



Cambridge International AS & A Level

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FURTHER MATHEMATICS

9231/42

Paper 4 Further Probability & Statistics

October/November 2020

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **12** pages. Blank pages are indicated.

- $$\bar{x} = 176.2 \qquad \sum(x - \bar{x})^2 = 313.1$$

Test, at the 5% significance level, the null hypothesis that the population mean height for members of this club is equal to 172.5 cm against the alternative hypothesis that the mean differs from 172.5 cm. [5]

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.

- 2 A large school is holding an essay competition and each student has submitted an essay. To ensure fairness, each essay is given a mark out of 100 by two different judges. The marks awarded to the essays submitted by a random sample of 12 students are shown in the following table.

Student	<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>F</i>	<i>G</i>	<i>H</i>	<i>I</i>	<i>J</i>	<i>K</i>	<i>L</i>
Judge 1	62	74	52	48	68	55	56	64	37	70	81	59
Judge 2	65	70	47	49	76	74	67	54	50	77	72	75

- (a) One of the students claims that Judge 2 is awarding higher marks than Judge 1.

Carry out a Wilcoxon matched-pairs signed-rank test at the 5% significance level to test whether the data supports the student’s claim. [7]

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It is discovered later that the marks awarded to student *A* have been entered incorrectly. In fact, Judge 1 awarded 65 marks and Judge 2 awarded 62 marks.

- (b) By considering how this change affects the test statistic, explain why the conclusion of the test carried out in part (a) remains the same. [2]

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It is required to test the goodness of fit of the distribution with probability density function f given by

Most of the relevant expected frequencies, correct to 2 decimal places, are given in the following table.

(a) Show that $p = 10.19$ and find the value of q . [3]

[illegible]

[illegible]

4 The continuous random variable X has cumulative distribution function F given by

$$F(x) = \begin{cases} 0 & x < 2, \\ \frac{1}{60}x^2 - \frac{1}{15} & 2 \leq x \leq 8, \\ 1 & x > 8. \end{cases}$$

(a) Find $P(3 \leq X \leq 6)$. [1]

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(b) Find $E(\sqrt{X})$. [3]

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- (c) Find $\text{Var}(\sqrt{X})$. [2]

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- (d) The random variable Y is defined by $Y = X^3$. Find the probability density function of Y . [3]

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This image shows a full page of a worksheet designed for handwriting practice. It features approximately 20 evenly spaced horizontal dotted lines across the entire page, providing a guide for letter height and placement. The background is plain white, and there are no other markings or text present.

- 6 Nassa is researching the lengths of a particular type of snake in two countries, A and B .
- (a) He takes a random sample of 10 snakes of this type from country A and measures the length, x m, of each snake. He then calculates a 90% confidence interval for the population mean length, μ m, for snakes of this type, assuming that snake lengths have a normal distribution. This confidence interval is $3.36 \leq \mu \leq 4.22$.

Find the sample mean and an unbiased estimate for the population variance. [4]

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- (b) Nassa also measures the lengths, y m, of a random sample of 8 snakes of this type taken from country B . His results are summarised as follows.

$\Sigma y = 27.86 \qquad \Sigma y^2 = 98.02$

Nassa claims that the mean length of snakes of this type in country B is less than the mean length of snakes of this type in country A . Nassa assumes that his sample from country B also comes from a normal distribution, with the same variance as the distribution from country A .

Test at the 10% significance level whether there is evidence to support Nassa’s claim. [8]

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