

Please check the examination details below before entering your candidate information

Candidate surname		Other names	
Pearson Edexcel International GCSE		Centre Number 	Candidate Number
Monday 15 June 2020			
Afternoon (Time: 2 hours)		Paper Reference 4PM1/01	
Further Pure Mathematics Paper 1			
Calculators may be used.			Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

International GCSE in Further Pure Mathematics Formulae sheet

Mensuration

Surface area of sphere = $4\pi r^2$

Curved surface area of cone = $\pi r \times$ slant height

Volume of sphere = $\frac{4}{3}\pi r^3$

Series

Arithmetic series

Sum to n terms, $S_n = \frac{n}{2}[2a + (n-1)d]$

Geometric series

Sum to n terms, $S_n = \frac{a(1-r^n)}{(1-r)}$

Sum to infinity, $S_\infty = \frac{a}{1-r} \quad |r| < 1$

Binomial series

$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$

Calculus

Quotient rule (differentiation)

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry

Cosine rule

In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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Answer all ELEVEN questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1 Differentiate with respect to x

$$6e^{3x^2} \cos 2x$$

(3)

(Total for Question 1 is 3 marks)



P 6 2 2 8 0 A 0 3 3 2

- 2 (a) Using the axes below sketch the line with equation

(i) $y = 6$

(ii) $y + x = 10$

(iii) $y = 2x - 5$

Show the coordinates of any point where each line crosses the coordinate axes.

(3)

- (b) Show, by shading on your sketch, the region R defined by the inequalities

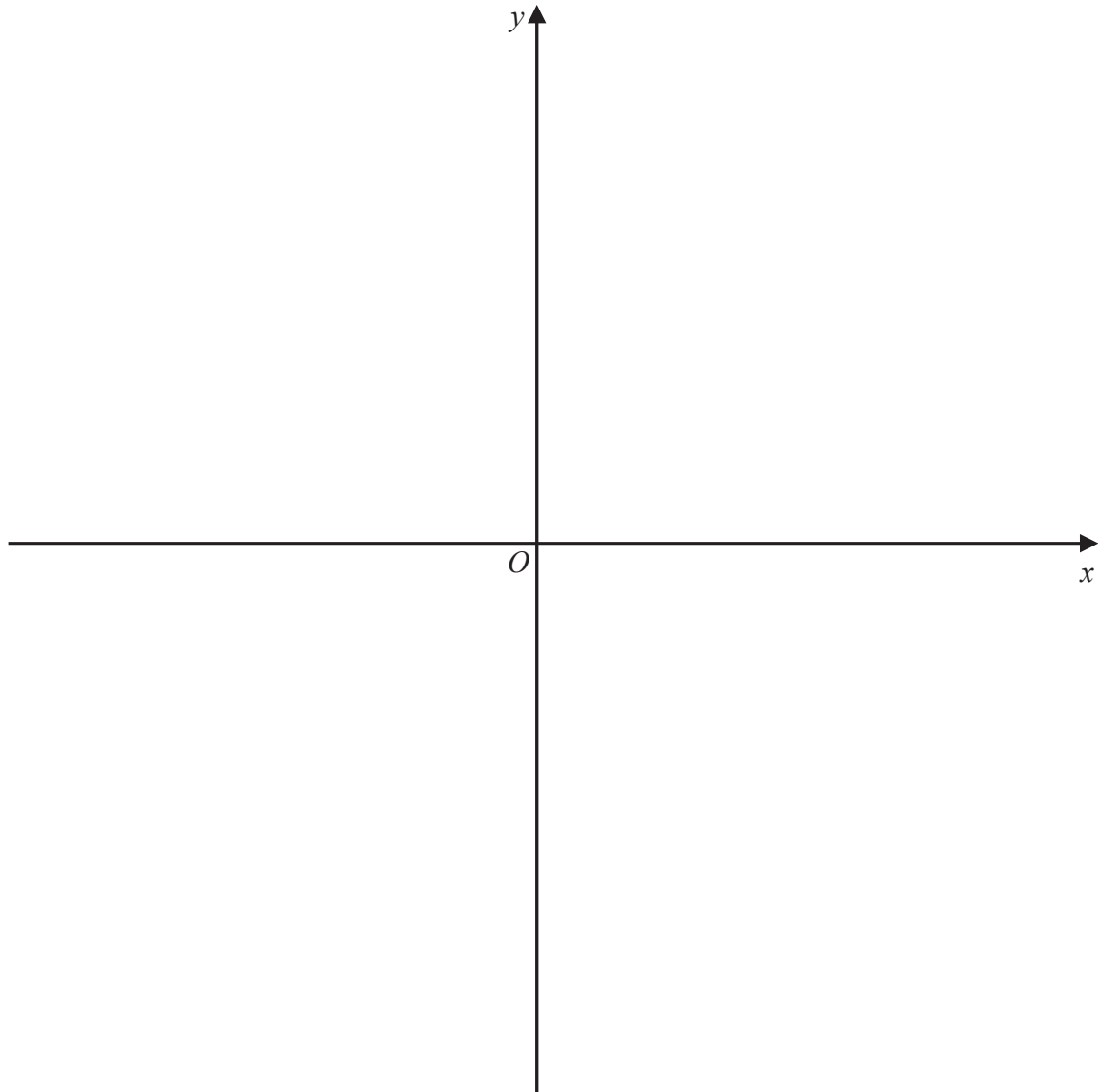
$y \leq 6$

$y + x \leq 10$

$y \geq 2x - 5$

$x \geq 0$

(1)



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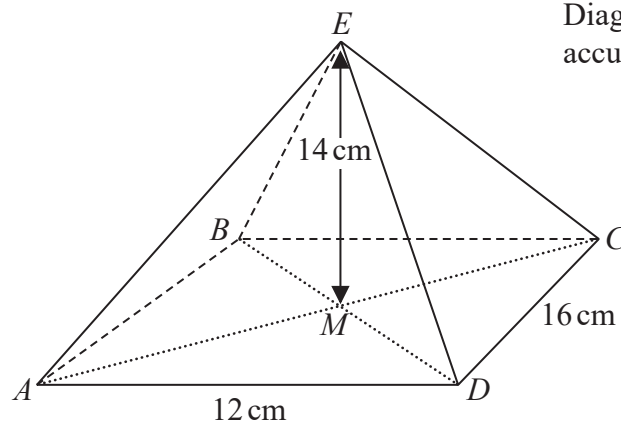


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accurately drawn

Figure 1

Figure 1 shows the right pyramid $ABCDE$. The base, $ABCD$, of the pyramid is a horizontal rectangle with $AD = 12$ cm and $CD = 16$ cm. The height ME of the pyramid is 14 cm where M is the point of intersection of the diagonals of the base.

The sloping edges, EA , EB , EC and ED of the pyramid are all of equal length.

- (a) Calculate, to 3 significant figures, the length of a sloping edge.

(3)

Calculate, in degrees to one decimal place, the size of

- (b) the angle between AE and the base,

(3)

- (c) the angle between the plane AED and the base.

(3)

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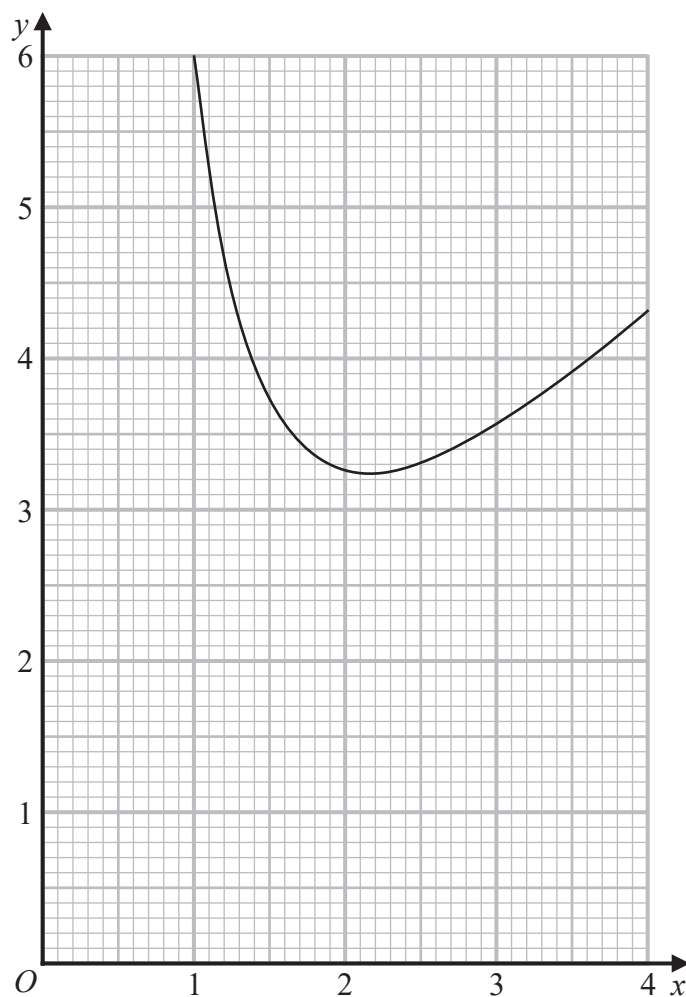


Figure 2

Figure 2 shows the graph of $y = x + \frac{5}{x^2}$ for $1 \leq x \leq 4$ drawn on a grid.

- (a) By drawing a suitable straight line on the grid, obtain estimates, to one decimal place, for the roots of the equation

$$x^3 - 4x^2 + 5 = 0$$

in the interval $1 \leq x \leq 4$

(3)

- (b) By drawing a suitable straight line on the grid, obtain an estimate, to one decimal place, for the root of the equation

$$x^3 - x^2 - 5 = 0$$

in the interval $1 \leq x \leq 4$

(4)

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Question 4 continued

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(Total for Question 4 is 7 marks)



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(Total for Question 3 is 7 marks)



- (4)

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Question 6 continued

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(Total for Question 6 is 10 marks)



7

$$f(x) = x^2 - 9x + 14$$

Given that $f(x)$ can be written in the form $(x + a)^2 + b$, where a and b are constants,

(a) find the value of a and the value of b . (2)

(b) Hence, or otherwise, find

- (i) the minimum value of $f(x)$
- (ii) the value of x for which this minimum occurs. (2)

The curve C has equation $y = f(x)$

The line l has equation $y = x + 5$

(c) Use algebra to find the coordinates of the points of intersection of C and l . (4)

(d) Use algebraic integration to find the exact area of the finite region bounded by C and l . (5)

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Question 7 continued

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Question 7 continued

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Question 7 continued

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(Total for Question 7 is 13 marks)



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Question 8 continued

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Question 8 continued

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(Total for Question 8 is 10 marks)



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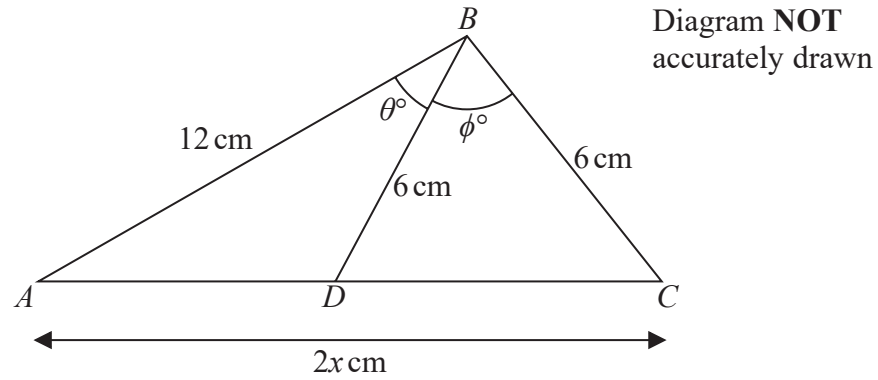


Figure 3

Figure 3 shows triangle ABC with $AB = 12$ cm, $BC = 6$ cm and $AC = 2x$ cm.

The point D is the midpoint of AC and $BD = 6$ cm.

$\angle ABD = \theta^\circ$ and $\angle DBC = \phi^\circ$ where $\theta \neq 0$ and $\phi \neq 0$

(a) Show that $\cos ADB = \frac{x^2 - 108}{12x}$ (2)

(b) Hence, or otherwise, show that $AC = 6\sqrt{6}$ cm. (4)

(c) Show that $\sin(\theta^\circ + \phi^\circ) = \sin \phi^\circ$ (4)

(d) Hence show that $\theta = 180 - 2\phi$ (2)

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Question 9 continued

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Question 9 continued

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(Total for Question 5 is 12 marks)



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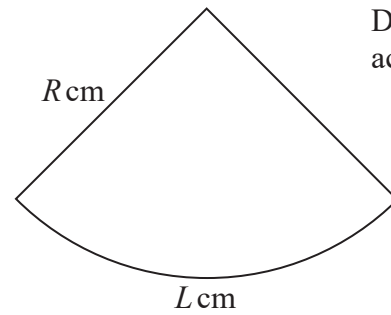
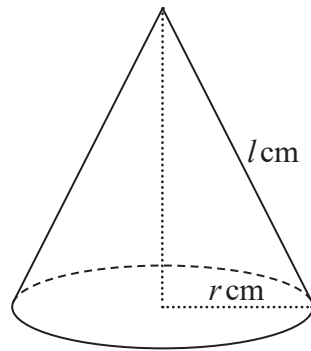


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accurately drawn

Figure 4

Figure 4 shows a right circular cone with base radius $r \text{ cm}$ and slant height $l \text{ cm}$.
Figure 4 also shows a sector of a circle with radius $R \text{ cm}$ and arc length $L \text{ cm}$.

The area of the curved surface of the cone is $A \text{ cm}^2$

By considering how the sector of the circle can be folded to exactly form the curved surface of the cone with R and L suitably chosen,

- (a) prove that $A = \pi r l$

(4)

Sand is poured onto a horizontal surface at a constant rate of $1.5 \text{ cm}^3/\text{s}$.

The sand forms a pile in the shape of a right circular cone with its base on the surface.

The curved surface area of the cone, $A \text{ cm}^2$, increases in such a way that the height of the cone is always three times the radius of the base of the cone.

Given that $\frac{dA}{dr} = k\pi r$, where k is a constant,

- (b) find the exact value of k .

(3)

- (c) Calculate the rate, in cm^2/s , to 3 significant figures, at which the curved surface area of the pile is increasing when the height of the pile is 24 cm .

(5)

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Question 10 continued

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Question 10 continued

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Question 10 continued

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(Total for Question 10 is 12 marks)



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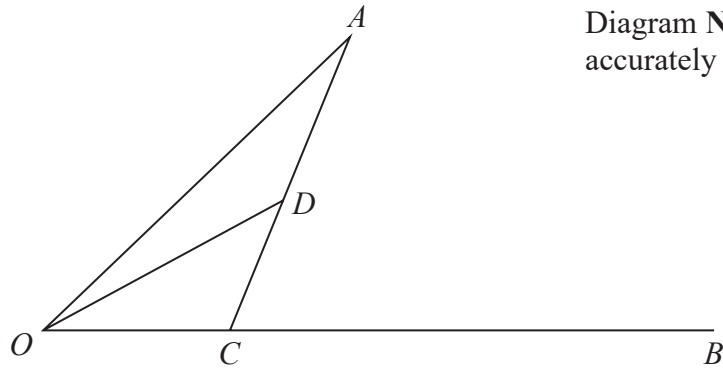
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Figure 5

In Figure 5, $\vec{OA} = \mathbf{a}$ and $\vec{OB} = \mathbf{b}$

The point C divides OB in the ratio $1:3$

The point D is the midpoint of AC

(a) Find, as a simplified expression in terms of $\mathbf{a}$ and $\mathbf{b}$

(i) $\vec{AC}$

(ii) $\vec{OD}$

(iii) $\vec{BD}$

(5)

The point E is such that $\vec{OE} = \lambda \vec{OA}$

Given that E , D and B are collinear

(b) find the value of λ

(4)

Given that $\frac{\text{area } \triangle OAC}{\text{area } \triangle OEB} = \mu$

(c) find the value of μ

(4)

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Question 11 continued

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Question 11 continued

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TOTAL FOR PAPER IS 100 MARKS

