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CAMBRIDGE
International Education

Cambridge International A Level

MATHEMATICS **9709/32**

Paper 3 Pure Mathematics 3 **October/November 2025**

MARK SCHEME

Maximum Mark: 75

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2025 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:
Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:
Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:
Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:
Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:
Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:
Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Mathematics-Specific Marking Principles

1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.

2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.

3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.

4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).

5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.

6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

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Annotations guidance for centres

Examiners use a system of annotations as a shorthand for communicating their marking decisions to one another. Examiners are trained during the standardisation process on how and when to use annotations. The purpose of annotations is to inform the standardisation and monitoring processes and guide the supervising examiners when they are checking the work of examiners within their team. The meaning of annotations and how they are used is specific to each component and is understood by all examiners who mark the component.

We publish annotations in our mark schemes to help centres understand the annotations they may see on copies of scripts. Note that there may not be a direct correlation between the number of annotations on a script and the mark awarded. Similarly, the use of an annotation may not be an indication of the quality of the response.

The annotations listed below were available to examiners marking this component in this series.

Annotations

Annotation	Meaning
	More information required
	Accuracy mark awarded zero
	Accuracy mark awarded one
	Independent accuracy mark awarded zero
	Independent accuracy mark awarded one
	Independent accuracy mark awarded two
	Benefit of the doubt
	Blank Page
	Incorrect
Dep	Used to indicate DM0 or DM1

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Annotation	Meaning
DM1	Dependent on the previous M1 mark(s)
FT	Follow through
~~	Indicate working that is right or wrong
Highlighter	Highlight a key point in the working
ISW	Ignore subsequent work
J	Judgement
JU	Judgement
M0	Method mark awarded zero
M1	Method mark awarded one
M2	Method mark awarded two
MR	Misread
O	Omission or Other solution
Off-page comment	Allows comments to be entered at the bottom of the RM marking window and then displayed when the associated question item is navigated to.
On-page comment	Allows comments to be entered in speech bubbles on the candidate response.
PE	Judgment made by the PE
Pre	Premature approximation
SC	Special case
SEEN	Indicates that work/page has been seen

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Annotation	Meaning
SF	Error in number of significant figures
✓	Correct
TE	Transcription error
XP	Correct answer from incorrect working

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Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

DM or **DB** When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.

- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
- For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
- The total number of marks available for each question is shown at the bottom of the Marks column.
- Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
- Square brackets [ ] around text or numbers show extra information not needed for the mark to be awarded.

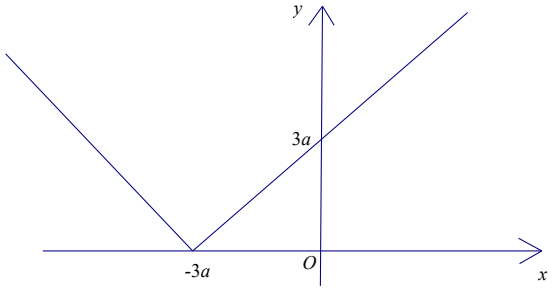
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Abbreviations

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

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Question	Answer	Marks	Guidance
1(a)		**B1**	Roughly symmetrical. Condone some inaccuracy, but needs to look as if they intended symmetry and straight lines. If not, then B0. Needs to be in the correct position. Needs to have two solid line segments. Needs to exist in both quadrants above the axis. Ignore dotted lines below the axis. Solid line below the axis is B0. Condone if no scale shown, but need to see $3a$ and $-3a$ marked. Ignore $y = a - 2x$ if seen.
		1	
1(b)	Obtain critical value $-\frac{2a}{3}$ from $x + 3a = a - 2x$	**B1**	Ignore $x = 4a$ if seen.
	State final answer $x > -\frac{2a}{3}$	**B1**	Need a clear conclusion – must imply rejection of $x = 4a$. B0 if using $\geqslant$.
	Alternative Method for Question 1(b)		
	Obtain critical value $-\frac{2a}{3}$ from $(x + 3a)^2 = (a - 2x)^2$	**B1**	Ignore $x = 4a$ if seen.
	State final answer $x > -\frac{2a}{3}$	**B1**	Need a clear conclusion – must imply rejection of $x = 4a$. B0 if using $\geqslant$.
		2	

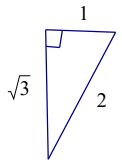
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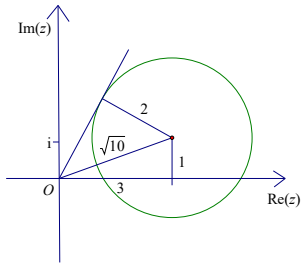
Question	Answer	Marks	Guidance
2	Use a correct law for the logarithm of a product or the logarithm of a power	***M1**	Not available after incorrect manipulation, e.g. $6^{x+1}=12^{2x-3}$
	Obtain $\ln 3+(x+1)\ln 2=\ln 4+(2x-3)\ln 3$	**A1**	Or equivalent with no powers
	Solve for x	**DM1**	E.g. $x=\frac{\ln\frac{2}{81}}{\ln\frac{2}{9}}$ Allow with logarithms evaluated.
	Obtain 2.46 only	**A1**	
	Alternative Method for Question 2		
	Use a correct law of indices for a product or a power	***M1**	E.g. $2^{x+1}=2\times 2^x$ Not available after incorrect manipulation, e.g. $6^{x+1}=12^{2x-3}$. $4=2^2$ on its own is not enough.
	Obtain $\left(\frac{2}{9}\right)^x=\frac{2}{81}$	**A1**	OE with powers of x only, e.g. $6\times 2^x=\frac{4}{27}\times 9^x$ Note: $\left(3^x\right)^2$ is not far enough.
	Solve for x	**DM1**	E.g. $x=\frac{\ln\frac{2}{81}}{\ln\frac{2}{9}}$ or $x=\ln_{\frac{2}{9}}\frac{2}{81}$. Allow with logarithms evaluated.
	Obtain 2.46 only	**A1**	
		4	

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Question	Answer	Marks	Guidance
3(a)	Complete method to obtain equation in y only or Obtain the y coordinate of P	**M1**	E.g. $(2-3)^2+(y-1)^2=4$ Or consider triangle and state $\pm\left(\sqrt{3}-1\right)$. 
	Obtain $2+\mathrm{i}\left(1-\sqrt{3}\right)$	**A1**	Or exact equivalent in the form $x + \mathrm{i}y$. Allow $2-\mathrm{i}\left(\sqrt{3}-1\right)$. Must not be coordinates, and not x, y stated separately.
		2	

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Question	Answer	Marks	Guidance
3(b)	State one relevant angle, e.g. $\tan^{-1}\frac{1}{3}$ or $\sin^{-1}\frac{2}{\sqrt{10}}$	**B1**	 Note: $\tan^{-1}\frac{1}{3}=\sin^{-1}\frac{1}{\sqrt{10}}$
	Complete method to obtain the required angle	**M1**	$\tan^{-1}\frac{1}{3}+\sin^{-1}\frac{2}{\sqrt{10}}$
	Obtain 1.01 radians or 57.7°	**A1**	Accept AWRT
	Alternative Method for Question 3(b)		
	If $y=mx$ is a tangent to the circle $\Rightarrow (x-3)^2+(mx-1)^2=4$ $\Rightarrow \left(\left(1+m^2\right)x^2+(-6-2m)x+6=0\right)$, then $(-6-2m)^2-24\left(1+m^2\right)=0$ and $m=\frac{3+2\sqrt{6}}{5}$	**B1**	Must be choosing the positive root.
	Substitute into the quadratic and solve for x, or use gradient to obtain tangent Required angle is $\frac{\pi}{2}-\sin^{-1}\left(\frac{9-\sqrt{6}/5}{\sqrt{6}}\right)$ OE	**M1**	Note $x=\frac{9-\sqrt{6}}{5}$
	Obtain 1.01 radians or 57.7°	**A1**	Accept AWRT
		3	

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Question	Answer	Marks	Guidance
4	Begin integration by parts and obtain $px^2\tan^{-1}x+q\int\frac{x^2}{1+x^2}\,\mathrm{d}x$	**M1***	Condone sign error in formula for integration by parts.
	Obtain $\frac{x^2}{2}\tan^{-1}x-\frac{1}{2}\int\frac{x^2}{1+x^2}\,\mathrm{d}x$	**A1**	OE Allow with $\arctan x$ or $\tan^{-1}x$.
	Use $\int\frac{x^2}{1+x^2}\,\mathrm{d}x=\int 1-\frac{1}{1+x^2}\,\mathrm{d}x$ and integrate to obtain $\beta x+\gamma\tan^{-1}x$	**DM1**	Split the fraction and integrate.
	Obtain $\frac{x^2}{2}\tan^{-1}x-\frac{1}{2}\left(x-\tan^{-1}x\right)$	**A1**	OE
	Substitute correct limits correctly in an expression of the form $\alpha x^2\tan^{-1}x+\beta x+\gamma\tan^{-1}x$	**DM1**	$\frac{\pi}{8}-0-\frac{1}{2}+\frac{\pi}{8}+0\left(-0\right)$ Dependent on both previous M marks. Need to see evidence of the use of the lower limit at least once. Must evaluate the trigonometry using radians.
	Obtain $\frac{\pi}{4}-\frac{1}{2}$	**A1**	ISW Or exact two term equivalent
		6	

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Question	Answer	Marks	Guidance
5(a)	Use correct product rule	**M1**	$f'(x)=(x-a)^2 g'(x)+2(x-a)g(x)$ Allow incorrect chain rule.
	Obtain correct derivative and state a clear conclusion	**A1**	**AG** E.g. take out a factor of $(x-a)$ and show the factorised form as far as $(x-a)h(x)$ correctly (no further comment needed), or show that $f'(a)=0$ and state that '$(x-a)$ is a factor'.
		2	

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Question	Answer	Marks	Guidance
5(b)	Use $f(3)=0$	**M1**	$2\times3^3-4\times3^2+3p+q=0$
	Obtain $3p+q=-18$	**A1**	OE Powers should be evaluated but do not need to be simplified.
	Use $f'(3)=0$	**M1**	$54-24+p=0$
	Obtain $p=-30$	**A1**	OE
	Obtain $p=-30, q=72$	**A1**	Correct only.
	Alternative Method for Question 5(b)		
	Attempt division of f(x) by $(x-3)^2$ as far as $(2x+Q)$	**M1**	$Q\neq0$
	Obtain quotient $(2x+8)$	**A1**	
	Equate linear remainder to zero and compare coefficients	**M1**	Or expand $(2x+8)(x-3)^2$ and compare coefficients. Method to obtain an equation in p or q.
	obtain one of $p=-30, q=72$	**A1**	
	Obtain $p=-30, q=72$	**A1**	Correct answers only.

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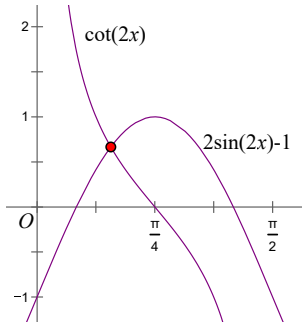
Question	Answer	Marks	Guidance
5(b)	**Alternative Method 2 for Question 5(b)**		
	Use $f(3)=0$	**M1**	$54-36+3p+q=0$
	Obtain $3p+q=-18$	**A1**	OE Powers evaluated.
	Divide f(x) by $(x-3)^2$ as far as $(2x+Q)$ and form an equation in p only **or** q only **or** in p and q	**M1**	Using this as part of a hybrid method they need to be working towards a second equation by considering coefficients in the remainder **or** use $f(-4)=0$ or equivalent for *their* $(2x+8)$.
	Obtain correct equation in p or q	**A1**	
	Obtain $p=-30, q=72$	**A1**	Correct answer only.
	Alternative Method 3 for Question 5(b)		
	$f'(x)=6x^2-8x+p$	**B1**	
	$=(x-3)(6x+10)$	**M1**	Use the factor $x-3$.
	Obtain $p=-30$	**A1**	
	$f(x)=(x-3)^2(2x+Q)$ $\left(=2x^3-4x^2-30x+q\right)$	**M1**	Use the factor $(x-3)^2$.
	$\Rightarrow Q=8,\quad q=72$	**A1**	

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Question	Answer	Marks	Guidance
5(b)	**Alternative Method 4 for Question 5(b)**		
	Expand $f(x)=(x-3)^2(Ax+B)$ and compare at least one coefficient other than for x^3	**M1**	$A=2$ can be found by inspection.
	Obtain $q=9B$ and $p=9A-6B$ or obtain $B=8$	**A1**	
	Use *their* A and B to solve for p or q	**M1**	$A=2$ $B=8$
	Obtain one of $p=-30, q=72$	**A1**	
	Obtain $p=-30, q=72$	**A1**	Correct answer only.
		5	

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Question	Answer	Marks	Guidance
6(a)	Sketch a relevant graph, e.g. $y = \cot 2x$ Scales must be correct if seen. Do not need a full scale, but do need to be able to verify the key points mentioned below: For $y = \cot 2x$, correct intercept on x-axis, asymptotes at $x = 0$, $x = \frac{1}{2}\pi$ implied (condone large gap between the curve and the asymptote on the RHS). Must be continuous. For $2\sin 2x - 1$, correct shape and position. No incorrect curvature. Correct maximum implied. Intercept at (0, -1).	**B1**	
	Sketch a second relevant graph, e.g. $y = 2\sin 2x - 1$ and justify the given statement	**B1**	Need to see enough of both graphs to confirm there is not a second intersection in the given interval. Need to mark the intersection with a dot or a cross, or say that the root lies at the point of intersection (or equivalent).
		2	
6(b)	Calculate the values of a relevant expression or pair of expressions at $x = 0.4$ and $x = 0.6$ Allow working on a smaller interval contained within the given interval	**M1**	E.g. $0.9712 > 0.435$ and $0.389 < 0.864$ $0.537 > 0$ and $-0.475 < 0$ Or using the iterative formula, $0.18 > 0$, $-0.17 < 0$ Or using $\tan 2x(2\sin 2x - 1) - 1 = 0$ $-0.55 < 0$, and $1.22 > 0$. M0 if working in degrees.
	Justify the given statement with correct calculated values	**A1**	Values to 2 sf or better. Accept values with statement $f(0.4) \times f(0.6) < 0$.
		2	

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Question	Answer	Marks	Guidance
6(c)	Use the iterative process $x_{n+1} = \frac{1}{2}\tan^{-1}\left(\frac{1}{2\sin 2x_n - 1}\right)$ correctly at least once	**M1**	M0 if working in degrees. Need to get as far as a second iteration completed.
	Obtain final answer 0.49	**A1**	
	Show sufficient iterations to 4 d.p. to justify 0.49 to 2 d.p. or show that there is a sign change in $(0.485, 0.495)$ $-0.0157 < 0$, $0.355 > 0$	**A1**	E.g. $0.5, 0.4858, 0.4967, 0.4883, 0.4947, \ldots$. or 0.4, 0.5804, 0.4378, 0.5395, 0.4595, 0.5188, 0.4726, 0.5075, 0.4804, 0.5009, 0.4851, 0.4972, 0.4879, 0.4950, 0.4895, 0.4937 or 0.6, 0.4291, 0.5483, 0.4544, 0.5235, 0.4695, 0.5101, 0.4786, 0.5025, 0.4840, 0.4981, 0.4872, 0.4955, 0.4891, 0.4940 The last 2 options are a lot of iterations. Allow the marks if they start correctly and finish correctly. Condone if there are some missing in the middle.
		3	

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Question	Answer	Marks	Guidance
7(a)	State or imply $6y^2\frac{dy}{dx}$ as the derivative of $2y^3$	**B1**	
	State or imply $3x^2\frac{dy}{dx}+6xy$ as the derivative of $3x^2y$	**B1**	
	Complete the differentiation and equate the derivative of the LHS to zero and solve for $\frac{dy}{dx}$ (the = 0 can be implied)	**M1**	Needs to be clear how the value of $\frac{dy}{dx}$ was obtained, e.g. collecting like terms and using brackets.
	Obtain $\frac{dy}{dx}=\frac{x^2+2xy}{2y^2-x^2}$ from correct working	**A1**	**AG** Accept $\frac{dy}{dx}=\frac{2xy+x^2}{2y^2-x^2}$. No incorrect statements, e.g. 'cancel by 3' or 'divide top and bottom by 3' are acceptable, but to have $\frac{dy}{dx}=\frac{3x^2+6xy}{6y^2-3x^2}$ and say "divide by 3" at the final step scores A0.
		4	
7(b)	Equate derivative to 0 and solve for x or for x in terms of y.	***M1**	E.g., $x^2+2xy=0\Rightarrow x=0$ or $x=-2y$. Must be using the numerator.
	Obtain $(0, 2)$	**B1**	Allow if the values are stated separately. Do not ISW.
	Use *their* $x=-2y$ to form an equation in one unknown Or equivalent e.g. substitute $y=-\frac{x^2}{2x}$	**dM1**	E.g., $2y^3-12y^3+8y^3=16$ or $-2\left(\frac{1}{8}x^3\right)+3\left(\frac{1}{2}x^3\right)-x^3=16.$
	Obtain $(4, -2)$	**A1**	Allow if the values are stated separately. Do not ISW
		4	

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Question	Answer	Marks	Guidance
8(a)	Use correct double angle formula to expand $\sin 4x$	*M1	$2\sin 2x\cos 2x$ OE
	Use correct double angle formulae to obtain an expression in $\sin x$ and $\cos x$	dM1	E.g., $4\sin x\cos x\left(2\cos^2 x-1\right)$ OE.
	Obtain $\sin 4x \equiv 4\sin x\left(2\cos^3 x-\cos x\right)$ from fully correct working	A1	AG
	Alternative Method for Question 8(a)		
	Use correct double angle formula to rearrange the RHS	*M1	E.g. $2\sin 2x\left(2\cos^2 x-1\right)$
	Use correct double angle formula to obtain an expression in $\sin 2x$ and $\cos 2x$	dM1	E.g. $2\sin 2x\cos 2x$
	Obtain $\sin 4x \equiv 4\sin x\left(2\cos^3 x-\cos x\right)$ from fully correct working	A1	AG
	Alternative Method 2 for Question 8(a)		
	Use correct angle sum formulae to expand $\sin 4x$ as far as an expression in $\sin x$, $\cos x$, $\sin 2x$ and $\cos 2x$	*M1	E.g. $\sin x\left(\cos x\cos 2x-\sin x\sin 2x\right)$ $+\cos x\left(\sin x\cos 2x+\cos x\sin 2x\right)$
	Use correct double angle formulae to obtain an expression in $\sin x$ and $\cos x$	dM1	E.g., $\sin x\cos x\left(2\cos^2 x-1\right)-2\sin^3 x\cos x$ $+\sin x\cos x\left(2\cos^2 x-1\right)+2\sin x\cos^3 x$
	Obtain $\sin 4x \equiv 4\sin x\left(2\cos^3 x-\cos x\right)$ from fully correct working	A1	
		3	

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Question	Answer	Marks	Guidance
8(b)	Use the identity to obtain $p\int \sin x\cos^6 x\,\mathrm{d}x + q\int \sin x\cos^4 x\,\mathrm{d}x$	**B1**	$8\int \sin x\cos^6 x\,\mathrm{d}x - 4\int \sin x\cos^4 x\,\mathrm{d}x$ Accept terms of the correct form but without the integral signs or the dx.
	Obtain $r\cos^7 x + s\cos^5 x$	**B1**	
	Obtain $-\frac{8}{7}\cos^7 x + \frac{4}{5}\cos^5 x$	**B1**	If using the substitution $u = \cos x$, accept the form $-\frac{8}{7}u^7 + \frac{4}{5}u^5$.
	Use the correct limits correctly in an expression of the form $r\cos^7 x + s\cos^5 x$	**M1**	OE Must be evaluated, e.g. $-\frac{8}{7}\times\frac{1}{8\sqrt{2}} + \frac{4}{5}\times\frac{1}{4\sqrt{2}} + \frac{8}{7} - \frac{4}{5}$.
	Obtain $\frac{1}{35}\left(\sqrt{2}+12\right)$	**A1**	Or exact simplified equivalent (e.g. as 2 terms).
		5	

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Question	Answer	Marks	Guidance
9(a)	State or imply the form $A+\frac{B}{x+2a}+\frac{C}{x+3a}$	**B1**	
	Use a correct method for finding a coefficient	**M1**	
	Obtain one of $A=1$, $B=2a$ and $C=-3a$	**A1**	**SC**: If B0 is scored because of an omission of 'A', then maximum M1A1 is available for one constant correct. **SC**: If they substitute a value for a, or if their working implies the use of $a=1$, they can score maximum B1M1.
	Obtain a second value	**A1**	
	Obtain the third value	**A1**	
	Alternative Method for Question 9(a)		
	State or imply $1+\frac{\text{linear expression}}{(x+2a)(x+3a)}$	**B1**	$1+\frac{-ax}{(x+2a)(x+3a)}$
	State or imply the form $1+\frac{B}{x+2a}+\frac{C}{x+3a}$	**B1**	
	Use a correct method for finding B or C	**M1**	
	Obtain one of $B=2a$ and $C=-3a$	**A1**	
	Obtain the second value	**A1**	
		5	

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Question	Answer	Marks	Guidance
9(b)	Integrate and obtain terms $Ax + B\ln(x+2a) + C\ln(x+3a)$	**B2FT**	B1 for any two terms correct, B2 for all three terms correct. The FT is on A, B and C: $x + 2a\ln(x+2a) - 3a\ln(x+3a)$. Allow for FT on a split completed in **(b)**.
	Substitute limits correctly in an integral containing at least 2 terms from the form $rx + s\ln(x+2a) + t\ln(x+3a)$	**M1**	E.g. $2a + 2a\ln\left(\frac{3}{1}\right) - 3a\ln\left(\frac{4}{2}\right)$
	Obtain $a\left(2 + \ln\left(\frac{9}{8}\right)\right)$ from correct working	**A1**	Accept equivalent fractions with integers. A0 XP if $a\left(2 + \ln\left(\frac{9}{8}\right)\right)$ is following an error in **(a)**.
		4	

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Question	Answer	Marks	Guidance
10(a)	State $\frac{\mathrm{d}V}{\mathrm{d}t} = 5000 - kh^2$	**B1**	SOI
	Use $V = 2500h$ and chain rule to obtain $\frac{\left(their \frac{\mathrm{d}V}{\mathrm{d}t}\right)}{2500}$	***M1**	OE $\frac{\mathrm{d}h}{\mathrm{d}t} = \frac{5000 - kh^2}{2500}$
	Use $h = 20, \frac{\mathrm{d}h}{\mathrm{d}t} = 0.4$ to obtain k	**dM1**	$0.4 = \frac{5000 - 400k}{2500} \Rightarrow k = 10$
	Obtain $\frac{\mathrm{d}h}{\mathrm{d}t} = \frac{500 - h^2}{250}$ from correct working	**A1**	AG There needs to be a complete statement for A1. Condone 'divide by 10' in place of showing the cancelling.
		4	

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Question	Answer	Marks	Guidance
10(b)	Separate variables correctly	**B1**	E.g. $\int \frac{1}{500-h^2}\,\mathrm{d}h = \frac{1}{250}\int 1\,\mathrm{d}t$ Condone missing integral signs or missing dh, dt, but not both.
	Obtain $\frac{1}{250}t$	**B1**	OE (depending on how they use the 250).
	Obtain $\frac{1}{2\sqrt{500}}\ln\left\|\frac{\sqrt{500}+h}{\sqrt{500}-h}\right\|$	**B1**	OE, e.g. $\frac{1}{20\sqrt{5}}\ln\left\|\frac{10\sqrt{5}+h}{10\sqrt{5}-h}\right\|$. Coefficients will depend on where the 250 is. Condone missing modulus signs.
	Use $t=0, h=0$ in an expression of the form $pt+q\ln(a+h)+r\ln(b-h)$ to obtain the constant of integration or as limits on a definite integral	**M1**	Requires a value for the constant. M0 if *their* equation has no solution. M0 if they never had a constant. Need some indication that the conclusion is based on using $t=0,\ h=0$, e.g. "$t=0,\ h=0\ \Rightarrow C=0$".
	Obtain $t=16.1\,(\mathrm{s})$	**A1**	Accept AWRT.
		5	

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Question	Answer	Marks	Guidance
11(a)	$\overrightarrow{MB} = -\mathbf{i} + 5\mathbf{j} + 2\mathbf{k}$	**B1**	Do not ISW. Accept as a column vector.
	$\overrightarrow{MC} = -5\mathbf{i} - 3\mathbf{j} + 4\mathbf{k}$	**B1**	Do not ISW. Accept as a column vector. **SC**: B0B1 for column vectors with **i**, **j**, **k** (or coordinates) (allow one slip).
		2	
11(b)	Carry out the correct process for evaluating the scalar product of $\overrightarrow{MB}$ and $\overrightarrow{MC}$	**M1**	Or $\overrightarrow{BM}$ and $\overrightarrow{CM}$. Need some evidence of an attempt to evaluate the scalar product.
	Using the correct process for the moduli, divide the scalar product by the product of the moduli for their two vectors.	**M1**	$\pm\left(\frac{5-15+8}{\sqrt{30}.\sqrt{50}}\right)$ The scalar product could be incorrect, but it must be a scalar. Condone a sign change.
	Obtain $-\frac{\sqrt{15}}{75}$	**A1**	Or exact equivalent, e.g. $-\frac{1}{5\sqrt{15}}, \frac{-2}{\sqrt{30}\sqrt{50}}$. A0 if they never have a statement "$\cos\theta = ...$". ISW if they have correct "$\cos\theta = ...$" and then state the angle.

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Question	Answer	Marks	Guidance
	Alternative Method for Question 11(b)		
	Carry out the correct process for finding the lengths of the sides of triangle BMC	**M1**	$MB=\sqrt{30},\ MC=\sqrt{50},\ BC=\sqrt{84}$
	Correct use of the cosine rule as far as $\cos\theta=....$	**M1**	$\cos M=\dfrac{their\lvert\mathrm{MB}\rvert^2+their\lvert\mathrm{MC}\rvert^2-84}{2their\lvert\mathrm{MB}\rvert\times their\lvert\mathrm{MC}\rvert}$ $\left(\cos M=\dfrac{50+30-84}{2\sqrt{50}\sqrt{30}}\right)$
	Obtain $\dfrac{-1}{\sqrt{375}}$	**A1**	Or exact equivalent. A0 if they never have a statement "$\cos\theta=....$". ISW if they have correct "$\cos\theta=....$" and then state the angle.
		3	

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Question	Answer	Marks	Guidance
11(c)	Working with triangle MBC: Correct method to calculate the exact value of $\sin(\angle CMB)$	**M1**	
	$\sin(\angle CMB) = \sqrt{\frac{374}{375}}$	**A1**	Or equivalent, e.g. $\sin(\angle CMB) = \sqrt{\frac{5400}{5625}}$. A0 XP if they had changed the sign in their working for the cosine in **(b)** and for the final answer.
	Correct method to calculate the area of triangle ABC using MB and MC	**M1**	2 × area of CMB.
	$2 \times \frac{1}{2}\sqrt{30}\sqrt{50} \times \sqrt{\frac{374}{375}} = 2\sqrt{374}$	**A1**	Or exact equivalent, e.g. $2\sqrt{2}\sqrt{11}\sqrt{17}$ or $\frac{\sqrt{3366000000}}{1500}$.
	Alternative Method for Question 11(c)		
	Working with triangle ABC: correct method to calculate the exact sine of an angle in the triangle ABC	**M1**	$\cos A = \frac{56}{\sqrt{120 \times 76}}$, $\cos B = \frac{64}{\sqrt{120 \times 84}}$, $\cos C = \frac{20}{\sqrt{76 \times 84}}$
	Obtain $\sin A = \frac{4\sqrt{374}}{\sqrt{120}\sqrt{76}}$ or $\sin B = \frac{4\sqrt{374}}{\sqrt{120}\sqrt{84}}$ or $\sin C = \frac{4\sqrt{374}}{\sqrt{76}\sqrt{84}}$	**A1**	Or exact equivalent.
	Correct method to calculate the area of triangle ABC	**M1**	Must have a matching set of sides for their angle.
	$\text{Area} = \frac{1}{2}\sqrt{120}\sqrt{76}\frac{4\sqrt{374}}{\sqrt{120}\sqrt{76}}$ or $\text{area} = \frac{1}{2}\sqrt{120}\sqrt{84}\frac{4\sqrt{374}}{\sqrt{120}\sqrt{84}}$ or $\text{area} = \frac{1}{2}\sqrt{76}\sqrt{84}\frac{4\sqrt{374}}{\sqrt{76}\sqrt{84}} = 2\sqrt{374}$	**A1**	Or exact equivalent.
		4	

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