



Mark Scheme (Results)

Summer 2018

Pearson Edexcel International A Level
In Mathematics
Statistics S3 (WST03/01)

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Summer 2018

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June 2018
WST03/01 Statistics 3
Mark Scheme

General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. **Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.**
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL IAL MATHEMATICS

General Instructions for Marking

1. The total number of marks for the paper is 75.
2. The Edexcel Mathematics mark schemes use the following types of marks:
 - **M marks: method marks are awarded for 'knowing a method and attempting to apply it',** unless otherwise indicated.
 - **A marks:** Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
 - **B marks** are unconditional accuracy marks (independent of M marks)
 - Marks should not be subdivided.
3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod – benefit of doubt
 - ft – follow through
 - the symbol \checkmark will be used for correct ft
 - cao – correct answer only
 - cso - correct solution only. There must be no errors in this part of the question to obtain this mark
 - isw – ignore subsequent working
 - awrt – answers which round to
 - SC: special case
 - oe – or equivalent (and appropriate)
 - dep – dependent
 - indep – independent
 - dp decimal places
 - sf significant figures
 - * The answer is printed on the paper
 - \square The second mark is dependent on gaining the first mark
4. **All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to** indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
 7. Ignore wrong working or incorrect statements following a correct answer.

June 2018 IAL - WST03/01 Statistics 3

Question Number	Scheme										Marks
1. (a)	Footballer	A	B	C	D	E	F	G	H	I	M1
	Rank x	1	2	3	4	5	6	7	8	9	
	Rank y	6	9	8	2	5	4	7	3	1	
	Rank x	9	8	7	6	5	4	3	2	1	
	Rank y	4	1	2	8	5	6	3	7	9	
	$\hat{\sigma} d^2 = 25 + 49 + 25 + 4 + 0 + 4 + 0 + 25 + 64 = 196$										M1 A1
	$r_s = 1 - \frac{6(196)}{9(9^2 - 1)}; = -0.63333333... \text{ or } -\frac{19}{30}$										dM1; A1
											[5]
(b)	$H_0 : \rho_s = 0, H_1 : \rho_s < 0$										B1
	Critical Value = - 0.6000 or -0.6 or CR: $r_s \leq -0.6000$										B1
	Since $r_s = -0.6333... \text{ lies in the CR (or } -0.6333 < -0.6)$, reject H_0										M1
	Either conclude that										Conclusion in context
	<ul style="list-style-type: none"> Russell's claim is true Footballers with lower BMI are slower 										
											[4]
(c)	Both Critical Value $r = -0.5822$ /CR: $r \leq -0.5822$ and										M1
	does not lie in the CR /Result is <u>not significant</u> /Do not reject H_0 (or accept H_0)										
	Conclude that there is <u>no negative correlation</u> oe Context not required here.										A1
											[2]
(d)	The relationship (between BMI and time taken to complete the obstacle course)										B1
	is non-linear oe										
											[1]
											12

Question 1 Notes

1. (a)	1st M1	Attempt to rank data for x and y at least 5 correct for each (allow reverse rankings)
	2nd M1	For finding the difference between each of the ranks and evaluating $\hat{\sigma} d^2$
	1st A1	$\hat{\sigma} d^2 = 196$ or from reverse rankings $\hat{\sigma} d^2 = 9 + 1 + 1 + 16 + 0 + 0 + 16 + 1 + 0 = 44$
	3rd dM1	is dependent on 1st M1 for use of $1 - \frac{6("196")}{9(9^2 - 1)}$ with their $\hat{\sigma} d^2$.
	2nd A1	awrt - 0.633 or $-\frac{19}{30}$ or from reverse rankings $\frac{19}{30}$
(b)	1st B1	Both hypotheses stated in terms of r or ρ_s .
	Note	One tail H_1 must be compatible with their ranking.
	2nd B1	Critical value of ± 0.6
	M1	For a correct statement relating their r_s ($ r_s < 1$) with their c.v. where $ \text{their c.v.} < 1$
	A1	For a contextualised comment which is rejecting H_0 , which must mention either " <u>negative correlation</u> ", " <u>BMI</u> " and " <u>time</u> " or " <u>lower BMI are slower</u> " o.e.
	Note	Follow through their r_s with their c.v. (provided $ \text{their c.v.} < 1$)
(c)	M1	Allow ± 0.5822 Ignore hypotheses in this part for the M1
		Use of -0.633 here is M0

Question Number	Scheme		Marks																																																							
2. (a)	$\hat{p} = \frac{7(3) + 8(5) + 9(18) + 10(28) + 11(17) + 12(4)}{12(3+5+18+28+17+4) \text{ or } 12(75)} \left\{ = \frac{738}{900} \right\} = 0.82 (*)$		Answer is given. See notes. M1 A1cso [2]																																																							
(b)	$r = 75 - {}^{12}C_9(0.82)^9(0.18)^3 \left\{ = 16.1296941\dots \right\}$ (formula) $s = 75 - (2.80 + 7.97 + \text{their } r + 22.04 + 18.26 + 6.93)$ $r = 16.1296941\dots ; s = 0.87\dots$		M1 A1; A1 [3]																																																							
(c)	H ₀ : Binomial distribution is a suitable (or good) model (or fit) H ₁ : Binomial distribution is not a suitable model		B1																																																							
	<table border="1"> <thead> <tr> <th>#</th> <th>O_i</th> <th>E_i</th> <th>Comb O_i</th> <th>Comb E_i</th> <th>$\frac{(O_i - E_i)^2}{E_i}$</th> <th>$\frac{O_i^2}{E_i}$</th> </tr> </thead> <tbody> <tr> <td>≤ 6</td> <td>0</td> <td>0.87</td> <td rowspan="3">8</td> <td rowspan="3">11.64</td> <td rowspan="3">1.1383...</td> <td rowspan="3">5.4983...</td> </tr> <tr> <td>7</td> <td>3</td> <td>2.80</td> </tr> <tr> <td>8</td> <td>5</td> <td>7.97</td> </tr> <tr> <td>9</td> <td>18</td> <td>16.13</td> <td>18</td> <td>16.13</td> <td>0.2168...</td> <td>20.0868...</td> </tr> <tr> <td>10</td> <td>28</td> <td>22.04</td> <td>28</td> <td>22.04</td> <td>1.6117...</td> <td>35.5717...</td> </tr> <tr> <td>11</td> <td>17</td> <td>18.26</td> <td>17</td> <td>18.26</td> <td>0.0869...</td> <td>15.8269...</td> </tr> <tr> <td>12</td> <td>4</td> <td>6.93</td> <td>4</td> <td>6.93</td> <td>1.2388...</td> <td>2.3088...</td> </tr> <tr> <td colspan="5" style="text-align: center;">Totals</td> <td>4.2925...</td> <td>79.2925...</td> </tr> </tbody> </table>	#	O _i	E _i	Comb O _i	Comb E _i	$\frac{(O_i - E_i)^2}{E_i}$	$\frac{O_i^2}{E_i}$	≤ 6	0	0.87	8	11.64	1.1383...	5.4983...	7	3	2.80	8	5	7.97	9	18	16.13	18	16.13	0.2168...	20.0868...	10	28	22.04	28	22.04	1.6117...	35.5717...	11	17	18.26	17	18.26	0.0869...	15.8269...	12	4	6.93	4	6.93	1.2388...	2.3088...	Totals					4.2925...	79.2925...		M1 M1
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	$X^2 = \text{awrt } 4.3$		A1																																																							
	$v = 5 - 1 - 1 = 3$		B1 ft																																																							
	$\chi_3^2(0.10) = 6.251 \Rightarrow \text{CR: } X^2 \geq 6.251$		B1 ft																																																							
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	Binomial distribution is a suitable model.	A correct conclusion (context not required here) which is based on <i>their</i> X ² -value and <i>their</i> χ ² -critical value.	A1																																																							
			[7] 12																																																							
Question 2 Notes																																																										
2. (a)	M1	At least 2 non zero products on the numerator and correct division for their method																																																								
	A1 cso	Correct answer $p = 0.82$ with no incorrect working seen																																																								
(b)	M1	For any correct method (or a correct expression) for finding either r or s .																																																								
	A1; A1	$r = \text{awrt } 16.13 ; s = \text{awrt } 0.87$																																																								
(c)	1st B1	Must have both hypotheses and mention Binomial at least once. Inclusion of 0.82 for p in hypotheses is B0 but condone in conclusion.																																																								
	1st M1	For an attempt to pool 8, 7 and ≤ 6 germinating seeds ONLY.																																																								
	2nd M1	For an attempt at the test statistic, at least 2 correct expressions/values (to awrt 2 d.p. or truncated 2 d.p.)																																																								
	1st A1	awrt 4.3																																																								
	2nd B1ft	For their evaluated $n - 1 - 1$. i.e. realising that they must subtract 2 from their n .																																																								
	3rd B1ft	For a correct fit for their $\chi_k^2(0.10)$, from their degrees of freedom																																																								
	Note	For 0.10 significance: $\chi_6^2 = 10.645$ $\chi_5^2 = 9.236$ $\chi_4^2 = 7.779$ $\chi_2^2 = 4.605$																																																								
	Final A1	Dependent on the 2nd Method mark only. A correct conclusion (context not required) which is accepting H ₀																																																								
	Note	No follow through on their hypotheses if they are stated the wrong way round.																																																								
	Note	Contradictory statements score A0. E.g. “significant, do not reject H ₀ ”.																																																								
	Note	Condone mentioning of B(12, 0.82) in conclusion.																																																								

Question Number	Scheme	Marks
3. (a)	$\left\{ \hat{m}_x = \bar{x} = \frac{92.0}{20} \Rightarrow \right\} \bar{x} = 4.6 \text{ (cm)}$	4.6 B1
	$\left\{ \hat{S}_x^2 = \right\} s_x^2 = \frac{433.4974 - 20(4.6)^2}{20 - 1} = 0.541968... \text{ (cm)}^2$	Applies $\frac{\hat{a}x^2 - 20(\text{their } \bar{x})^2}{20 - 1}$ M1
		awrt 0.542 A1
		[3]
(b)	Combined Sample: Mean = $\frac{92.0 + 142.5}{20 + 30} = 4.69$	4.69 B1 Can be implied.
	$s^2 = \frac{433.4974 + 689.5078 - 50(4.69)^2}{20 + 30 - 1}; = 0.4734734694$	awrt 0.473 or 0.4735 (can be implied) M1; A1
	$\frac{s}{\sqrt{n}} = \frac{\sqrt{0.4734734694...}}{\sqrt{50}}; = 0.09731119868...$	For use of s/√50 M1; awrt 0.0973 A1
		[5]
(c)	$H_0 : m = 4.5 \quad H_1 : m > 4.5$	Correct hypotheses B1
	$z = \frac{"4.69" - 4.5}{\frac{0.71}{\sqrt{50}}}; = 1.892257583...$	$\pm \frac{\text{their } 4.69 - 4.5}{\frac{0.71}{\sqrt{50}}}$ or equivalent. M1; awrt 1.89 A1
	One tailed c.v. $Z = 1.6449$ or CR: $Z \geq 1.6449$ or p-value = awrt 0.029 or awrt $0.029 < 0.05$	Critical value of 1.6449 or a correct probability comparison. B1
	[in the CR/significant/Reject $H_0/ 0.029 < 0.05$]	
	Conclude either <ul style="list-style-type: none"> there is evidence to <u>support</u> the <u>farmer's claim</u> that the <u>mean width</u> of duck <u>eggs</u> is <u>greater than 4.5</u> cm. 	A correct conclusion which is rejecting H_0 in context and is based on <i>their</i> z-value and <i>their</i> critical value, where $ c.v. > 1$. A1
	[5]	
		13

Question 3 Notes

3. (a)	M1	Also allow M1 for applying $\frac{20}{(20 - 1)} \left(\frac{\sum x^2}{20} - (\text{their } \bar{x})^2 \right)$
(b)	1st M1	Also allow 1 st M1 for applying $\frac{50}{(50 - 1)} \left(\frac{\sum x^2 + \sum y^2}{20 + 30} - (\text{their } \bar{x}_{\text{comb}})^2 \right)$
	Note	Award B1M1A1M1A1 for awrt 0.0973 which follows from no working.
(c)	1st M1	Condone use of 4.6 for this M1 mark.
	2nd A1	Conclusion must refer to either "farmer's claim" or "mean width" and "eggs".

Question Number	Scheme	Marks																												
4. (a)	<p>H_0 : Mean number of reported first-aid incidents per 1000 employees is the <u>same</u> at each warehouse.</p> <p>H_1 : Mean number of reported first-aid incidents per 1000 employees is <u>not the same</u>.</p>	B1																												
	<table border="1" data-bbox="225 405 756 853"> <thead> <tr> <th>Warehouse</th> <th>Calculation</th> <th>Expected</th> </tr> </thead> <tbody> <tr> <td>A</td> <td>$\frac{(2)(114)}{12}$</td> <td>19</td> </tr> <tr> <td>B</td> <td>$\frac{(1)(114)}{12}$</td> <td>9.5</td> </tr> <tr> <td>C</td> <td>$\frac{(3.8)(114)}{12}$</td> <td>36.1</td> </tr> <tr> <td>D</td> <td>$\frac{(3)(114)}{12}$</td> <td>28.5</td> </tr> <tr> <td>E</td> <td>$\frac{(2.2)(114)}{12}$</td> <td>20.9</td> </tr> </tbody> </table>	Warehouse	Calculation	Expected	A	$\frac{(2)(114)}{12}$	19	B	$\frac{(1)(114)}{12}$	9.5	C	$\frac{(3.8)(114)}{12}$	36.1	D	$\frac{(3)(114)}{12}$	28.5	E	$\frac{(2.2)(114)}{12}$	20.9	<p>Some attempt at using the correct formula to find their 5 expected values (expected number of incidents). Can be implied by at least one correct E_i.</p> <p>All expected frequencies are correct.</p>										
Warehouse	Calculation	Expected																												
A	$\frac{(2)(114)}{12}$	19																												
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Observed	Expected	$\frac{(O - E)^2}{E}$	$\frac{O^2}{E}$																											
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10	9.5	0.0263...	10.5263...																											
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23	20.9	0.2110...	25.3110...																											
Totals		1.7200...	115.72...																											
	$X^2 = \sum \frac{(O - E)^2}{E} \text{ or } \sum \frac{O^2}{E} - 114 = \text{awrt } 1.72$	awrt 1.72 A1																												
	$n = 5 - 1 = 4 \Rightarrow \chi_4^2(0.05) = 9.488 \Rightarrow \text{CR: } X^2 \geq 9.488$	9.488 B1																												
	[not in the CR/not significant/Do not Reject H_0 /Accept H_0]																													
	<p>Conclude either:</p> <ul style="list-style-type: none"> • <u>manager's claim</u> is supported • that the mean number of reported first-aid incidents per 1000 employees is <u>the same</u> at each warehouse. 	<p>A correct conclusion in context which is based on <i>their</i> X^2 value and <i>their</i> χ^2-critical value.</p>																												
		[7]																												
	(b) Select every 4 th record from warehouse C.	B1																												
	{having chosen the first record by}																													
	selecting a random number.	dB1																												
		[2]																												
		9																												
Question 4 Notes																														

(a)
SC 1

Expected values of 9.5 used

Observed	Expected	$\frac{(O - E)^2}{E}$
7.5	9.5	0.4210...
10	9.5	0.0263...
10.5...	9.5	0.1108...
8.6...	9.5	0.0730...
10.4...	9.5	0.0959...
Totals		0.727...

Can score B1M1A0M1A0B1A1ft (5 out of 7)

SC 2

Expected values of 9.43... used

Observed	Expected	$\frac{(O - E)^2}{E}$	$\frac{O^2}{E}$
7.5	9.43	0.3948...	5.965...
10	9.43	0.0345...	10.6050...
10.5...	9.43	0.1275...	11.7507...
8.6...	9.43	0.0617...	7.9655...
10.4...	9.43	0.1114...	11.5910...
Totals		0.729...	47.877...

Can score B1M1A0M1A0B1A0 (4 out of 7)

(b)

Use of 3800 in part (b) is B0B0

Question Number	Scheme	Marks
5.	95% CI for m is (30.612, 31.788); $c\%$ CI for m is (30.66, 31.74)	
(a)	$\frac{2(1.96)S}{\sqrt{25}} = 31.788 - 30.612 \{= 1.176\}$	M1 oe
	$\frac{2zS}{\sqrt{25}} = 31.788 - 30.612$	1.96 B1
	$\left\{ \Rightarrow S = \frac{(1.176)(5)}{2(1.96)} \Rightarrow \right\} S = 1.5$	$S = 1.5$ A1
		[3]
(b)	$\frac{2z(1.5)}{\sqrt{25}} = 31.74 - 30.66 \{= 1.08\}$	M1 oe
	$\frac{2z("1.5")}{\sqrt{25}} = 31.74 - 30.66$	$z = 1.8$ A1ft
	$z = \frac{(1.08)(5)}{2("1.5")} \rightarrow z = 1.8$	$z = 1.8$ A1ft
	$\left[\frac{c}{100} = \right] 2(0.9641) - 1$	2F(their "1.8") - 1 oe M1
	$\Rightarrow c = 92.8$ (3sf)	awrt 92.8 A1
		[4]
		7

Question 5 Notes

5. (a)	M1	Also allow M1 (oe) for $31.2 + \frac{\text{"their } z" S}{\sqrt{25}} = 31.778$, where $31.2 = \frac{30.612 + 31.778}{2}$
(b)	1st M1	Also allow M1 (oe) for $31.2 + \frac{z(\text{"their "1.5"})}{\sqrt{25}} = 31.74$, where $31.2 = \frac{30.66 + 31.74}{2}$
	1st A1ft	For a correct (ft) expression using their value of σ
	2nd M1	awrt 0.928 implies this mark
	Note	Use of 1.6449 gives $\sigma = 1.787\dots$ and leads to $z = 1.51\dots$ and $c = 86.9$ (3sf) (M1A1ftM1A0)

Question Number	Scheme	Marks
6.	Y has a continuous uniform distribution $[a - 3, a + 6]$	
(a)	$E(Y) = \frac{a+6+a-3}{2} \left\{ = \frac{(2a+3)}{2} \text{ or } a + \frac{3}{2} \right\}$	M1
	$\text{Var}(Y) = \frac{(a+6-a+3)^2}{12} \left\{ = \frac{81}{12} \text{ or } \frac{27}{4} \text{ or } 6.75 \right\}$	May be implied M1
	$\bar{Y} \sim N\left(a + \frac{3}{2}, \frac{9}{80}\right)$	$N\left(a + \frac{3}{2}, \frac{9}{80}\right)$ A1
		[3]
(b)	$13.4 - 2.3263\sqrt{\frac{9}{80}} < m < 13.4 + 2.3263\sqrt{\frac{9}{80}}$	$13.4 \pm "z"(their SE_{\bar{y}})$ 2.3263 M1 B1
	$13.4 - 2.3263\sqrt{\frac{9}{80}} < a + \frac{3}{2} < 13.4 + 2.3263\sqrt{\frac{9}{80}}$	
	$13.4 - 2.3263\sqrt{\frac{9}{80}} + 4.5 < a + 6 < 13.4 + 2.3263\sqrt{\frac{9}{80}} + 4.5$	$13.4 \pm "z"(their SE_{\bar{y}}) + 4.5$ M1
	$17.11973576... < a + 6 < 18.68026474...$	awrt (17.1, 18.7) A1
		[4]
	Alternative Method for part (b)	
(b)	$13.4 - 2.3263\sqrt{\frac{9}{80}} < m < 13.4 + 2.3263\sqrt{\frac{9}{80}}$	$13.4 \pm "z"(their SE_{\bar{y}})$ 2.3263 M1 B1
	$11.11973526... < a < 12.68026474...$	
	$11.11973526... + 6 < a + 6 < 12.68026474... + 6$	$13.4 \pm "z"(their SE_{\bar{y}}) - 1.5 + 6$ M1
	$17.11973576... < a + 6 < 18.68026474...$	awrt (17.1, 18.7) A1
		[4]
		7
Question 6 Notes		
(b)	1 st M1 The inequalities may be seen separately. For only considering 1-tail of confidence interval (usually the upper tail) allow access to 1 st M1 only (so M1B1M0A0 is possible). A second division of their SE by 60 is 1 st M0	

Question Number	Scheme		Marks	
7. (i) (a)	$A \sim N(21, 2^2), B \sim N(32, 7^2)$ and $C \sim N(45, 9^2)$ A, B, C are independent.			
	$T = A + B + C$			
	$E(T) = 21 + 32 + 45$ or $\text{Var}(T) = 2^2 + 7^2 + 9^2$	A fully correct method of finding $E(T)$ or $\text{Var}(T)$	M1	
	$E(T) = 98$ and $\text{Var}(T) = 134$	Both $E(T) = 98$ and $\text{Var}(T) = 134$	A1	
	{So $T \sim N(98, 134)$ }			
	$\{P(T > 90) = \}$ $P\left(Z > \frac{90 - 98}{\sqrt{134}}\right)$	Standardising (\pm) with their mean and their standard deviation	M1	
	$= P(Z > -0.69109\dots)$			
	$= 0.7549$ (or $0.75525\dots$)	awrt 0.755	A1	
			[4]	
	(b)	$\{P(A > B) = P(A - B > 0)\}$		
		$E(A - B) = 21 - 32$ or $\text{Var}(T) = 2^2 + 7^2$	A fully correct method of finding $E(A - B)$ or $\text{Var}(A - B)$	M1
		$E(A - B) = -11$ and $\text{Var}(A - B) = 53$	Both $E(A - B) = -11$ and $\text{Var}(A - B) = 53$	A1
{So $A - B \sim N(-11, 53)$ }				
$\{P(A - B > 0)\} \Rightarrow P\left(Z > \frac{0 - (-11)}{\sqrt{53}}\right)$		Standardising (\pm) with their mean and their standard deviation	M1	
$= P(Z > 1.510966\dots)$				
	$= 0.06539855\frac{1}{4}$ (or 0.0655)	0.0655 or awrt 0.0654	A1	
		[4]		
(ii)	$\{P(X_1 > \bar{X} + kS) = 0.1 \Rightarrow P(X_1 - \bar{X} > kS) = 0.1\}$			
	$X_1 - \bar{X}; \left\{ = X_1 - \frac{(X_1 + X_2 + X_3 + X_4)}{4} = \frac{3X_1 - (X_2 + X_3 + X_4)}{4} \right\}$	For attempting to find the distribution of $X_1 - \bar{X}$	M1	
	$E(X_1 - \bar{X}) = 0$	Correct mean	A1	
	$\text{Var}(X_1 - \bar{X}) = \frac{9\sigma^2 + 3\sigma^2}{4^2}; \Rightarrow X_1 - \bar{X} \sim N(0, 0.75\sigma^2)$	Correct expression for $\text{Var}(X_1 - \bar{X})$	dM1	
		$X_1 - \bar{X} \sim N(0, 0.75S^2)$	A1	
	$\left\{ P(X_1 - \bar{X} > kS) = 0.1 \Rightarrow P\left(Z > \frac{kS - 0}{\sqrt{0.75S^2}}\right) = 0.1 \right\}$			
	So, $\frac{k}{\sqrt{0.75}} = 1.2816$	Standardising using their $\sqrt{\text{Var}(X_1 - \bar{X})}$. Note that S must cancel and equating to a z-value, $ z > 1$.	M1	
		1.2816	B1	
$\{k = \sqrt{0.75} (1.2816)\} \Rightarrow k = 1.109898157\dots$	awrt 1.11	A1		
		[7]		
			15	

Question 7 Notes

7. (i) (a)	1st M1	Can be implied by either a correct $E(T)$ or $\text{Var}(T)$
(i) (b)		Allow equivalent method using $B - A < 0$
(ii)	Final A1	Dependent upon all previous M marks in (ii)

