



Cambridge International AS & A Level

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MATHEMATICS

9709/12

Paper 1 Pure Mathematics 1

October/November 2022

1 hour 50 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has **20** pages. Any blank pages are indicated.



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3

1 Points A and B have coordinates $(5, 2)$ and $(10, -1)$ respectively.

(a) Find the equation of the perpendicular bisector of AB . [3]

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(b) Find the equation of the circle with centre A which passes through B . [3]

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[5]

[illegible]

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- 3 (a)** Find the set of values of k for which the equation $8x^2 + kx + 2 = 0$ has no real roots. [2]

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- (b)** Solve the equation $8 \cos^2 \theta - 10 \cos \theta + 2 = 0$ for $0^\circ \leq \theta \leq 180^\circ$. [3]

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[4]

[illegible]

6 The equation of a curve is $y = 4x^2 + 20x + 6$.

(a) Express the equation in the form $y = a(x + b)^2 + c$, where a , b and c are constants. [3]

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(b) Hence solve the equation $4x^2 + 20x + 6 = 45$. [3]

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- (c) Sketch the graph of $y = 4x^2 + 20x + 6$ showing the coordinates of the stationary point. You are not required to indicate where the curve crosses the x - and y -axes. [3]

[illegible]

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.

[4]

This image shows a full page of a handwriting practice worksheet. It consists of multiple sets of three horizontal dashed lines, providing a guide for letter height and placement. The lines are evenly spaced across the entire page, leaving ample room for writing practice. There is no text or other markings on the page.

(b) Find the x -coordinate of the stationary point. [2]

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(c) State the set of values of x for which y increases as x increases. [1]

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- 9 Functions f and g are defined by

$$f(x) = x + \frac{1}{x} \quad \text{for } x > 0,$$
$$g(x) = ax + 1 \quad \text{for } x \in \mathbb{R},$$

where a is a constant.

- (a) Find an expression for $gf(x)$. [1]

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- (b) Given that $gf(2) = 11$, find the value of a . [2]

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- (c) Given that the graph of $y = f(x)$ has a minimum point when $x = 1$, explain whether or not f has an inverse. [1]

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It is given instead that $a = 5$.

- (d) Find and simplify an expression for $g^{-1}f(x)$. [3]

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- (e) Explain why the composite function fg cannot be formed. [1]

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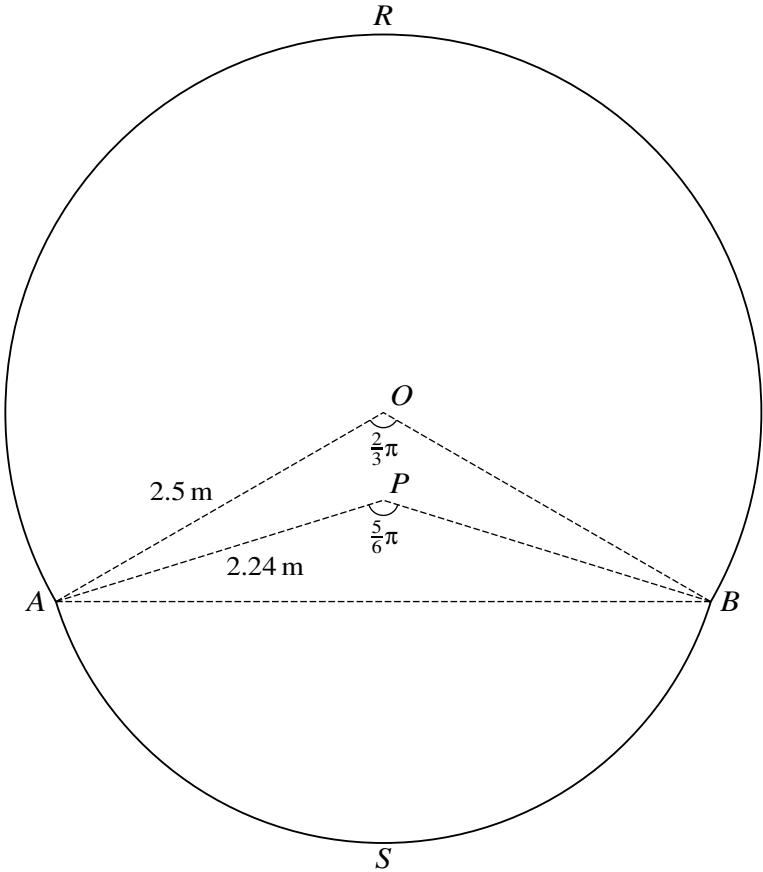
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The diagram shows a cross-section $RASB$ of the body of an aircraft. The cross-section consists of a sector $OARB$ of a circle of radius 2.5 m, with centre O , a sector $PASB$ of another circle of radius 2.24 m with centre P and a quadrilateral $OAPB$. Angle $AOB = \frac{2}{3}\pi$ and angle $APB = \frac{5}{6}\pi$.

- (a) Find the perimeter of the cross-section $RASB$, giving your answer correct to 2 decimal places. [3]

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- (b) Find the difference in area of the two triangles AOB and APB , giving your answer correct to 2 decimal places. [2]

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- (c) Find the area of the cross-section $RASB$, giving your answer correct to 1 decimal place. [3]

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- 11 (a)** Find the coordinates of the minimum point of the curve $y = \frac{9}{4}x^2 - 12x + 18$. [3]

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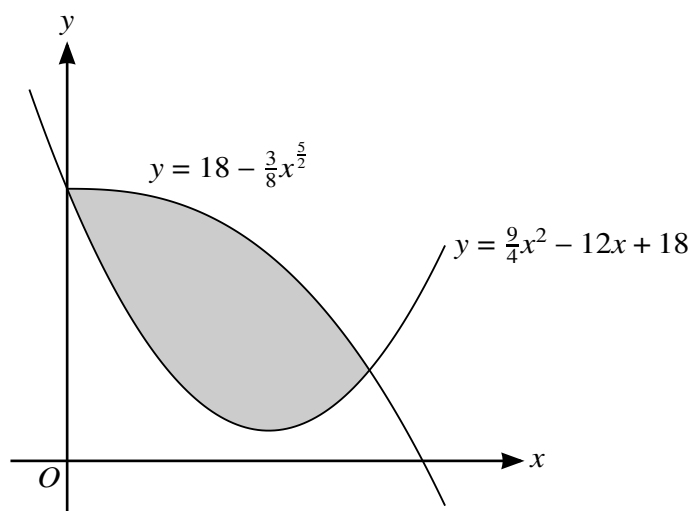
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The diagram shows the curves with equations $y = \frac{9}{4}x^2 - 12x + 18$ and $y = 18 - \frac{3}{8}x^{\frac{5}{2}}$. The curves intersect at the points (0, 18) and (4, 6).

- (b)** Find the area of the shaded region. [5]

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(c) A point P is moving along the curve $y = 18 - \frac{3}{8}x^{\frac{5}{2}}$ in such a way that the x -coordinate of P is increasing at a constant rate of 2 units per second.

Find the rate at which the y -coordinate of P is changing when $x = 4$. [3]

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[illegible]

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