



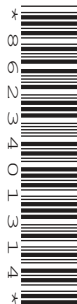
Cambridge International AS & A Level

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NAME
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**FURTHER MATHEMATICS****9231/33**

Paper 3 Further Mechanics

May/June 2020**1 hour 30 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity (g) is needed, use 10 ms^{-2} .

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Blank pages are indicated.

- 1 A particle P of mass m is attached to one end of a light inextensible string of length a . The other end of the string is attached to a fixed point O on a smooth horizontal plane. The particle P moves in horizontal circles about O . The tension in the string is $4mg$.

Find, in terms of a and g , the time that P takes to make one complete revolution. [2]

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- 2 A particle Q of mass m kg falls from rest under gravity. The motion of Q is resisted by a force of magnitude mkv N, where $v\text{ ms}^{-1}$ is the speed of Q at time t s and k is a positive constant.

Find an expression for v in terms of g , k and t . [6]

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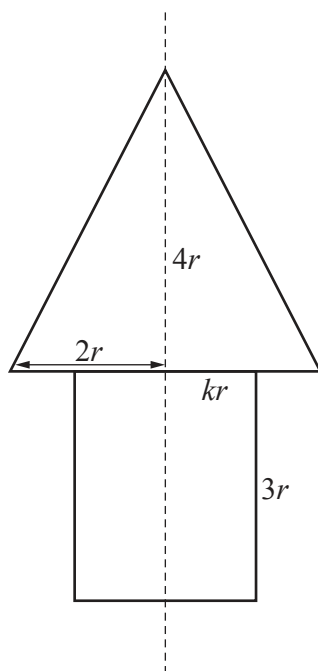
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This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.

This image shows a full page of a handwriting practice worksheet. It consists of approximately 20 horizontal rows. Each row is defined by two parallel dashed lines, creating a series of uniform gaps for letter height. The lines are evenly spaced across the entire page, providing a guide for consistent letter formation. There is no text or other markings on the page.

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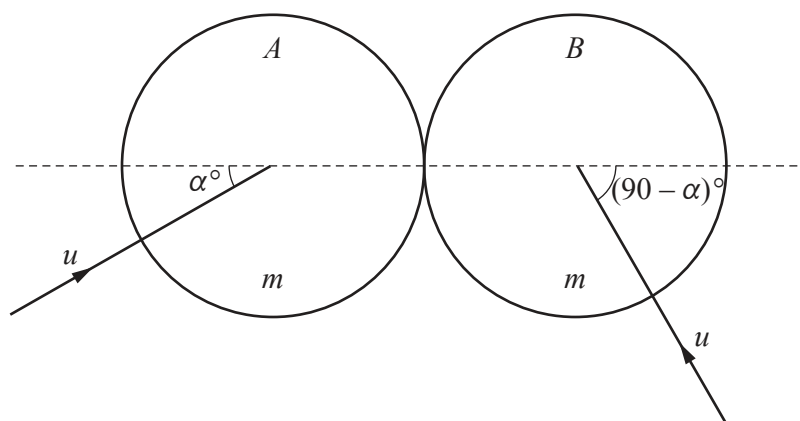


A uniform solid circular cone, of vertical height $4r$ and radius $2r$, is attached to a uniform solid cylinder, of height $3r$ and radius kr , where k is a constant less than 2. The base of the cone is joined to one of the circular faces of the cylinder so that the axes of symmetry of the two solids coincide (see diagram). The cone and the cylinder are made of the same material.

- (a) Show that the distance of the centre of mass of the combined solid from the vertex of the cone is $\frac{(99k^2 + 96)r}{18k^2 + 32}$. [4]

[illegible]

- [illegible]



Immediately after the collision, B moves in a direction at right angles to the line of centres.

- (a) Show that $\tan \alpha = \frac{1+e}{1-e}$. [4]

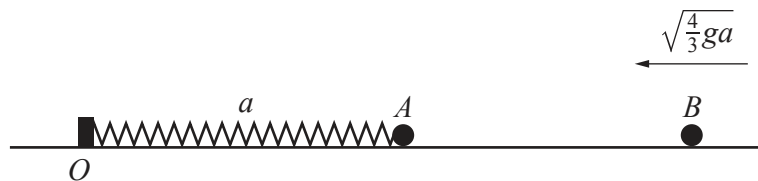
[illegible]

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One end of a light spring of natural length a and modulus of elasticity $4mg$ is attached to a fixed point O . The other end of the spring is attached to a particle A of mass km , where k is a constant. Initially the spring lies at rest on a smooth horizontal surface and has length a . A second particle B , of mass m , is moving towards A with speed $\sqrt{\frac{4}{3}ga}$ along the line of the spring from the opposite direction to O (see diagram).

The particles A and B collide and coalesce. At a point C in the subsequent motion, the length of the spring is $\frac{3}{4}a$ and the speed of the combined particle is half of its initial speed.

- (a) Find the value of k .

[6]

[4]

[illegible]

[illegible]

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