


Please check the examination details below before entering your candidate information

Candidate surname	Other names
<b>Pearson Edexcel</b>	Centre Number
<b>International GCSE</b>	Candidate Number
<b>Friday 10 January 2020</b>	
Morning (Time: 2 hours)	Paper Reference <b>4PM1/01</b>
<p style="text-align: center;"><b>Further Pure Mathematics</b></p> <p><b>Level 2</b></p> <p><b>Paper 1</b></p> <div style="text-align: right; margin-top: 10px;">  </div>	
<b>Calculators may be used.</b>	Total Marks

**Instructions**

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.  
Anything you write on the formulae page will gain NO credit.

**Information**

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

**Advice**

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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## International GCSE in Further Pure Mathematics Formulae sheet

**Mensuration**Surface area of sphere =  $4\pi r^2$ Curved surface area of cone =  $\pi r \times$  slant heightVolume of sphere =  $\frac{4}{3}\pi r^3$ **Series****Arithmetic series**Sum to  $n$  terms,  $S_n = \frac{n}{2}[2a + (n-1)d]$ **Geometric series**Sum to  $n$  terms,  $S_n = \frac{a(1-r^n)}{(1-r)}$ Sum to infinity,  $S_\infty = \frac{a}{1-r}$   $|r| < 1$ **Binomial series** $(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots$  for  $|x| < 1, n \in \mathbb{Q}$ **Calculus****Quotient rule (differentiation)**

$$\frac{d}{dx} \left( \frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

**Trigonometry****Cosine rule**In triangle  $ABC$ :  $a^2 = b^2 + c^2 - 2bc \cos A$ 

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

**Logarithms**

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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**Question 1 continued**

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**Question 1 continued**

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**(Total for Question 1 is 9 marks)**



2 (a) On the grid below, draw the line with equation

(i)  $5x + 2y = 10$       (ii)  $y = x$

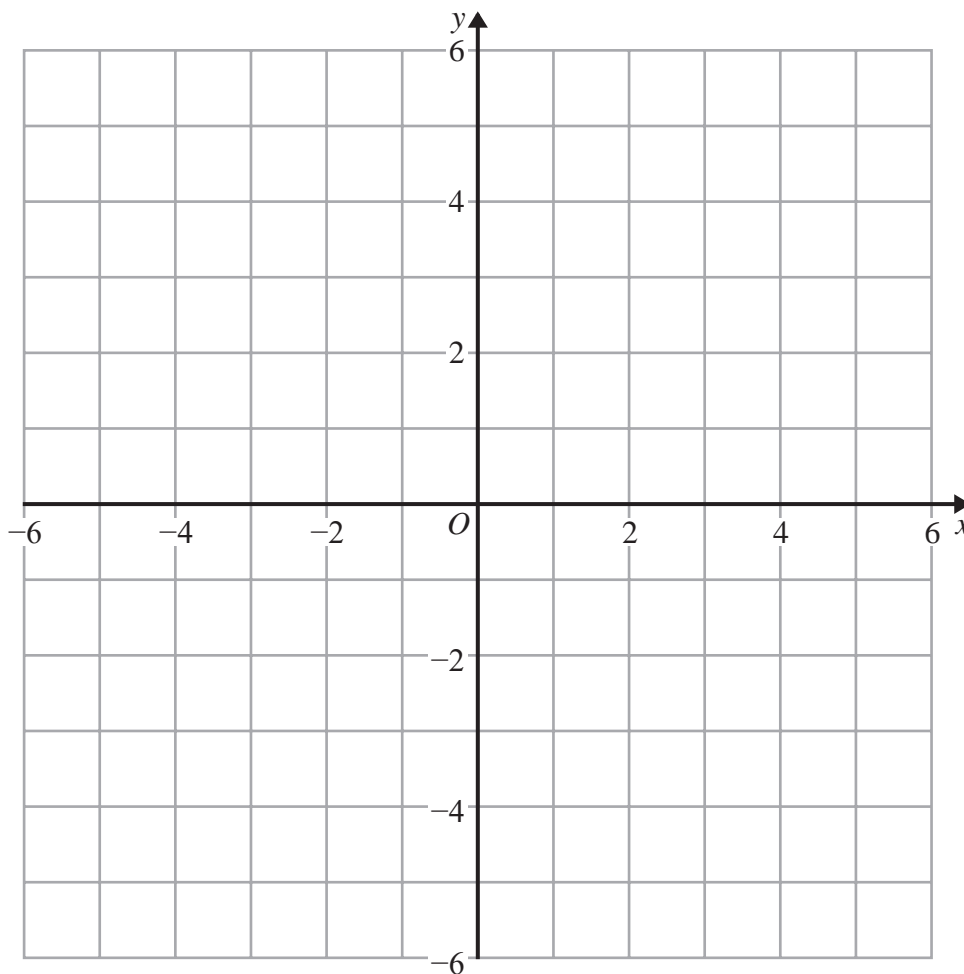
(2)

(b) Show, by shading on the grid, the region  $R$  defined by the inequalities

$y \leq x$        $5x + 2y \leq 10$        $y \geq -2$        $x \geq 1$

Label the region  $R$ .

(2)



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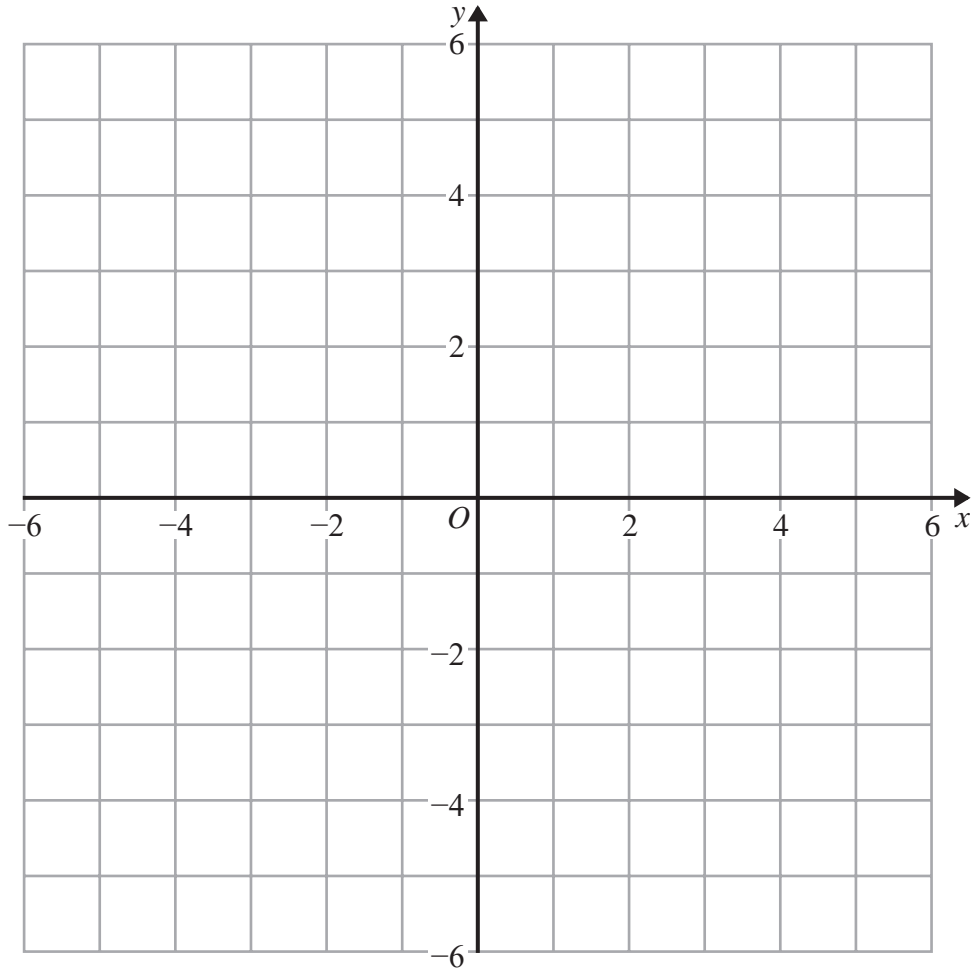
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**Question 2 continued**

**Only use this grid if you need to redraw your graph.**



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**(Total for Question 2 is 4 marks)**



3 Given that  $(x - 4)$  is a factor of  $px^3 - 31x^2 + 25x + 12$  where  $p$  is a constant,

(a) show that  $p = 6$

(2)

(b) Solve the equation  $6x^3 - 31x^2 + 25x + 12 = 0$

Show clear algebraic working.

(4)

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**Question 3 continued**

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**(Total for Question 3 is 6 marks)**





**Question 4 continued**

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**(Total for Question 4 is 6 marks)**



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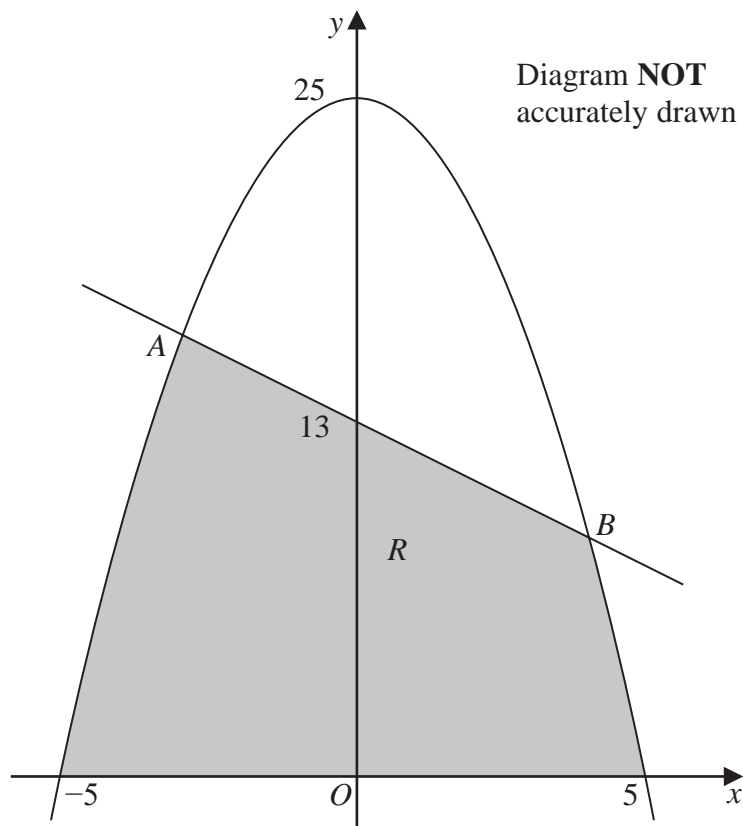


Figure 2

Figure 2 shows part of the curve with equation  $y = 25 - x^2$  and part of the line with equation  $y + x = 13$

The curve and the line intersect at the points  $A$  and  $B$ .

- (a) Use algebra to find the coordinates of  $A$  and the coordinates of  $B$ . (4)

The region  $R$ , shown shaded in Figure 2, is bounded by the curve, the straight line and the  $x$ -axis.

- (b) Use algebraic integration to find the area of  $R$ . (7)

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**Question 5 continued**

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**Question 5 continued**

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- 6 The point  $A$  has coordinates  $(3, 0)$  and the point  $B$  has coordinates  $(2, 2)$ .  
The line  $L_1$  passes through  $B$  and is perpendicular to  $AB$ .

- (a) Find an equation of  $L_1$

Give your answer in the form  $ax + by + c = 0$

(5)

The line  $L_2$  with equation  $x - 7y - 3 = 0$  intersects the line  $L_1$  at the point  $C$ .  
The midpoint of  $AC$  is  $M$ .

- (b) Find the coordinates of  $M$ .

(5)

- (c) Find the area of the triangle  $ABM$ .

(4)

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**Question 6 continued**

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**Question 6 continued**

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**(Total for Question 6 is 14 marks)**



7 Solve the equation

$$\log_7(8x^2 - 6x + 3) - \log_{49}x^2 = 3\log_7 2$$

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**Question 7 continued**

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**(Total for Question 7 is 5 marks)**





**Question 8 continued**

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**Question 8 continued**

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**(Total for Question 8 is 11 marks)**



- 9 (a) Expand  $\sqrt{1 - 4x}$  in ascending powers of  $x$  up to and including the term in  $x^3$ , giving each coefficient as an integer. (3)
- (b) Use your expansion with a suitable value for  $x$  to obtain an estimate of  $\sqrt{0.76}$ . Give your answer correct to 4 decimal places. (3)
- (c) Hence find, to 3 decimal places, an estimate of  $\sqrt{19}$ . (2)

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**Question 9 continued**

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**Question 9 continued**

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**(Total for Question 9 is 8 marks)**



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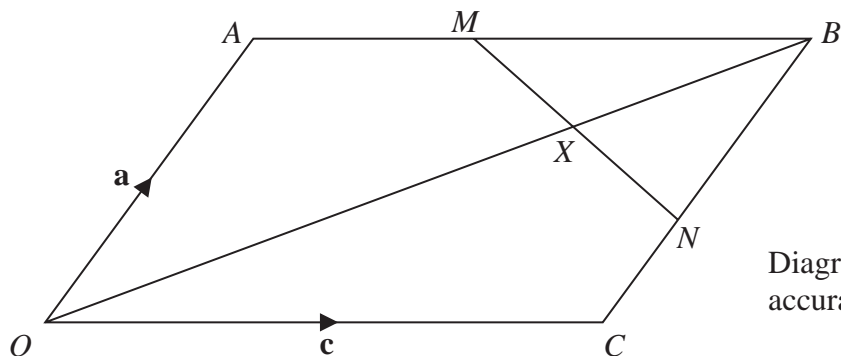


Diagram NOT accurately drawn

Figure 3

Figure 3 shows the parallelogram  $OABC$

$$\vec{OA} = \mathbf{a} \quad \vec{OC} = \mathbf{c}$$

The midpoint of  $AB$  is  $M$  and the midpoint of  $BC$  is  $N$ .

The line  $OB$  intersects  $MN$  at the point  $X$ .

(a) Find in terms of  $\mathbf{a}$  and  $\mathbf{c}$ ,

(i)  $\vec{OB}$

(ii)  $\vec{MN}$

(2)

Given  $\vec{MX} = \lambda \vec{MN}$  and that  $\vec{OX} = \mu \vec{OB}$ ,

(b) use a vector method to find the value of  $\lambda$  and the value of  $\mu$ .

(8)

(c) Hence find, in its simplest form, the ratio

Area of quadrilateral  $OXNC$  : Area of parallelogram  $OABC$ .

(3)

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**Question 10 continued**

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**Question 10 continued**

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**(Total for Question 10 is 13 marks)**



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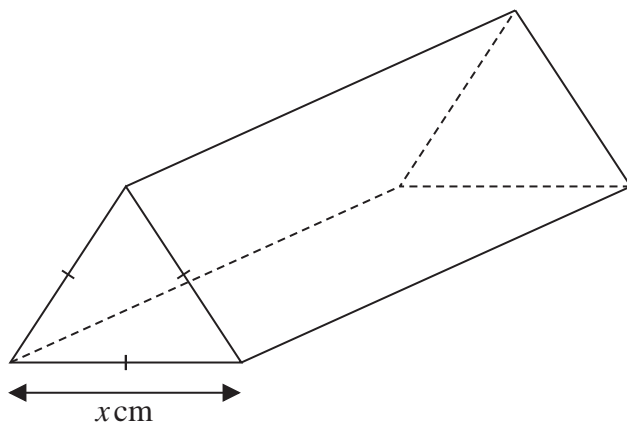


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Figure 4

A company manufactures chocolate bars that are inside packaging that is in the shape of a right triangular prism.

The cross section of the prism is an equilateral triangle with sides of length  $x$  cm, as shown in Figure 4.

The volume of the prism is  $72 \text{ cm}^3$

The total surface area of the prism is  $S \text{ cm}^2$

(a) Show that

$$S = \frac{\sqrt{3}x^2}{2} + \frac{288\sqrt{3}}{x} \tag{6}$$

Given that  $x$  can vary,

(b) use calculus to find, to 4 significant figures, the value of  $x$  for which  $S$  is a minimum, justifying that this value gives a minimum value of  $S$ . (5)

(c) Find, to 3 significant figures, the minimum value of  $S$ . (2)

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**Question 11 continued**

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