <math>\chi_{2, 0.95}^2 = 5.99[1]</math> B1</p> <p>Valid method for reaching conclusion: Accept <math>H_0</math> if <math>\chi^2 &lt; \text{tabular value}</math> M1</p> <p>Correct conclusion, from correct values: (AEF) Reliability is indep. of supplier A1</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 8         | 8     |
| 7               | <p>Find gradient <math>b_2</math> of line <math>x</math> on <math>y</math> from <math>b_1b_2 = r^2</math>: <math>3.25 b_2 = 0.56^2, b_2 = 0.0965</math> M1 A1</p> <p>Find <math>\bar{y}</math> from line <math>y</math> on <math>x</math>: <math>y = 3.25 \times (15.6/10) - 4.27 = 0.8</math> M1 A1</p> <p>Find regression line of <math>x</math> on <math>y</math>:<br/> (M0 for <math>y</math> on <math>x</math>) <math>(x - \bar{x} = b_2 (y - \bar{y}))</math><br/> <math>(x - 1.56) = 0.0965 (y - 0.8)</math> M1 A1<br/> <math>x = 0.0965y + 1.48</math> A1</p> <p>State both hypotheses (B0 for <math>r \dots</math>): <math>H_0: \rho = 0, H_1: \rho \neq 0</math> B1</p> <p>State or use correct tabular two-tail <math>r</math>-value: <math>r_{10, 5\%} = 0.632</math> *B1</p> <p>State or imply valid method for reaching conclusion: Accept <math>H_0</math> if <math>0.56 &lt; r\text{-value}</math> (AEF) M1</p> <p>Correct conclusion (AEF, dep *B1): There is no non-zero correlation A1</p>                                                                                                                                                                                                                                                                                                                                                                                                                   | 7         | 11    |

| Page 6 | Mark Scheme                                     | Syllabus | Paper |
|--------|-------------------------------------------------|----------|-------|
|        | Cambridge International A Level – May/June 2015 | 9231     | 23    |

| Question Number | Mark Scheme Details                                                                                                                          | Part Mark | Total |
|-----------------|----------------------------------------------------------------------------------------------------------------------------------------------|-----------|-------|
| 8               | Calculate sample mean: $\bar{x} = 45.29 / 7 = 6.47$ M1                                                                                       |           |       |
|                 | Estimate population variance: $s_1^2 = (295.36 - 45.29^2 / 7) / 6 = 0.389 \text{ or } 0.6236^2$ M1                                           |           |       |
|                 | (allow biased here: 0.3334 or 0.5774 <sup>2</sup> )                                                                                          |           |       |
|                 | State hypotheses: (AEF; B0 for $\bar{x}$ ) $H_0: \mu = 6.2, H_1: \mu > 6.2$ B1                                                               |           |       |
|                 | Calculate value of $t$ (or $-t$ ; to 3 s.f.): $t = (\bar{x} - 6.2) / (s_1 / \sqrt{7}) = 1.15$ M1 A1                                          |           |       |
|                 | State or use correct tabular $t$ -value (to 3 s.f.): $t_{6, 0.95} = 1.94[3]$ B1                                                              |           |       |
|                 | (or can compare $\bar{x}$ with $6.2 + 0.458 = 6.66$ )                                                                                        |           |       |
|                 | Consistent conclusion (AEF, fit on both $t$ -values): [Accept $H_0$ ]                                                                        |           |       |
|                 | Popn. mean not greater than 6.2 B1                                                                                                           |           |       |
|                 | Find estimate of population mean: $\frac{1}{2} (5.89 + 6.75) = 6.32$ M1 A1                                                                   | 7         |       |
|                 | Find estimate of population variance $s_2^2$ : $t \sqrt{(s_2^2 / 8)} = \frac{1}{2} (6.75 - 5.89) [= 0.43]$ M1                                |           |       |
|                 | <b>SR</b> Allow M1 for $t \sqrt{(s_2^2 / 7)}$ , max 4/5                                                                                      |           |       |
|                 | Use of correct tabular value: $t_{7, 0.975} = 2.36[5]$ A1                                                                                    |           |       |
|                 | (Use of 2.36 may lose final A1)                                                                                                              |           |       |
|                 | (to 3 d.p.) $s_2^2 = 0.2645 \text{ or } 32/121$ A1                                                                                           | 5         | 12    |
| 9               | Find $a$ by equating $\int_2^\infty f(x)dx$ to 1: $[-ae^{-(x-2)}]_2^\infty = a = 1$ AG B1                                                    | 1         |       |
|                 | Find or state distribution function $F(x)$ for $x \geq 2$ : $F(x) = \int f(x) dx = -ae^{-(x-2)} + c$ M1 A1                                   |           |       |
|                 | State $F(x)$ for $x < 2$ : $F(x) = 0$ for $x < 2$ A1                                                                                         |           |       |
|                 | Find median value $m$ from $F(m) = \frac{1}{2}$ : $1 - e^{-(m-2)} = \frac{1}{2}, e^{m-2} = 2$ M1 A1                                          | 5         |       |
|                 | $m = 2 + \ln 2 \text{ or } 2 - \ln \frac{1}{2} \text{ or } 2.69$                                                                             |           |       |
| (i)             | Find or state $G(y)$ from $Y = e^X$ for $x \geq 2$ : $G(y) = P(Y < y) = P(e^X < y)$ M1 A1                                                    |           |       |
|                 | $= P(X < \ln y) = F(\ln y)$                                                                                                                  |           |       |
|                 | $= 1 - e^{-(\ln y - 2)} = 1 - e^2/y$                                                                                                         |           |       |
|                 | Find $g(y)$ by differentiation (allow $e^2 = 7.39$ ): $g(y) = e^2/y^2$ A1                                                                    |           |       |
|                 | State corresponding range of $y$ : for $y \geq e^2$ [ $g(y) = 0$ for $y < e^2$ ] A1                                                          | 4         |       |
| (ii)            | Find $P(Y > 10)$ : $P(Y > 10) = 1 - G(10)$ M1 A1                                                                                             |           |       |
|                 | M0 for $G(10)$ or $1 - g(10)$ $= e^2/10 \text{ or } 0.739$                                                                                   | 2         | 12    |
| 10A             | Use conservation of energy when $P$ is level with $A$ : $\frac{1}{2}mv_1^2 = \frac{1}{2}mu^2 - \frac{1}{2}mga$ B1                            |           |       |
|                 | Use $F = ma$ radially at this point: $T_1 = mv_1^2 / \frac{1}{2}a$ B1                                                                        |           |       |
|                 | Eliminate $v_1^2$ to find $T_1$ : $T_1 = (2m/a)(u^2 - ag)$ AG B1                                                                             | 3         |       |
| (i)             | State or imply that string loses contact when vertical M1                                                                                    |           |       |
|                 | Use conservation of energy at this point: $\frac{1}{2}mv_2^2 = \frac{1}{2}mu^2 - mga$ B1                                                     |           |       |
|                 | Use $F = ma$ radially just before this point: $T_2 = mv_2^2 / \frac{1}{2}a - mg$ B1                                                          |           |       |
|                 | Use $F = ma$ radially just after this point: $T_3 = mv_2^2 / (3a/2) - mg$ B1                                                                 |           |       |
|                 | <b>EITHER:</b> Find $v_2^2$ and hence $u^2$ from $T_2/T_3 = 5$ : $mv_2^2 / \frac{1}{2}a - mg = 5\{mv_2^2 / (3a/2) - mg\}, v_2^2 = 3ag$ M1 A1 |           |       |
|                 | $u^2 = 3ag + 2ag = 5ag$ AG                                                                                                                   |           |       |
|                 | <b>OR:</b> Eliminate $v_2^2$ in $T_2/T_3 = 5$ and find $u^2$ : $(m/a)(2u^2 - 5ag) = 5(m/a)(2u^2/3 - 7ag/3)$ M1 A1                            |           |       |
|                 | $4u^2/3 = 20ag/3, u^2 = 5ag$ AG (M1 A1)                                                                                                      | 6         |       |

|               |                                                        |                 |              |
|---------------|--------------------------------------------------------|-----------------|--------------|
| <b>Page 7</b> | <b>Mark Scheme</b>                                     | <b>Syllabus</b> | <b>Paper</b> |
|               | <b>Cambridge International A Level – May/June 2015</b> | <b>9231</b>     | <b>23</b>    |

[illegible]