



Cambridge International AS & A Level

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FURTHER MATHEMATICS**9231/32**

Paper 3 Further Mechanics

October/November 2023**1 hour 30 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

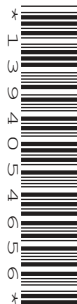
INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity (g) is needed, use 10 ms^{-2} .

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Any blank pages are indicated.



[4]

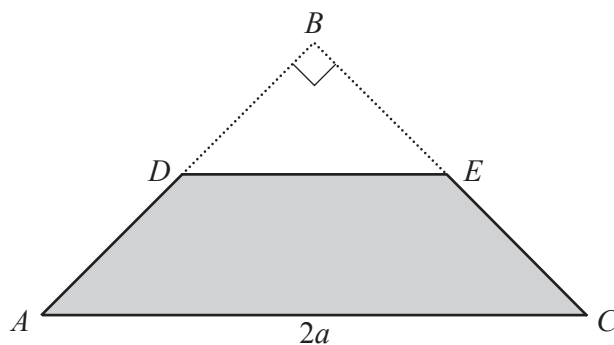
[illegible]

Find v in terms of x , giving your answer in the form $v = \frac{Ax+B}{(x+1)}$, where A and B are constants to be determined. [6]

[illegible]

4

3



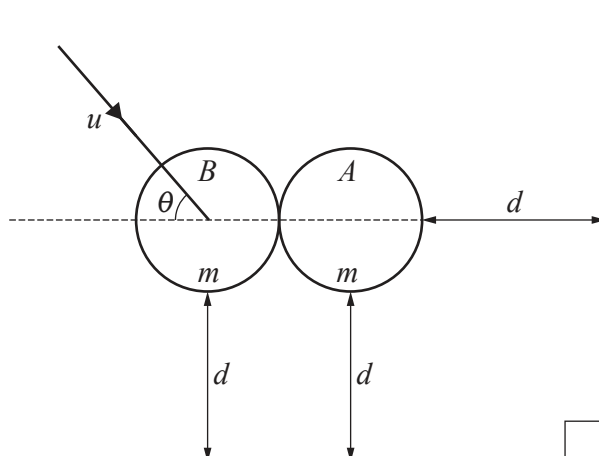
A uniform lamina is in the form of an isosceles triangle ABC in which $AC = 2a$ and angle $ABC = 90^\circ$. The point D on AB is such that the ratio $DB:AB = 1:k$. The point E on CB is such that DE is parallel to AC . The triangle DBE is removed from the lamina (see diagram).

- (a) Find, in terms of k , the distance of the centre of mass of the remaining lamina $ADEC$ from the midpoint of AC . [4]

[illegible]

[3]

This image shows a full page of a worksheet designed for handwriting practice. It consists of approximately 20 horizontal rows. Each row is defined by two parallel dotted lines, creating a series of uniform gaps for writing. The entire page is otherwise blank, with no text or other markings.



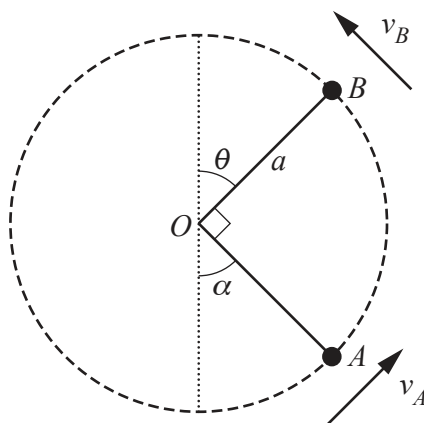
(a) Find the value of $\tan \theta$.

[4]

[illegible]

[illegible]

5



A bead of mass m moves on a smooth circular wire, with centre O and radius a , in a vertical plane. The bead has speed v_A when it is at the point A where OA makes an angle α with the downward vertical through O , and $\cos \alpha = \frac{3}{5}$. Subsequently the bead has speed v_B at the point B , where OB makes an angle θ with the upward vertical through O . Angle AOB is a right angle (see diagram). The reaction of the wire on the bead at B is in the direction OB and has magnitude equal to $\frac{1}{6}$ of the magnitude of the reaction when the bead is at A .

- (a) Find, in terms of m and g , the magnitude of the reaction at B . [6]

[illegible]

- [illegible]

6 A particle P is projected with speed u at an angle α above the horizontal from a point O on a horizontal plane and moves freely under gravity. The horizontal and vertical displacements of P from O at a subsequent time t are denoted by x and y respectively.

(a) Derive the equation of the trajectory of P in the form

$$y = x \tan \alpha - \frac{gx^2}{2u^2} \sec^2 \alpha.$$

[3]

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During its flight, P must clear an obstacle of height h m that is at a horizontal distance of 32 m from the point of projection. When $u = 40\sqrt{2} \text{ m s}^{-1}$, P just clears the obstacle. When $u = 40 \text{ m s}^{-1}$, P only achieves 80% of the height required to clear the obstacle.

(b) Find the two possible values of h . [6]

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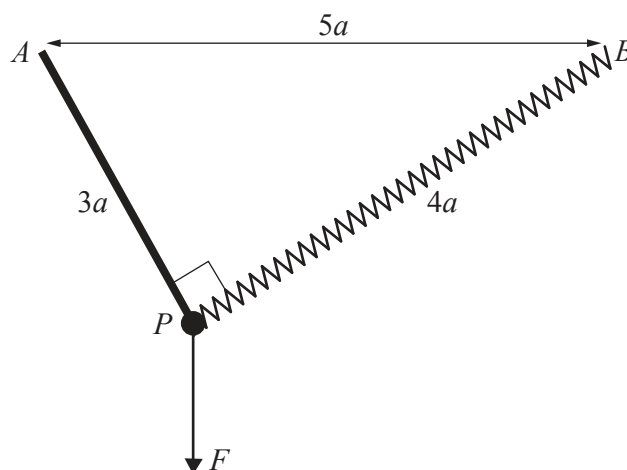
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Initially, P is held in equilibrium by a vertical force F with the stretched length of the spring equal to $4a$ (see diagram). The particle is released from rest in this position and has a speed of $\frac{6}{5}\sqrt{2ag}$ when the rod becomes horizontal.

- (a) Find the value of k . [5]

[illegible]

(b) Find F in terms of m and g . [2]

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(c) Find, in terms of m and g , the tension in the rod immediately before it is released. [2]

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