

Please check the examination details below before entering your candidate information

Candidates surname	Other names
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Centre Number	Candidate Number
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Pearson Edexcel International GCSE

Time 2 hours	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="padding: 2px 5px;">Paper reference</td> <td style="text-align: center; font-size: 24px; font-weight: bold;">4PM1/02</td> </tr> </table>	Paper reference	4PM1/02
Paper reference	4PM1/02		

Further Pure Mathematics

PAPER 2



Calculators may be used.	Total Marks
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Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

International GCSE in Further Pure Mathematics Formulae sheet

MensurationSurface area of sphere = $4\pi r^2$ Curved surface area of cone = $\pi r \times$ slant heightVolume of sphere = $\frac{4}{3}\pi r^3$ **Series****Arithmetic series**Sum to n terms, $S_n = \frac{n}{2}[2a + (n-1)d]$ **Geometric series**Sum to n terms, $S_n = \frac{a(1-r^n)}{(1-r)}$ Sum to infinity, $S_\infty = \frac{a}{1-r} \quad |r| < 1$ **Binomial series** $(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots$ for $|x| < 1, n \in \mathbb{Q}$ **Calculus****Quotient rule (differentiation)**

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry**Cosine rule**In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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Answer all ELEVEN questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

- 1 Find the set of values of k for which the equation

$$2kx^2 + 5kx + 5k - 3 = 0 \quad \text{where } k \neq 0$$

has real roots.

(4)

(Total for Question 1 is 4 marks)



- 2 A particle P moves along the x -axis. At time t seconds, the displacement, x metres, of P from the origin O is given by

$$x = t^4 - 13.5t + 12$$

- (a) Find the velocity, in m/s, of P when $t = 3$ (2)
- (b) Find the value of t for which P is instantaneously at rest. (2)
- (c) Find the acceleration, in m/s^2 , of P when $t = 2$ (2)

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Question 2 continued

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(Total for Question 2 is 6 marks)



3 O , A and B are fixed points such that

$$\vec{OA} = (p\mathbf{i} - 4\mathbf{j}) \quad \vec{OB} = \mathbf{i} + (2p + 1)\mathbf{j}$$

Given that $\sqrt{2} |\vec{OA}| = |\vec{OB}|$ and $p > 0$

(a) find the value of p

(4)

Using this value of p

(b) find a unit vector that is parallel to \vec{AB}

(5)

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Question 3 continued

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(Total for Question 3 is 9 marks)



Question 4 continued

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Question 4 continued

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(Total for Question 4 is 7 marks)



5 The roots of the quadratic equation $2x^2 + (6 + 2p)x + 2p = 0$ are α and β

(a) Write down an expression in terms of p for

(i) $\alpha + \beta$

(ii) $\alpha\beta$

(2)

(b) Show that $(\alpha - \beta)^2 = 9 + 2p + p^2$

(4)

Given that $(\alpha - \beta) = 3$

(c) find the possible values of p

(3)

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Question 5 continued

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Question 5 continued

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(Total for Question 5 is 9 marks)



- 6 (a) Using a formula from page 2, show that $\cos 2A = 1 - 2\sin^2 A$ (2)

The finite region R is bounded by the curve with equation $y = 3 + 2\sin x$, the x -axis, the y -axis and the line with equation $x = \frac{\pi}{4}$

The region R is rotated through 360° about the x -axis.

- (b) Use calculus to find the volume of the solid generated. Give your answer to the nearest integer. (6)

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Question 6 continued

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(Total for Question 6 is 8 marks)



Question 7 continued

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Question 7 continued

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(Total for Question 7 is 11 marks)



8

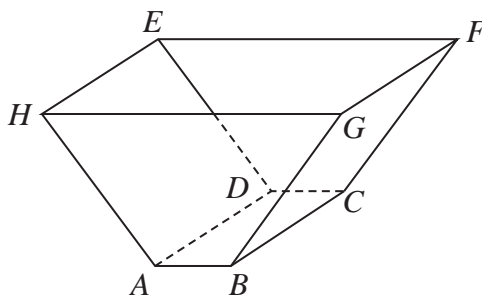


Diagram NOT accurately drawn

Figure 2

Figure 2 shows a waste paper basket in the shape of a right prism with 5 faces and a cross section that is a trapezium. The top, $EFGH$, of the waste paper basket is open.

The base of the prism $ABCD$ is a rectangle with

$$AB = DC = 2x \text{ cm and } AD = BC = h \text{ cm}$$

The cross sections $HGBA$ and $EFCD$ are such that

$$EF = HG = 8x \text{ cm and } AH = BG = CF = DE = 5x \text{ cm}$$

The top, $EFGH$, of the waste paper basket is such that

$$EH = FG = h \text{ cm}$$

The volume of the waste paper basket is 2250 cm^3

The total surface area of the 5 faces of the waste paper basket is $S \text{ cm}^2$

- (a) Show that $S = 40x^2 + \frac{1350}{x}$ (5)

Given that x can vary,

- (b) use calculus, to find, to 3 significant figures, the value of x for which S is a minimum. (5)
 Justify that this value of x gives a minimum value of S

- (c) Find, to 3 significant figures, the minimum value of S (2)

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Question 8 continued

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Question 8 continued

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(Total for Question 8 is 12 marks)



- 9 The straight line L_1 passes through the point A with coordinates $(4, 7)$ and has gradient m , where $m < 0$

Another straight line L_2 is perpendicular to L_1 and passes through the point B with coordinates $(4, k)$ where $k \neq 7$

The lines L_1 and L_2 intersect at the point C .

Given that the y coordinate of C is Y

(a) show that $Y = \frac{7 + m^2k}{m^2 + 1}$ (7)

Given that the triangle ABC is isosceles,

(b) find the value of m (5)

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Question 9 continued

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Question 9 continued

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(Total for Question 9 is 12 marks)



10 Solve the equation

$$\log_4 x + \log_{16} x + \log_2 x = 10.5$$

Show your working clearly.

(5)

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Question 10 continued

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(Total for Question 10 is 5 marks)



11 A curve C has equation

$$y = \frac{(2a-1)x+1}{ax-6} \quad \text{where } a \text{ is a constant and } x \neq \frac{6}{a}$$

(a) Find $\frac{dy}{dx}$

(3)

The curve crosses the y -axis at the point A .

The normal to C at the point A is the line l with equation $66y - 72x + 11 = 0$

Show that

(b) (i) $a = 3$

(4)

(ii) the equation of C is $y = \frac{5x+1}{3x-6}$ where $x \neq 2$

(1)

(c) Using the axes on the opposite page, sketch C , showing clearly the asymptotes with their equations and the coordinates of the points where C crosses the coordinate axes.

(5)

The line l meets C again at the point D .

(d) Find the x coordinate of D .

Give your answer as an improper fraction.

(4)

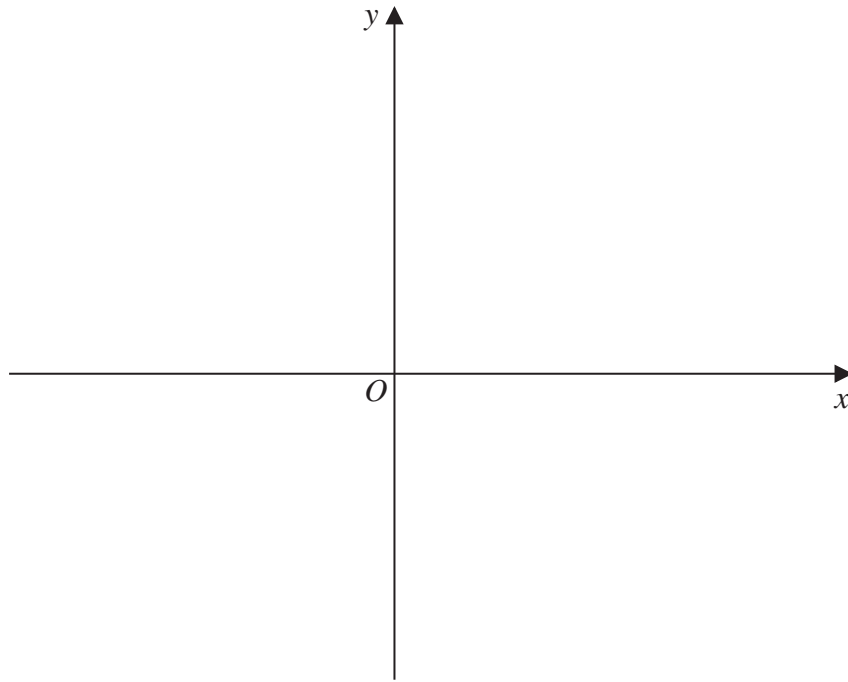
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Question 11 continued



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Question 11 continued

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Area for writing answers, consisting of multiple horizontal dotted lines.



