



1. A train travels along a straight horizontal track between two stations  $A$  and  $B$ .

The train starts from rest at station  $A$  and accelerates uniformly for  $T$  seconds until it reaches a speed of  $20 \text{ m s}^{-1}$

The train then travels at a constant speed of  $20 \text{ m s}^{-1}$  for 3 minutes before decelerating uniformly until it comes to rest at station  $B$ .

The magnitude of the acceleration of the train is twice the magnitude of the deceleration.

- (a) On the axes below, sketch a speed–time graph to illustrate the motion of the train as it moves from station  $A$  to station  $B$ .



If you need to redraw your graph, use the axes on page 3

(3)

Stations  $A$  and  $B$  are 4.8 km apart.

- (b) Find the value of  $T$

(5)

- (c) Find the acceleration of the train during the first  $T$  seconds of its motion.

(2)

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2. Two particles,  $A$  and  $B$ , are moving in a straight line in opposite directions towards each other on a smooth horizontal surface when they collide directly.

Particle  $A$  has mass  $3m$  kg and particle  $B$  has mass  $m$  kg.

Immediately before the collision, both particles have a speed of  $1.5 \text{ m s}^{-1}$

Immediately after the collision, the direction of motion of  $A$  is unchanged and the difference between the speed of  $A$  and speed of  $B$  is  $1 \text{ m s}^{-1}$

- (a) Find (i) the speed of  $A$  immediately after the collision,  
(ii) the speed of  $B$  immediately after the collision. (5)
- (b) Find, in terms of  $m$ , the magnitude of the impulse exerted on  $B$  in the collision. (3)

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3. A particle  $P$  is moving with constant acceleration  $(-4\mathbf{i} + \mathbf{j})\text{ms}^{-2}$

At time  $t = 0$ ,  $P$  has velocity  $(14\mathbf{i} - 5\mathbf{j})\text{ms}^{-1}$

(a) Find the speed of  $P$  at time  $t = 2$  seconds.

(3)

(b) Find the size of the angle between the direction of  $\mathbf{i}$  and the direction of motion of  $P$  at time  $t = 2$  seconds.

(3)

At time  $t = T$  seconds,  $P$  is moving in the direction of vector  $(2\mathbf{i} - 3\mathbf{j})$

(c) Find the value of  $T$

(4)

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4.

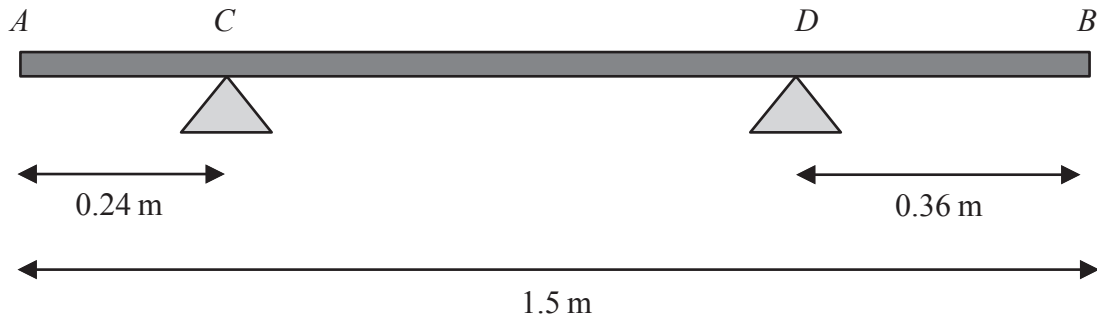


Figure 1

A branch  $AB$ , of length  $1.5\text{ m}$ , rests horizontally in equilibrium on two supports.

The two supports are at the points  $C$  and  $D$ , where  $AC = 0.24\text{ m}$  and  $DB = 0.36\text{ m}$ , as shown in Figure 1.

When a force of  $150\text{ N}$  is applied vertically upwards at  $B$ , the branch is on the point of tilting about  $C$ .

When a force of  $225\text{ N}$  is applied vertically downwards at  $B$ , the branch is on the point of tilting about  $D$ .

The branch is modelled as a non-uniform rod  $AB$  of weight  $W$  newtons.

The distance from the point  $C$  to the centre of mass of the rod is  $x$  metres.

Use the model to find

- (i) the value of  $W$
- (ii) the value of  $x$

(8)

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5.

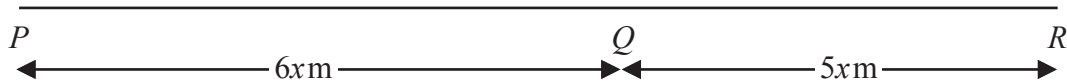


Figure 2

Three points  $P$ ,  $Q$  and  $R$  are on a horizontal road where  $PQR$  is a straight line.

The point  $Q$  is between  $P$  and  $R$ , with  $PQ = 6x$  metres and  $QR = 5x$  metres, as shown in Figure 2.

A vehicle moves along the road from  $P$  to  $Q$  with constant acceleration.

The vehicle is modelled as a particle.

At time  $t = 0$ , the vehicle passes  $P$  with speed  $u \text{ m s}^{-1}$

At time  $t = 12$  s, the vehicle passes  $Q$  with speed  $2u \text{ m s}^{-1}$

Using the model,

- (a) show that  $x = 3u$  (2)

As the vehicle passes  $Q$ , the acceleration of the vehicle changes instantaneously to  $1.5 \text{ m s}^{-2}$

The vehicle continues to move with a constant acceleration of  $1.5 \text{ m s}^{-2}$  and passes  $R$  with speed  $3u \text{ m s}^{-1}$

Using the model,

- (b) find the value of  $u$ , (3)
- (c) find the distance travelled by the vehicle during the first 14 seconds after passing  $P$  (4)

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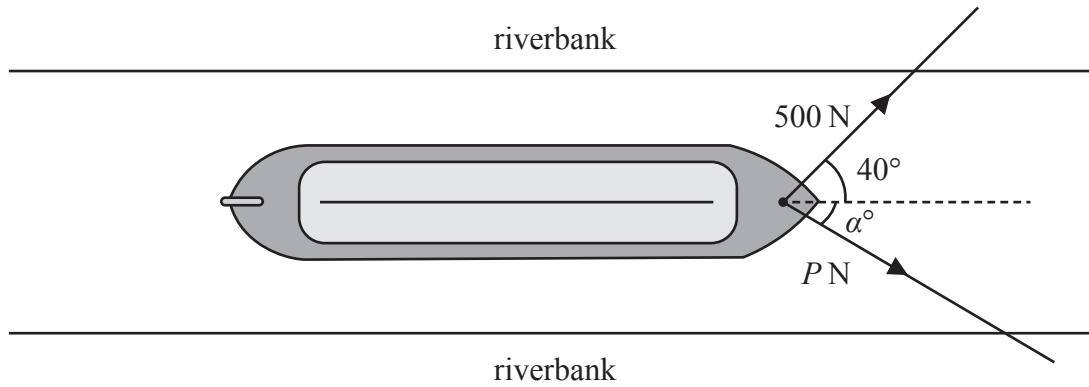


Figure 3

A boat is pulled along a river at a constant speed by two ropes.

The banks of the river are parallel and the boat travels horizontally in a straight line, parallel to the riverbanks.

- The tension in the first rope is 500 N acting at an angle of  $40^\circ$  to the direction of motion, as shown in Figure 3.
- The tension in the second rope is  $P$  newtons, acting at an angle of  $\alpha^\circ$  to the direction of motion, also shown in Figure 3.
- The resistance to motion of the boat as it moves through the water is a constant force of magnitude 900 N

The boat is modelled as a particle. The ropes are modelled as being light and lying in a horizontal plane.

Use the model to find

- the value of  $\alpha$
- the value of  $P$

(8)

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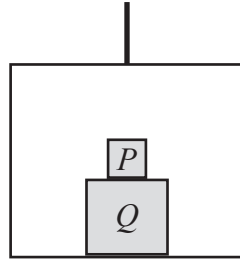


Figure 4

A simple lift operates by means of a vertical cable which is attached to the top of the lift.

The lift has mass  $m$

A box  $Q$  is placed on the floor of the lift.

A box  $P$  is placed directly on top of box  $Q$ , as shown in Figure 4.

The cable is modelled as being light and inextensible and air resistance is modelled as being negligible.

The tension in the cable is  $\frac{42mg}{5}$

The lift and its contents move vertically upwards with acceleration  $\frac{2g}{5}$

Using the model,

- (a) find, in terms of  $m$ , the combined mass of boxes  $P$  and  $Q$  (4)

During the motion of the lift, the force exerted on box  $P$  by box  $Q$  is  $\frac{14mg}{5}$

Using the model,

- (b) find, in terms of  $m$ , the mass of box  $P$  (3)

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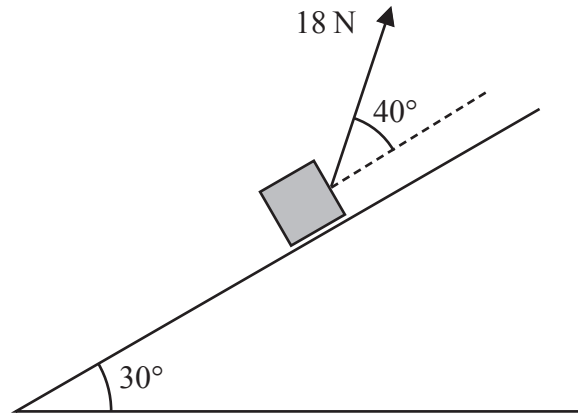


Figure 5

A parcel of mass 2 kg is pulled up a rough inclined plane by the action of a constant force.

The force has magnitude 18 N and acts at an angle of  $40^\circ$  to the plane.

The line of action of the force lies in a vertical plane containing a line of greatest slope of the inclined plane.

The plane is inclined at an angle of  $30^\circ$  to the horizontal, as shown in Figure 5.

The coefficient of friction between the plane and the parcel is 0.3

The parcel is modelled as a particle  $P$

- (a) Find the acceleration of  $P$  (8)

The points  $A$  and  $B$  lie on a line of greatest slope of the plane, where  $AB = 5$  m and  $B$  is above  $A$ . Particle  $P$  passes through  $A$  with speed  $2 \text{ m s}^{-1}$  in the direction  $AB$ .

- (b) Find the speed of  $P$  as it passes through  $B$ . (3)

The force of 18 N is removed at the instant  $P$  passes through  $B$ . As a result,  $P$  comes to rest at the point  $C$ .

- (c) Determine whether  $P$  will remain at rest at  $C$ . You must show all stages of your working clearly. (4)

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