



# Cambridge International AS & A Level

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**FURTHER MATHEMATICS****9231/44**

Paper 4 Further Probability &amp; Statistics

**May/June 2025**

MARK SCHEME

Maximum Mark: 50

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**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2025 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

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This document consists of **15** printed pages.

**PUBLISHED****Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

**GENERIC MARKING PRINCIPLE 1:**

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

**GENERIC MARKING PRINCIPLE 2:**

Marks awarded are always **whole marks** (not half marks, or other fractions).

**GENERIC MARKING PRINCIPLE 3:**

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

**GENERIC MARKING PRINCIPLE 4:**

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

**GENERIC MARKING PRINCIPLE 5:**

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

**GENERIC MARKING PRINCIPLE 6:**

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

**Mathematics Specific Marking Principles**

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (ISW).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number or sign does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

**Annotations guidance for centres**

Examiners use a system of annotations as a shorthand for communicating their marking decisions to one another. Examiners are trained during the standardisation process on how and when to use annotations. The purpose of annotations is to inform the standardisation and monitoring processes and guide the supervising examiners when they are checking the work of examiners within their team. The meaning of annotations and how they are used is specific to each component and is understood by all examiners who mark the component.

We publish annotations in our mark schemes to help centres understand the annotations they may see on copies of scripts. Note that there may not be a direct correlation between the number of annotations on a script and the mark awarded. Similarly, the use of an annotation may not be an indication of the quality of the response.

The annotations listed below were available to examiners marking this component in this series.

**Annotations**

| Annotation                                                                          | Meaning                                |
|-------------------------------------------------------------------------------------|----------------------------------------|
|    | More information required              |
|    | Accuracy mark awarded zero             |
|    | Accuracy mark awarded one              |
|    | Independent accuracy mark awarded zero |
|  | Independent accuracy mark awarded one  |
|  | Independent accuracy mark awarded two  |
|  | Benefit of the doubt                   |
|  | Blank Page                             |
|  | Incorrect                              |
| Dep                                                                                 | Used to indicate DM0 or DM1            |

| <b>Annotation</b>                                                                   | <b>Meaning</b>                                                                                                                             |
|-------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------|
| DM1                                                                                 | Dependent on the previous M1 mark(s)                                                                                                       |
|    | Follow through                                                                                                                             |
|    | Indicate working that is right or wrong                                                                                                    |
| Highlighter                                                                         | Highlight a key point in the working                                                                                                       |
|    | Ignore subsequent work                                                                                                                     |
|    | Judgement                                                                                                                                  |
|    | Judgement                                                                                                                                  |
|    | Method mark awarded zero                                                                                                                   |
|    | Method mark awarded one                                                                                                                    |
|    | Method mark awarded two                                                                                                                    |
|    | Misread                                                                                                                                    |
|    | Omission or Other solution                                                                                                                 |
| Off-page comment                                                                    | Allows comments to be entered at the bottom of the RM marking window and then displayed when the associated question item is navigated to. |
| On-page comment                                                                     | Allows comments to be entered in speech bubbles on the candidate response.                                                                 |
|  | Judgment made by the PE                                                                                                                    |
|  | Premature approximation                                                                                                                    |
|  | Special case                                                                                                                               |

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| <b>Annotation</b>                                                                 | <b>Meaning</b>                         |
|-----------------------------------------------------------------------------------|----------------------------------------|
|  | Indicates that work/page has been seen |
|  | Error in number of significant figures |
|  | Correct                                |
|  | Transcription error                    |
|  | Correct answer from incorrect working  |

**PUBLISHED****Mark Scheme Notes**

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

**Types of mark**

- M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B** Mark for a correct result or statement independent of method marks.
- DM or DB** When a part of a question has two or more ‘method’ steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
  - For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
  - The total number of marks available for each question is shown at the bottom of the Marks column.
  - Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
  - Square brackets [ ] around text or numbers show extra information not needed for the mark to be awarded.

**Abbreviations**

|        |                                                                                                                                                                                       |
|--------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| AEF/OE | Any Equivalent Form (of answer is equally acceptable) / Or Equivalent                                                                                                                 |
| AG     | Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)                                                   |
| CAO    | Correct Answer Only (emphasising that no ‘follow through’ from a previous error is allowed)                                                                                           |
| CWO    | Correct Working Only                                                                                                                                                                  |
| ISW    | Ignore Subsequent Working                                                                                                                                                             |
| SOI    | Seen Or Implied                                                                                                                                                                       |
| SC     | Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance) |
| WWW    | Without Wrong Working                                                                                                                                                                 |
| AWRT   | Answer Which Rounds To                                                                                                                                                                |

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| Question | Answer                                                                               | Marks     | Guidance                                                                                                                                                                                                                                                                                                                                                 |
|----------|--------------------------------------------------------------------------------------|-----------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1        | $[t =] \pm \frac{10.24 - 10.6}{\sqrt{\frac{0.52}{12}}}$                              | <b>M1</b> | Must be in correct form, allow $\frac{0.52}{\sqrt{12}}$ in denominator.                                                                                                                                                                                                                                                                                  |
|          | $(\pm)1.729$                                                                         | <b>A1</b> | CWO, AWRT $(\pm)1.73$ .                                                                                                                                                                                                                                                                                                                                  |
|          | ' $-1.729$ ' $< -1.363$ (or $1.729 > 1.363$ ), reject $H_0$ (significant).           | <b>M1</b> | Compare <i>their</i> $t$ with $\pm 1.363$ (consistent signs) and appropriate conclusion (may be in terms of $H_1$ ).<br>Reject $H_0$ can be implied by an attempt at an appropriate conclusion in context.<br>Allow M1 for comparison of <i>their</i> $t$ with $\pm 1.356$ , $\pm 1.796$ , or $\pm 1.782$ (consistent signs) and appropriate conclusion. |
|          | Sufficient evidence to support/suggest that the [population] mean is less than 10.6. | <b>A1</b> | Correct conclusion in context from correct working ignoring hypotheses.<br>Level of uncertainty in language used (for example, not 'prove').<br>Allow $\mu$ or mean for population mean.                                                                                                                                                                 |
|          |                                                                                      | <b>4</b>  |                                                                                                                                                                                                                                                                                                                                                          |

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| Question | Answer                                                                                                      | Marks     | Guidance                                                                                                                                                                                                                                                                                                  |
|----------|-------------------------------------------------------------------------------------------------------------|-----------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 2(a)     | $H_0$ : <b>population</b> median = 8.00<br>$H_1$ : <b>population</b> median > 8.00                          | <b>B1</b> | Allow $m$ , but not $\mu$ . If $m$ defined, must see <b>population</b> .                                                                                                                                                                                                                                  |
|          | –0.34, 0.48, 0.21, –0.02, 0.01, –0.23, 0.25, 0.11, 0.03, 0.16, –0.08                                        | <b>M1</b> | Attempt at (signed) differences.                                                                                                                                                                                                                                                                          |
|          | –10, 11, 7, –2, 1, –8, 9, 5, 3, 6, –4                                                                       | <b>M1</b> | Attempt at (signed) ranks, ranks may be reversed.                                                                                                                                                                                                                                                         |
|          | $(P = 42, Q = 24) \quad T = 24$                                                                             | <b>A1</b> |                                                                                                                                                                                                                                                                                                           |
|          | '24' > 13, accept $H_0$ (not significant).                                                                  | <b>M1</b> | Compare <i>their</i> 24 (from rank sum only) with 13 and appropriate conclusion (may be in terms of $H_1$ ).<br>Accept $H_0$ can be implied by an attempt at an appropriate conclusion in context.<br>Allow M1 for comparison of <i>their</i> 24 (from rank sum only) with 10 and appropriate conclusion. |
|          | Insufficient evidence to support/suggest that the average sound level is more than 8.00.                    | <b>A1</b> | Correct conclusion in context from correct working ignoring hypotheses.<br>Level of uncertainty in language used (for example, not 'prove').<br>Must refer to <b>average/median sound</b> (level).                                                                                                        |
|          |                                                                                                             | <b>6</b>  |                                                                                                                                                                                                                                                                                                           |
| 2(b)     | It is not known if the population is normal.<br>It is not known if the (underlying) distribution is normal. | <b>B1</b> | Must refer to population and/or distribution.<br>B0 for data is normal.<br>B0 for (population) differences are normal.                                                                                                                                                                                    |
|          |                                                                                                             | <b>1</b>  |                                                                                                                                                                                                                                                                                                           |

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| Question                                                                                                                                                                                                   | Answer                                                                                                                                                                                                                                                                                                                          | Marks                                                                                                                                                                                                                                                                                                                | Guidance                                                                                                                                                                        |            |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------|------------|-------|-----------|------------|------------|-----|-----------|------------|------------|---------|-----------|------------|------------|-----------|-------------------------------------------------------------------------------------------------------------------|
| 3                                                                                                                                                                                                          | $H_0$ : type of item sold is independent of salesperson.<br>$H_1$ : type of item sold is not independent of salesperson.                                                                                                                                                                                                        | <b>B1</b>                                                                                                                                                                                                                                                                                                            | Allow dependent, association or relationship for not independent.<br>For example: $H_0$ : No association/relationship between...<br>$H_1$ : Association/relationship between... |            |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |
|                                                                                                                                                                                                            | <table><tr><td></td><td>Laptop</td><td>Camera</td><td>Television</td></tr><tr><td>Avril</td><td>31 (28.5)</td><td>40 (41.80)</td><td>24 (24.70)</td></tr><tr><td>Ben</td><td>23 (29.1)</td><td>45 (42.68)</td><td>29 (25.22)</td></tr><tr><td>Charlie</td><td>21 (17.4)</td><td>25 (25.52)</td><td>12 (15.08)</td></tr></table> |                                                                                                                                                                                                                                                                                                                      | Laptop                                                                                                                                                                          | Camera     | Television | Avril | 31 (28.5) | 40 (41.80) | 24 (24.70) | Ben | 23 (29.1) | 45 (42.68) | 29 (25.22) | Charlie | 21 (17.4) | 25 (25.52) | 12 (15.08) | <b>M1</b> | Calculate expected values ( <b>must be seen</b> ).<br>M1 for at least 4 expected values correct to 3sf or better. |
|                                                                                                                                                                                                            |                                                                                                                                                                                                                                                                                                                                 | Laptop                                                                                                                                                                                                                                                                                                               | Camera                                                                                                                                                                          | Television |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |
|                                                                                                                                                                                                            | Avril                                                                                                                                                                                                                                                                                                                           | 31 (28.5)                                                                                                                                                                                                                                                                                                            | 40 (41.80)                                                                                                                                                                      | 24 (24.70) |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |
|                                                                                                                                                                                                            | Ben                                                                                                                                                                                                                                                                                                                             | 23 (29.1)                                                                                                                                                                                                                                                                                                            | 45 (42.68)                                                                                                                                                                      | 29 (25.22) |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |
|                                                                                                                                                                                                            | Charlie                                                                                                                                                                                                                                                                                                                         | 21 (17.4)                                                                                                                                                                                                                                                                                                            | 25 (25.52)                                                                                                                                                                      | 12 (15.08) |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |
|                                                                                                                                                                                                            |                                                                                                                                                                                                                                                                                                                                 | <b>A1</b>                                                                                                                                                                                                                                                                                                            | All expected values correct to 3sf or better.                                                                                                                                   |            |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |
|                                                                                                                                                                                                            | $\frac{(31 - 28.5)^2}{28.5} + \frac{(40 - 41.8)^2}{41.8} + \dots + \frac{(15.08 - 12)^2}{15.08}$ <p>OR</p> $\frac{31^2}{28.5} + \frac{40^2}{41.8} + \dots + \frac{12^2}{15.08} - 250$                                                                                                                                           | <b>M1</b>                                                                                                                                                                                                                                                                                                            | At least 2 terms (not including 250) of correct form seen.<br>May see individual terms not summed.<br>May be implied by AWR 3.67 or 3.68.                                       |            |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |
| Test statistic = 3.67 (or 3.68)                                                                                                                                                                            | <b>A1</b>                                                                                                                                                                                                                                                                                                                       | AWRT 3.67 or 3.68.                                                                                                                                                                                                                                                                                                   |                                                                                                                                                                                 |            |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |
| '3.67' < 7.779, accept $H_0$ (not significant).                                                                                                                                                            | <b>M1</b>                                                                                                                                                                                                                                                                                                                       | Compare <i>their</i> 3.67 (or 3.68) with 7.779 and appropriate conclusion (may be in terms of $H_1$ ).<br>Accept $H_0$ can be implied by an attempt at an appropriate conclusion in context.<br>Allow M1 for comparison of <i>their</i> 3.67 (or 3.68) with 9.488 and appropriate conclusion.                        |                                                                                                                                                                                 |            |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |
| Insufficient evidence to suggest that type of item sold and salesperson are not independent.<br>OR<br>Insufficient evidence to suggest that there is dependence between type of item sold and salesperson. | <b>A1</b>                                                                                                                                                                                                                                                                                                                       | Correct conclusion in context from correct working ignoring hypotheses. Condone 'no sufficient evidence'.<br>Level of uncertainty in language used (for example, not 'prove').<br>Must refer to both item and salesperson.<br>Do not accept statements such as 'there is sufficient evidence to suggest...'.<br><br> |                                                                                                                                                                                 |            |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |
|                                                                                                                                                                                                            | <b>7</b>                                                                                                                                                                                                                                                                                                                        |                                                                                                                                                                                                                                                                                                                      |                                                                                                                                                                                 |            |            |       |           |            |            |     |           |            |            |         |           |            |            |           |                                                                                                                   |

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| Question | Answer                                                                                                                                                                                                                     | Marks        | Guidance                                                                                                                                                                                                        |
|----------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 4(a)     | $\int_0^1 kx \, dx + \int_1^2 kx^2 \, dx = 1 \quad \left[ \left[ \frac{1}{2} kx^2 \right]_0^1 + \left[ \frac{1}{3} kx^3 \right]_1^2 = 1 \right]$<br>$\frac{1}{2}k + \frac{1}{3}k(8-1) = 1$                                 | <b>M1</b>    | Linear equation in terms of <b>k</b> formed following attempt to integrate (all powers correct) and use of correct limits.<br>May consider area of triangle $(\frac{1}{2} \times 1 \times k)$ for first region. |
|          | $\frac{17}{6}k = 1, \quad k = \frac{6}{17}$                                                                                                                                                                                | <b>A1</b>    | AG, shown convincingly. No errors seen.                                                                                                                                                                         |
|          |                                                                                                                                                                                                                            | <b>2</b>     |                                                                                                                                                                                                                 |
| 4(b)     | $F(x) = \begin{cases} 0 & x < 0 \\ \frac{3}{17}x^2 & 0 \leq x < 1 \\ \frac{2}{17}x^3 + \frac{1}{17} & 1 \leq x \leq 2 \\ 1 & x > 2 \end{cases}$                                                                            | <b>M1</b>    | Attempt to integrate <b>both</b> parts, all powers correct, condone missing <i>c</i> .<br>Sight of expressions for $0 \leq x < 1$ and $1 \leq x \leq 2$ sufficient.                                             |
|          |                                                                                                                                                                                                                            | <b>A1</b>    | Both parts correct with $c = \frac{1}{17}$ .<br>Sight of expressions for $0 \leq x < 1$ and $1 \leq x \leq 2$ sufficient.                                                                                       |
|          |                                                                                                                                                                                                                            | <b>A1</b>    | All correct, fully defined including domain.<br>Domain must cover all reals, may overlap at boundaries.                                                                                                         |
|          |                                                                                                                                                                                                                            | <b>3</b>     |                                                                                                                                                                                                                 |
| 4(c)     | $F(m) = \frac{1}{2} \text{ so } \frac{2}{17}m^3 + \frac{1}{17} = \frac{1}{2}$                                                                                                                                              | <b>M1</b>    | Use $1 \leq m \leq 2$ and <i>their</i> $F(x)$ (or areas) to form equation with 0.5.                                                                                                                             |
|          | $m^3 = \frac{15}{4}, \quad m = \sqrt[3]{\frac{15}{4}} \quad [=1.55]$                                                                                                                                                       | <b>A1 FT</b> | FT <i>their non-zero c</i> , to obtain <i>m</i> with $1 \leq m \leq 2$ .                                                                                                                                        |
|          |                                                                                                                                                                                                                            | <b>2</b>     |                                                                                                                                                                                                                 |
| 4(d)     | $\left[ E\left(\frac{1}{X}\right) = \right] \int_0^1 \frac{6}{17}x \left(\frac{1}{x}\right) dx + \int_1^2 \frac{6}{17}x^2 \left(\frac{1}{x}\right) dx = \frac{6}{17}[x]_0^1 + \frac{6}{17}\left[\frac{1}{2}x^2\right]_1^2$ | <b>M1</b>    | Correct method and attempt to integrate both parts. All powers correct, limits not required.                                                                                                                    |
|          | $\frac{6}{17}\left(1+2-\frac{1}{2}\right) = \frac{15}{17} \quad [=0.882]$                                                                                                                                                  | <b>A1</b>    | CWO, AWRT 0.882.                                                                                                                                                                                                |
|          |                                                                                                                                                                                                                            | <b>2</b>     |                                                                                                                                                                                                                 |

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| Question | Answer                                                                                                                                        | Marks        | Guidance                                                                                                                                 |
|----------|-----------------------------------------------------------------------------------------------------------------------------------------------|--------------|------------------------------------------------------------------------------------------------------------------------------------------|
| 5(a)     | Probabilities: $\frac{8}{27}, \frac{12}{27}, \frac{6}{27}, \frac{1}{27}$ for 0, 1, 2, 3 heads                                                 | <b>B1</b>    |                                                                                                                                          |
|          | $\frac{8}{27} + \frac{12}{27}t + \frac{6}{27}t^2 + \frac{1}{27}t^3$                                                                           | <b>B1 FT</b> | FT <i>their</i> probabilities to form a 4-term cubic. Must have $\sum p = 1$ .<br>$\left(\frac{2}{3} + \frac{1}{3}t\right)^3$ scores B2. |
|          |                                                                                                                                               | <b>2</b>     |                                                                                                                                          |
| 5(b)     | $\left(\frac{8}{27} + \frac{12}{27}t + \frac{6}{27}t^2 + \frac{1}{27}t^3\right)\left(\frac{25}{36} + \frac{10}{36}t + \frac{1}{36}t^2\right)$ | <b>M1</b>    | Attempt to multiply <i>their</i> $G_X(t)$ and <i>their</i> $G_Y(t)$ .                                                                    |
|          | $\frac{1}{972}(200 + 380t + 278t^2 + 97t^3 + 16t^4 + t^5)$                                                                                    | <b>M1</b>    | Expand to form polynomial of degree 5 (need not be simplified).                                                                          |
|          |                                                                                                                                               | <b>A1</b>    | CWO                                                                                                                                      |
|          |                                                                                                                                               | <b>3</b>     |                                                                                                                                          |
| 5(c)     | $G'_Z(t) = \frac{1}{972}(380 + 556t + 291t^2 + 64t^3 + 5t^4)$                                                                                 | <b>M1</b>    | Attempt at differentiating <i>their</i> $G_Z(t)$ .                                                                                       |
|          | $E(Z) = G'_Z(1) = \frac{1296}{972} = \frac{4}{3}$                                                                                             | <b>A1 FT</b> | FT <i>their</i> $G_Z(t)$ .                                                                                                               |
|          | $G''_Z(t) = \frac{1}{972}(556 + 582t + 192t^2 + 20t^3)$                                                                                       | <b>M1</b>    | Attempt at differentiating <i>their</i> $G'_Z(t)$ .                                                                                      |
|          | $\text{Var}(Z) = \frac{1350}{972} + \frac{4}{3} - \left(\frac{4}{3}\right)^2 = \frac{25}{18} + \frac{4}{3} - \left(\frac{4}{3}\right)^2$      | <b>M1</b>    | Use correct formula using <i>their</i> $G'_Z(1)$ and <i>their</i> $G''_Z(1)$ .                                                           |
|          | $\frac{17}{18} \quad [= 0.944]$                                                                                                               | <b>A1</b>    | CWO                                                                                                                                      |
|          |                                                                                                                                               | <b>5</b>     |                                                                                                                                          |

| Question | Answer                                                            | Marks        | Guidance                                                                                                                                                                    |
|----------|-------------------------------------------------------------------|--------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 6(a)     | $\sum x = 30.4$                                                   | <b>B1</b>    |                                                                                                                                                                             |
|          | 2.262                                                             | <b>B1</b>    | 2.26 or 2.262 seen.                                                                                                                                                         |
|          | Subtract: $s_x = \frac{\sqrt{10}(3.13 - 2.95)}{(2 \times 2.262)}$ | <b>M1</b>    | Subtracting, or substituting, to find an equation involving $s_x$ .<br>Allow M1 for any of the following $t$ values seen instead of 2.262:<br>1.812, 1.833, 2.228 or 3.690. |
|          | $s_x^2 = 0.0158$ or $s_x = 0.126$                                 | <b>A1 FT</b> | FT <i>their</i> 2.262 following M1.<br>Implied by AWRT 92.6 following M1.                                                                                                   |
|          | $\sum x^2 = 9 \times 0.0158307 + \frac{30.4^2}{10} = 92.6$        | <b>A1 FT</b> | FT <i>their</i> 2.262.<br>CWO                                                                                                                                               |
|          |                                                                   | <b>5</b>     |                                                                                                                                                                             |

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| Question | Answer                                                                                                   | Marks     | Guidance                                                                                                                                                                                                                                                                                                              |
|----------|----------------------------------------------------------------------------------------------------------|-----------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 6(b)     | $H_0 : \mu_Y = \mu_X$<br>$H_1 : \mu_Y > \mu_X$                                                           | <b>B1</b> | If in words, must contain ‘ <b>population</b> means’.<br>Allow $H_0: \mu_d = 0, H_1: \mu_d > 0$ if defined or consistent with working.                                                                                                                                                                                |
|          | $76.98 - \frac{24.8^2}{8}$                                                                               | <b>M1</b> | May be embedded, for example $s_y^2 = \frac{1}{7} \left( 76.98 - \frac{1}{8} (24.8^2) \right)$ .                                                                                                                                                                                                                      |
|          | $s_p^2 = \frac{9s_x^2 + 7s_y^2}{10 + 8 - 2} [= 0.015155]$                                                | <b>M1</b> | Correct form using <i>their</i> $s_x^2$ and <i>their</i> $s_y^2$ , may be embedded.                                                                                                                                                                                                                                   |
|          |                                                                                                          | <b>A1</b> | SOI, can be implied by any $ t $ that rounds to 1.02 or 1.03.                                                                                                                                                                                                                                                         |
|          | $t = \frac{3.04 - 3.1}{s_p \sqrt{\frac{1}{10} + \frac{1}{8}}} = -1.028$                                  | <b>M1</b> | Correct form using <i>their</i> $s_p$ .                                                                                                                                                                                                                                                                               |
|          |                                                                                                          | <b>A1</b> | AWRT $\pm 1.02$ or $\pm 1.03$ implies M1 A1.                                                                                                                                                                                                                                                                          |
|          | [18 degrees of freedom, so critical value is 1.746.]<br>'1.028' < 1.746, accept $H_0$ (not significant). | <b>M1</b> | Compare <i>their</i> $t$ with $\pm 1.746$ (consistent signs) and appropriate conclusion (may be in terms of $H_1$ ).<br>Accept $H_0$ can be implied by an attempt at an appropriate conclusion in context.<br>Allow M1 for comparison of <i>their</i> $t$ with $\pm 1.740$ or $\pm 2.120$ and appropriate conclusion. |
|          | Insufficient evidence to support Mona’s claim.                                                           | <b>A1</b> | Correct conclusion in context from correct working ignoring hypotheses.<br>Level of uncertainty in language used (for example, not ‘prove’).                                                                                                                                                                          |
|          |                                                                                                          | <b>8</b>  |                                                                                                                                                                                                                                                                                                                       |