



Mark Scheme (Results)

Summer 2017

Pearson Edexcel International GCSE
In Mathematics A (4MA0) Paper 4HR



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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.
- **Types of mark**
 - M marks: method marks
 - A marks: accuracy marks
 - B marks: unconditional accuracy marks (independent of M marks)
- **Abbreviations**
 - cao – correct answer only
 - ft – follow through
 - isw – ignore subsequent working
 - SC - special case
 - oe – or equivalent (and appropriate)
 - dep – dependent
 - indep – independent
 - eeo – each error or omission

- **No working**

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score no marks.

- **With working**

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the “correct” answer has been obtained from incorrect working, award 0 marks.

Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks.

If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.

If there is no answer on the answer line then check the working for an obvious answer.

- **Ignoring subsequent work**

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

- **Parts of questions**

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another.

International GCSE Maths				
Apart from questions 9, 14, 17, 21b and 23 (where the mark scheme states otherwise) the correct answer, unless clearly obtained from an incorrect method, should be taken to imply a correct method.				
Q	Working	Answer	Mark	Notes
1 (a)	Eg $\frac{30}{12} \times 110$ or 2.5×110 or $\frac{30}{12}$ or 2.5 or $\frac{110}{12} \times 30$ or $9.16(666...) \times 30$ or $\frac{110}{12}$ or $9.16(666...) \text{ oe}$	275	2	M1 Accept 9.16(666...) rounded or truncated to at least 3 SF A1
(b)	Eg $\frac{375}{100} \times 12$ or 3.75×12 or $375 \div \frac{100}{12}$ or $375 \div 8.33(333...)$ or $\frac{12}{100} \times 375$ or 0.12×375	45	2	M1 For a complete method Accept 8.33(333...) rounded to at least 3 SF A1
				Total 4 marks

2	(a) (i)		5, 15	1	B1
	(ii)		5, 7, 9, 10, 11, 13, 15	1	B1
	(b)		4, 6, 8, 10, 12, 14	2	B2 B2 for all correct and none incorrect. If not B2 then B1 for 4 or more correct and no more than 1 incorrect.
					Total 4 marks

3	(a)		14.37028405	2	M1 102.66 or 1.843(9...) or 7.143(9..) A1 Accept 14.37(028.....) rounded or truncated to at least 4SF
	(b)		14.4	1	B1 ft As long as from at least 4sf
					Total 3 marks

4	$10 \times 4.2 \times 7.5$ or $315 \text{ (cm}^3\text{)}$ oe	18	4	M1	For volume of cuboid
	Eg $0.5 \times 7 \times x \times 5$ or $17.5x$ oe			M1	indep For volume of triangular prism
	$10 \times 4.2 \times 7.5 = 0.5 \times 7 \times x \times 5$ or $17.5x = 315$ oe or $\frac{10 \times 4.2 \times 7.5}{0.5 \times 7 \times 5}$ or $\frac{315}{17.5}$ oe			M1	Dep on M2 For a correct equation involving volume of cuboid and volume of prism or For a correct expression for x
				A1	18 SCB2 for For volume of cuboid = 315 and final answer = 9
				Total 4 marks	

5	(a)		$12 - 28c$	1	B1
	(b)		$y(y + 8)$	1	B1
	(c)	$x^2 - 3x + 7x - 21$	$x^2 + 4x - 21$	2	M1 For 3 correct terms or for 4 correct terms ignoring signs or for $x^2 + 4x + c$ for any non-zero value of c or for $\dots + 4x - 21$ A1 cao
	(d)	$5p - 3p = 9$ or $2p = 9$ or $-9 = 3p - 5p$ or $-9 = -2p$	4.5	2	M1 A1 oe eg $\frac{9}{2}$ or $4\frac{1}{2}$
	(e)		y^{11}	1	B1
	(f)		h^8	1	B1
	(g)		e^{15}	1	B1
					Total 9 marks

6	(a)		$30 < d \leq 40$	1	B1	Accept 30 – 40
	(b)	$5 \times 5 + 15 \times 12 + 25 \times 17 + 35 \times 20 + 45 \times 6$ or $25 + 180 + 425 + 700 + 270$ or 1600		4	M2	$f \times d$ for at least 4 products with correct mid- interval values and intention to add. If not M2 then award M1 for d used consistently for at least 4 products within interval (including end points) and intention to add or for at least 4 correct products with correct mid-interval values with no intention to add
		$\frac{25 + 180 + 425 + 700 + 270}{5 + 12 + 17 + 20 + 6} \text{ or } \left(= \frac{1600}{60} \right)$			M1	dep on M1 (ft their products) NB: accept their 60 if addition of frequencies is shown
			26.7		A1	Accept 26.6 – 26.7 inclusive Accept 27 if M3 awarded Do not accept fractions or mixed numbers, eg $\frac{80}{3}$ or $26\frac{2}{3}$
					Total 5 marks	

7	(a)	$4x \geq 27 - 13$ or $4x \geq 14$ or $-4x \leq 13 - 27$ or $-4x \leq -14$		2	M1 Accept an equation in place of an inequality or accept wrong inequality sign or accept 3.5 oe given as answer A1 oe Must be the final answer
	(b)		Correct line drawn	1	B1 For a closed circle at -1 with line that goes at least as far as 3 or for a closed circle at -1 with an arrow on a line pointing to the right
	(c)		$-2, -1, 0, 1, 2$	2	B2 B1 for list with one error or omission: e.g. $-2, -1, 0, 1, 2, 3$; $-1, 0, 1, 2$; $-2, -1, 1, 2$; $-3, -2, -1, 0, 1, 2$ SCB1 for $-3, -2, -1, 0, 1$
					Total 5 marks

8	$(x^2 =) 18^2 - 13^2 \text{ or } 324 - 169 \text{ or } 155$	12.4	3	M1	Squaring and subtracting
	$(x =) \sqrt{18^2 - 13^2} \text{ or } \sqrt{155}$			M1dep	for square rooting
				A1	Accept 12.4 – 12.46 inclusive
	Alternative Methods - Using Trigonometry Eg $\sin^{-1}\left(\frac{13}{18}\right)$ and $18\cos"46.2(382...)"$ oe or $\cos^{-1}\left(\frac{13}{18}\right)$ and $18\sin"43.7(617...)"$ oe			M2	For a complete method
				A1	Accept 12.4 – 12.46 inclusive
				Total 3 marks	

9	Eg $9x = 22.5$ or $18y = 27$ or $-18y = -27$ or $5x - (13 - 4x) = 9.5$ or $4x + 5x - 9.5 = 13$ or $5\left(\frac{13 - 2y}{4}\right) - 2y = 9.5$ or $4\left(\frac{9.5 + 2y}{5}\right) + 2y = 13$	$x = 2.5, y = 1.5$	3	M1	For a complete method to eliminate one variable (condone one arithmetic error)
	M1			Dep on M1 For substituting the other variable or starting again to eliminate the other variable	
	A1			dep on M1 NB: candidates showing no correct working score 0 marks.	
				Total 3 marks	

10	(a)		22 000 000	1	B1
	(b)		9.5×10^5	1	B1
Total 2 marks					

11	7500×0.04 or 300 or 7500×1.04 or 7800 or 7500×1.04^n ($n > 1$) Eg $7500 + \frac{4}{100} \times 7500 + \frac{4}{100} \times (7500 +$ “300”) $+ \frac{4}{100} \times (7500 + “300” + “312”)$ or $7500 + “300” + “312” + “324.48”$	8436.48	3	M1 For interest for first year or for $7500 \times 0.04 \times 3$ oe or 900 or for $7500 + 7500 \times 0.04 \times 3$ oe or an answer of 8400 M1 For a complete method	M2 for 7500×1.04^3 oe
				A1 Accept answers in the range 8436 – 8437 NB: Answer in the range 936 -937 gets M2A0	
				Total 3 marks	

12	(a)		$y = \frac{1}{2}x - 1$ oe	2	M1	For (y=) $\frac{3}{6}x + c$ (c may be any number or letter) or For (y=) $mx - 1$ where m is non-zero or for Gradient = $\frac{3}{6}$ oe or $m = \frac{3}{6}$ oe clearly stated
					A1	For a fully a correct equation for L Eg $y = \frac{3}{6}x - 1$ or $2y = x - 2$ or $y - 1 = \frac{1}{2}(x - 4)$ or $y - -2 = \frac{1}{2}(x - -2)$ M1A0 for $L = \frac{1}{2}x - 1$ or $\frac{1}{2}x - 1$
	(b)	$4 = \frac{1}{2} \times 5 + c$ or $y - 4 = \frac{1}{2}(x - 5)$	$y = \frac{1}{2}x + 1\frac{1}{2}$	2	M1ft	For correct substitution of given coordinate into their equation Follow through their gradient in (a)
					A1	oe Eg $y = \frac{1}{2}(x + 3)$ SCB1 for (l=) $\frac{1}{2}x + 1\frac{1}{2}$
Total 4 marks						

13	(Angle $ABD \Rightarrow \tan^{-1}(\frac{5}{9})$ or (Angle $ADB \Rightarrow \tan^{-1}(\frac{9}{5})$ or (Angle $ABC \Rightarrow \cos^{-1}(\frac{9}{15})$ or (Angle $ACB \Rightarrow \sin^{-1}(\frac{9}{15})$ ($BD \Rightarrow \sqrt{9^2 + 5^2}$ or ($AC \Rightarrow \sqrt{15^2 - 9^2}$ ($DC \Rightarrow \sqrt{15^2 - 9^2} - 5$	24	4	M1	For correct method to find angle ABD or ADB or ABC or ACB or for correct method to find side BD , AC or DC .
	A1			For angle $ABD = 29.(0546\dots)$ or for angle $ADB = 60.(9453\dots)$ or for angle $ABC = 53.(1301\dots)$ or for angle $ACB = 36.(8698\dots)$ or For $BD = \sqrt{106}$ or $10.(2956\dots)$ or for $AC = 12$ or for $DC = 7$ Accept rounded or truncated to at least 2SF	
	M1			For a complete method to find x or $\sin x$ or $\cos x$ Accept $0.912 \leq \cos x \leq 0.9152$ Accept $0.407 \leq \sin x \leq 0.413$	
	A1			Awrt 24	
	Eg ($x \Rightarrow \cos^{-1}(\frac{9}{15}) - \tan^{-1}(\frac{5}{9})$ or ($x \Rightarrow 180 - 90 - "29.(0546\dots)" - "36.(8698\dots)"$ or $\cos x = \frac{15^2 + "10.(2956\dots)"^2 - 7^2}{2 \times 15 \times "10.(2956\dots)"}$ or $\cos x = 0.913(009)$ or $\sin x = \frac{7 \sin "36.(8698\dots)" }{\sqrt{106}}$ or $\sin x = \frac{7 \sin "119.(054\dots)" }{15}$ or $\sin x = 0.407(940\dots)$				
					Total 4 marks

14	$\frac{6(5-x)}{2} - \frac{6(x-1)}{3} = 6 \times 1 \text{ or}$ $3(5-x) - 2(x-1) = 6 \text{ or}$ $\frac{3(5-x) - 2(x-1)}{6} (=1) \text{ or}$ $\frac{3(5-x)}{6} - \frac{2(x-1)}{6} (=1)$	2.2	4	M1	For a clear intention to multiply both sides by 6 or a multiple of 6 or to express LHS as a single fraction with denominator of 6 or a multiple of 6 or to express LHS as the sum of 2 fractions with denominator of 6 or a multiple of 6
	$15 - 3x - 2x + 2 = 6 \text{ or}$ $\frac{15 - 3x - 2x + 2}{6} = 1$ $\frac{15 - 3x}{6} - \frac{2x - 2}{6} = 1$			M1	Expanding brackets in a correct equation.
	Eg $-3x - 2x = 6 - 2 - 15$ or $-5x = -11$ or $3x + 2x = 15 + 2 - 6$ or $5x = 11$			M1	dep on both preceding marks for a correct rearrangement of a correct equation with terms in x on one side and numbers on the other.
				A1	oe Dependent on M2
				Total 4 marks	

15	(a)(i)		61°	1	B1
	(ii)		Alternate segment theorem	1	B1 Dep on B1 for (a)(i) Accept alternate segment(s) Accept angles in alternate segments are equal or Accept Angle between a chord and a tangent is equal to the angle on the circumference subtended/made by the same chord
	(b)	$180 - (180 - (61 + 53))$		2	M1 For $61 + 53$ or $180 - 66$
			114°		A1 cao
					Total 4 marks

16	(a)	$\frac{2}{6} \times \frac{1}{5}$ oe	$\frac{1}{15}$	2	M1	For a complete method
					A1	oe Eg $\frac{2}{30}$ Accept 0.066(666...) rounded or truncated to at least 3 decimal places
	(b)	$\frac{4}{6} \times \frac{3}{5}$ or 0.4 or $\frac{2}{6} \times \frac{1}{5}$ or 0.066(666...) or $\frac{1}{6} \times \frac{3}{5}$ or $\frac{3}{6} \times \frac{1}{5}$ or 0.1 or $\frac{3}{6} \times \frac{2}{5}$ or 0.2 or $\frac{2}{6} \times \frac{1}{5}$ or 0.066(666...)	$\frac{7}{15}$	3	M1	One correct product that gives an even number
		$\frac{4}{6} \times \frac{3}{5} + \frac{2}{6} \times \frac{1}{5}$ or $\frac{1}{6} \times \frac{3}{5} + \frac{3}{6} \times \frac{1}{5} + \frac{3}{6} \times \frac{2}{5} + \frac{2}{6} \times \frac{1}{5}$			M1	Sum of correct products
					A1	oe Accept 0.466(666...) rounded or truncated to at least 3 decimal places

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17	$\frac{3 \pm \sqrt{9 + 220}}{22} \text{ or } \frac{3 \pm \sqrt{9 + 220}}{2 \times 11} \text{ or}$ $\frac{3 \pm \sqrt{(-3)^2 - -220}}{2 \times 11} \text{ or } \frac{3 \pm \sqrt{(-3)^2 - -220}}{22}$ NB: denominator must be 2×11 or 22 and there must be evidence for correct order of operations in the numerator Do not accept sign error or omission of brackets		3	M2 Or for $\frac{- - 3 \pm \sqrt{(-3)^2 - 4 \times 11 \times -5}}{2 \times 11} \text{ (allow partial correct evaluation)}$ and $\frac{3 \pm \sqrt{229}}{22}$ If not M2 then M1 for $\frac{- - 3 \pm \sqrt{(-3)^2 - 4(11)(-5)}}{2 \times 11}$ Condone one sign error in substitution; Condone omission of brackets Allow partial correct evaluation
		0.82 and -0.55		A1 for awrt 0.82 and awrt -0.55 Award M2 A1 for awrt 0.82, -0.55 with sufficient correct working that would gain at least M1
	Alternative scheme			
	$11[(x - \frac{3}{22})^2 - \frac{229}{484}] \text{ oe}$			M1

	$\frac{3}{22} \pm \sqrt{\frac{229}{484}}$ oe			M1
		0.82 and -0.55		A1 for awrt 0.82 and awrt -0.55 Award M2 A1 for awrt 0.82, -0.55 with sufficient correct working that would gain at least M1
				Total 3 marks

18	$480 = k \times 5^2$ or $480 \propto k \times 5^2$ oe or or $(k =) \frac{480}{5^2}$ or $(k =) 19.2$ oe $k \propto \frac{480}{5^2}$ or $k \propto 19.2$ oe		3	M1
	"19.2" $\times 1.5^2$			M1 Dep on M1 or for $A = 19.2x^2$ oe
		43.2		A1 oe
				Total 3 marks

19	(a)	Frequency densities: 1.2, 2.8, 1.6, 0.4, 0.2	A fully correct histogram	3	M1	For 3 or more correctly calculated freq densities or For a correct scale indicated or 1 small square = 1 (person) 1 big square = 25 (people)
					M1	For at least 2 additional correct bars (with or without scale) Implies first M1
					A1	All 4 additional bars correct
	(b)	$\frac{100}{150} \times 240 + 100$ or $1.6 \times 100 + 100$ or “160” + 100 oe or $600 - (120 + 140 + \frac{1}{3} \times 240)$ or $600 - (120 + 140 + 50 \times 1.6)$ or $600 - 340$ oe	260	2	M1	A fully complete method to find the number of people who took from 200 to 300 minutes + 100
					A1	
					Total 5 marks	

20	(a)		-5	1	B1
	(b)		23	1	B1
	(c)	$(f(-7)) = \frac{1}{-7+5}$ or $(f(-7)) = -\frac{1}{2}$ or $2\left(\frac{1}{-7+5}\right) + 3$ or $2 \times -\frac{1}{2} + 3$		2	M1
			2		A1
	(d)	$x-3=2y$ or $\frac{x}{2}=y+\frac{3}{2}$ or $y-3=2x$ or $\frac{y}{2}=x+\frac{3}{2}$ or $\frac{y-3}{2}$ or $\frac{y}{2}-\frac{3}{2}$		2	M1
			$\frac{x-3}{2}$		A1 oe Eg $\frac{x}{2}-\frac{3}{2}$
					Total 6 marks

21	(a) (i)		$3\mathbf{b} - 6\mathbf{a}$	1	B1 Oe Need not be simplified Mark the final answer
	(ii)		$2\mathbf{b} - 4\mathbf{a}$	1	B1ft oe eg $\frac{2}{3}(3\mathbf{b} - 6\mathbf{a})$ Need not be simplified Mark the final answer
	(iii)		$6\mathbf{b} - 3\mathbf{a}$	1	B1 oe Need not be simplified Mark the final answer
	(b)	Eg $\overrightarrow{XY} = 2\mathbf{b} - \mathbf{a}$ oe or $\overrightarrow{YB} = 4\mathbf{b} - 2\mathbf{a}$	shown	2	M1 Work out $\overrightarrow{XY}$ or $\overrightarrow{YX}$ or $\overrightarrow{YB}$ or $\overrightarrow{BY}$ A1 Dep on M1 Correct conclusion from correct simplified vectors Eg $\overrightarrow{XB} = 3\overrightarrow{XY}$ or $\overrightarrow{YB} = 2\overrightarrow{XY}$ or $\overrightarrow{XB} = 1.5\overrightarrow{YB}$ or XB and XY are parallel or YB and XY are parallel or XB and YB are parallel
					Total 5 marks

22			4	B1	Identifying correct triangle
	$\sqrt{8^2 + 15^2}$ or $\sqrt{289}$ or 17			M1	Complete method to find MG
	Eg $\tan 24 = \frac{BG}{\sqrt{8^2 + 15^2}}$ or $\tan 24 = \frac{BG}{17}$ or $\frac{BG}{\sin 24} = \frac{\sqrt{8^2 + 15^2}}{\sin(90 - 24)}$ or $\frac{BG}{\sin 24} = \frac{17}{\sin 66}$ ($BG =$) $17 \tan 24$ or ($BG =$) $\frac{17}{\sin 66} \times \sin 24$			M1	Dep For a correct equation involving BG or a correct expression for BG Implies B1
		7.57		A1	Accept 7.56 – 7.57
				Total 4 marks	

23	27.25 or 27.35 or 17.5 or 18.5 or 9.805 or 9.815		3	B1	Accept 27.349 or 27.3499... or 18.49 or 18.499... or 9.8149 or 9.81499...
	$(t =) \frac{27.25 - 18.5}{9.815}$			M1	For $\frac{LB - UB_1}{UB_2}$ oe where $27.25 \leq LB < 27.3$ and $18 < UB_1 \leq 18.5$ and $9.81 < UB_2 \leq 9.815$
		0.891		A1	dep on seeing $\frac{27.25 - 18.5}{9.815}$ Correct working must be seen Accept 0.891 - 0.8915
				Total 3 marks	

24	Eg $12.6^2 = 10.4^2 + 18^2 - 2 \times 10.4 \times 18 \times \cos L$ or $158.76 = 108.16 + 324 - 374.4 \cos L$ Note: $\cos K = \frac{-57.08}{262.08} (= -0.217(796\dots))$ and $K = 102.(579\dots)$ $\cos M = \frac{374.6}{453.6} (= 0.825(837\dots))$ and $M = 34.3(264\dots)$		5	M1 Correct substitution into cosine rule to find L or For $\cos K = \frac{10.4^2 + 12.6^2 - 18^2}{2 \times 10.4 \times 12.6}$ oe AND $\sin L = \frac{12.6 \sin "102.(579\dots)"}{18}$ or For $\cos M = \frac{18^2 + 12.6^2 - 10.4^2}{2 \times 18 \times 12.6}$ oe AND $\sin L = \frac{12.6 \sin "34.3(264\dots)"}{10.4}$
	Eg $\cos L = \frac{10.4^2 + 18^2 - 12.6^2}{2 \times 10.4 \times 18}$ or $\cos L = \frac{273.4}{374.4}$ or $\cos L = 0.73(0235\dots)$ oe or $L = 43.0(938\dots)$			A1 Rearranging cosine rule correctly. Accept $L = 43^\circ$ Accept $43.0(938\dots)$ rounded or truncated to at least 3 SF
	(Area of sector =) $\frac{"43.0(938\dots)"}{360} \times \pi \times 10.4^2$ or $40.6(752\dots)$			M1 Dep on at least M1 Accept $40.5 - 40.7$
				B1 For (area of triangle =) $63.9(471\dots)$ Accept $63.8 - 64.0$
		23.3		A1 Accept $23.2 - 23.3$
				Total 5 marks

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