

Cambridge Assessment
International Education

Cambridge International AS & A Level

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FURTHER MATHEMATICS**9231/31**

Paper 3 Further Mechanics

October/November 2024**1 hour 30 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity (g) is needed, use 10 ms^{-2} .

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Any blank pages are indicated.



- 1** A particle P is projected with speed $u \text{ m s}^{-1}$ at an angle $\tan^{-1}2$ above the horizontal from a point O on a horizontal plane and moves freely under gravity. When P has travelled a distance 56 m horizontally from O , it is at a vertical height $H \text{ m}$ above the plane. When P has travelled a distance 84 m horizontally from O , it is at a vertical height $\frac{1}{2}H \text{ m}$ above the plane.

Find, in either order, the value of u and the value of H .

[5]

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.



Find T in terms of m and g .

[5]

[illegible]



- 3 A particle P of mass m kg is attached to one end of a light elastic string of natural length 2 m and modulus of elasticity $2mg$ N. The other end of the string is attached to a fixed point O . The particle P hangs in equilibrium vertically below O . The particle P is pulled down vertically a distance d m below its equilibrium position and released from rest.

(a) Given that the particle just reaches O in the subsequent motion, find the value of d . [6]

[illegible]



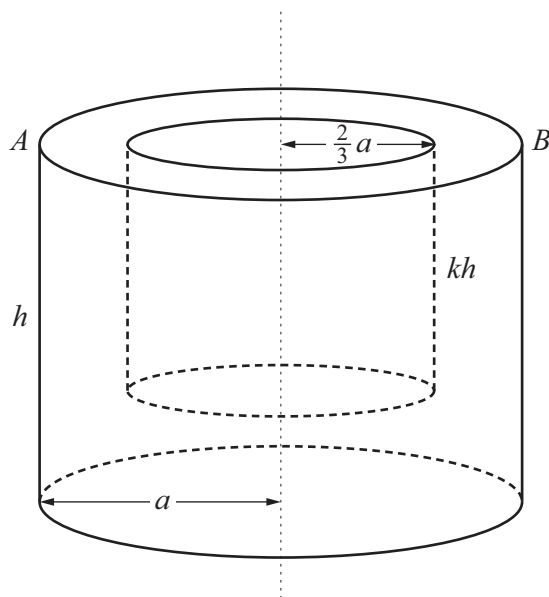
5

(b) Hence find the speed of P when it is 2 m below O .

[2]

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An object is formed by removing a cylinder of radius $\frac{2}{3}a$ and height kh ($k < 1$) from a uniform solid cylinder of radius a and height h . The vertical axes of symmetry of the two cylinders coincide. The upper faces of the two cylinders are in the same plane as each other. The points A and B are the opposite ends of a diameter of the upper face of the object (see diagram).

- (a) Find, in terms of h and k , the distance of the centre of mass of the object from AB . [4]

This image shows a full page of a handwriting practice worksheet. It consists of multiple sets of three horizontal dashed lines, providing a guide for letter height and placement. The lines are evenly spaced across the entire page, which is otherwise blank.



(b) Given that $h = \frac{8}{3}a$, find the possible values of k . [3]

[illegible]



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$$\frac{v}{x} = \frac{3-t}{1+t}$$

and when $t = 0, x = 5$.

- (a) Find an expression for x in terms of t .

[4]

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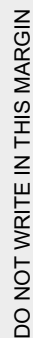
(b) Find the magnitude of F when $t = 3$.

[3]

[illegible]



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(b) Find the value of ω . [3]

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(c) Find the value of β . [2]

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- 7 A particle P is projected with speed u at an angle $\tan^{-1}\left(\frac{4}{3}\right)$ above the horizontal from a point O on a horizontal plane and moves freely under gravity. When P is moving horizontally, it strikes a smooth inclined plane at the point A . This plane is inclined to the horizontal at an angle α , and the line of greatest slope through A lies in the vertical plane through O and A .

As a result of the impact, P moves vertically upwards. The coefficient of restitution between P and the inclined plane is e .

- (a) Show that $e \tan^2 \alpha = 1$. [4]

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In its subsequent motion, the greatest height reached by P above A is $\frac{3}{16}$ of the vertical height of A above the horizontal plane.

(b) Find the value of e .

[6]

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