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Mark Scheme (Results)

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Pearson Edexcel International GCSE
Mathematics A (4PM0)
Paper 02

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.

- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.

- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.

- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.

- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.

  Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.

- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.

- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.

- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

- **Types of mark**
  - M marks: method marks
  - A marks: accuracy marks
  - B marks: unconditional accuracy marks (independent of M marks)

- **Abbreviations**
  - cao – correct answer only
  - ft – follow through
  - isw – ignore subsequent working
  - SC - special case
  - oe – or equivalent (and appropriate)
  - dep – dependent
  - indep – independent
  - eeoo – each error or omission

- **No working**

  If no working is shown then correct answers normally score full marks

  If no working is shown then incorrect (even though nearly correct) answers score

  no marks.

- **With working**

  If there is a wrong answer indicated always check the working in the body of the script and award any marks appropriate from the mark scheme.

  If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

Any case of suspected misread loses two A (or B) marks on that part, but can gain the M marks. Mark all work on follow through but enter A0 (or B0) for the first two A or B marks gained.

If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If there are multiple attempts shown, then all attempts should be marked and the highest score on a single attempt should be awarded.

- **Follow through marks**

Follow through marks which involve a single stage calculation can be awarded without working since you can check the answer yourself, but if ambiguous do not award.

Follow through marks which involve more than one stage of calculation can only be awarded on sight of the relevant working, even if it appears obvious that there is only one way you could get the answer given.

- **Ignoring subsequent work**

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially shows that the candidate did not understand the demand of the question.

- **Linear equations**

Full marks can be gained if the solution alone is given, or otherwise unambiguously indicated in working (without contradiction elsewhere). Where the correct solution only is shown substituted, but not identified as the solution, the accuracy mark is lost but any method marks can be awarded.

- **Parts of questions**

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another

General Principles for Further Pure Mathematics Marking
(but note that specific mark schemes may sometimes override these general principles)

Method mark for solving a 3 term quadratic equation:

1. <u>Factorisation</u>:

$$\left(x^2 + bx + c\right) = \left(x + p\right)\left(x + q\right), \text{ where } |pq| = |c| \quad \text{leading to } x = ...$$

$$\left(ax^2 + bx + c\right) = \left(mx + p\right)\left(nx + q\right) \text{ where } |pq| = |c| \text{ and } |mn| = |a| \quad \text{leading to } x = ...$$

2. <u>Formula</u>:
Attempt to use the **correct** formula (shown explicitly or implied by working) with values for a, b and c, leading to $x = ...$

3. <u>Completing the square</u>:

$$x^2 + bx + c = 0: \ \left(x \pm \tfrac{b}{2}\right)^2 \pm q \pm c = 0, \quad q \neq 0 \qquad \text{leading to } x = ...$$

Method marks for differentiation and integration:

1. <u>Differentiation</u>
    Power of at least one term decreased by 1. $\left(x^n \rightarrow x^{n-1}\right)$

2. <u>Integration</u>:
    Power of at least one term increased by 1. $\left(x^n \rightarrow x^{n+1}\right)$

Use of a formula:

Generally, the method mark is gained by **either**

> quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values

> **or**, where the formula is <u>not</u> quoted, the method mark can be gained by implication from the substitution of <u>correct</u> values and then proceeding to a solution.

Answers without working:

The rubric states "Without sufficient working, correct answers <u>may</u> be awarded no marks".

General policy is that if it could be done "in your head" detailed working would not be required. (Mark schemes may override this eg in a case of "prove or show...."

Exact answers:

When a question demands an exact answer, all the working must also be exact. Once a candidate loses exactness by resorting to decimals the exactness cannot be regained.

Rounding answers (where accuracy is specified in the question)

Penalise only once per question for failing to round as instructed - ie giving more digits in the answers. Answers with fewer digits are automatically incorrect, but the isw rule may allow the mark to be awarded before the final answer is given.
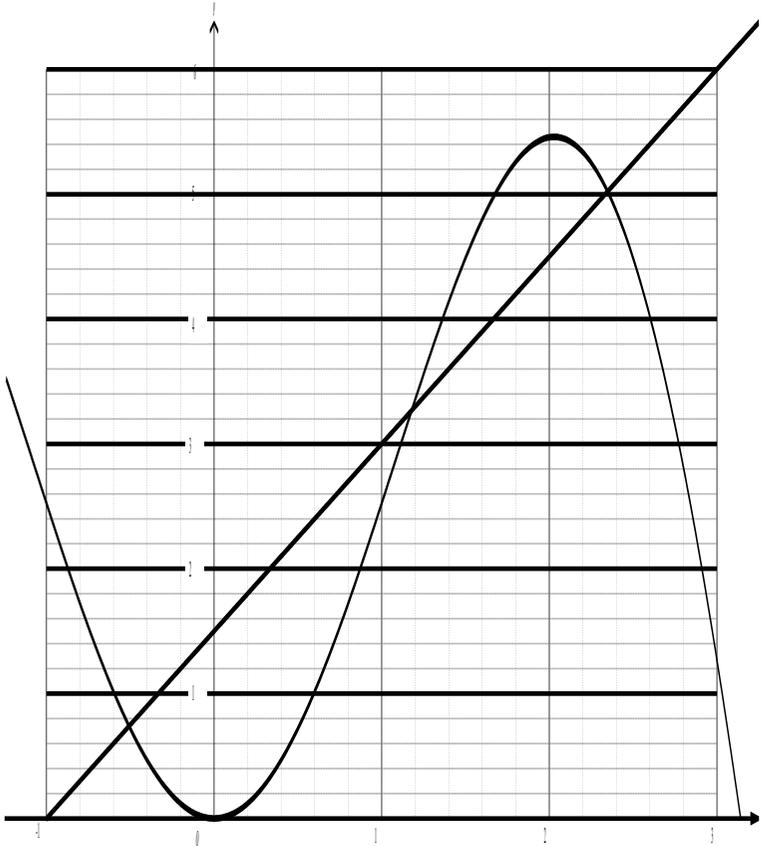
Question	Working	Mark	Notes	
1. (a)	$\dfrac{x}{\sin C} = \dfrac{2x}{\sin 100°}$ $\sin C = \dfrac{\sin 100°}{2}$ $C = 29.5°$ $\angle BAC = 180° - 100° - 29.5° = 50.5°$	4	M1 M1 A1 A1	dep cao ft
(b)	$\frac{1}{2} x \times 2x \sin 50.5° = 16$ $x = \sqrt{\dfrac{16}{\sin 50.5°}} = \sqrt{20.735} = 4.55$	3	M1 M1 A1	dep cao
			Total 7 Marks	

Question		Working	Mark	Notes
2.	(a)	$S = 2\pi r \dfrac{V}{\pi r^2} + 2\pi r^2, = \dfrac{2V}{r} + 2\pi r^2$ ✱	2	M1 A1 cso
	(b)	$\dfrac{\mathrm{d}S}{\mathrm{d}r} = -\dfrac{2V}{r^2} + 4\pi r$ or $-\dfrac{3200}{r^2} + 4\pi r$	7	M1
		For S$_{\min}$: $-\dfrac{2V}{r^2} + 4\pi r = 0$ or $-\dfrac{3200}{r^2} + 4\pi r = 0$		M1 dep
		$\dfrac{2V}{r^2} = 4\pi r \Rightarrow r^3 = \dfrac{V}{2\pi}$ or $\dfrac{3200}{r^2} = 4\pi r \Rightarrow r^3 = \dfrac{800}{\pi}$		
		$r = \sqrt[3]{\dfrac{800}{\pi}}$ $(= 6.338...)$		A1 oe
		$S = \dfrac{2 \times 1600}{6.338...} + 2\pi \times 6.338...^2 = 757$		M1 A1 cao
		$\dfrac{\mathrm{d}^2 S}{\mathrm{d}r^2} = \dfrac{4V}{r^3} + 4\pi$ or $\dfrac{6400}{r^3} + 4\pi > 0$ (for $r > 0$) $\Rightarrow$ minimum		M1 A1 ft *or* consider gradient either side of SV (numerical values must be shown).
				Total 9 Marks

Question		Working	Mark	Notes
3.	(a)	$3^2 - 4 \times 2 \times c = 0$	2	M1
		$c = \dfrac{9}{8},\ 1\dfrac{1}{8}$ or 1.125		A1 cao
	(b)	$x = \dfrac{-3 \pm 0}{2 \times 2}$ or $\left(2x + \tfrac{3}{2}\right)\left(x + \tfrac{3}{4}\right) = 0$ *or* $\left(4x + 3\right)^2 = 0$	2	M1 oe
		$x = -\dfrac{3}{4}$ or -0.75		A1
				Total 4 Marks

Question		Working	Mark	Notes
4.	(a)	$\dfrac{\sqrt{2}}{2}$ or $\dfrac{1}{\sqrt{2}}$	1	B1 oe
	(b)	$\sin(45^\circ + \theta) = \sin 45^\circ \cos\theta + \cos 45^\circ \sin\theta$ $= \dfrac{\sqrt{2}}{2}\dfrac{\sqrt{3}}{2\sqrt{2}} + \dfrac{\sqrt{2}}{2}\dfrac{\sqrt{5}}{2\sqrt{2}},\ \ = \dfrac{\sqrt{3}}{4} + \dfrac{\sqrt{5}}{4}\ = \dfrac{\sqrt{3} + \sqrt{5}}{4}$ ✱	2	 M1 A1
	(c)	$\cos(45^\circ + 30^\circ) = \cos 45^\circ \cos\theta - \sin 45^\circ \sin\theta$ $= \dfrac{\sqrt{2}}{2}\dfrac{\sqrt{3}}{2\sqrt{2}} - \dfrac{\sqrt{2}}{2}\dfrac{\sqrt{5}}{2\sqrt{2}},\ \ = \dfrac{\sqrt{3}}{4} - \dfrac{\sqrt{5}}{4}\ = \dfrac{\sqrt{3} - \sqrt{5}}{4}$	2	 M1 A1
	(d)	$\sin(45^\circ + \theta)\cos(45^\circ + \theta) = \left(\dfrac{\sqrt{3} + \sqrt{5}}{4}\right)\left(\dfrac{\sqrt{3} - \sqrt{5}}{4}\right) = \dfrac{3 - 5}{16}$ $= \dfrac{-2}{16} = -\dfrac{1}{8}$ ✱	2	M1 A1
				Total 7 Marks

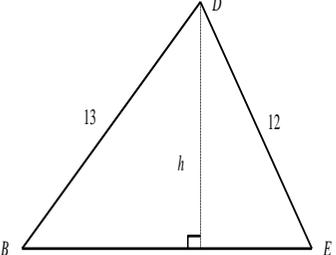| Question	Working	Mark	Notes
5. (a)	$x\sin x = 1 \Rightarrow 3x\sin x = 3$ $x = 1.1$ and $x = 2.8$	3	M1 A1 A1
(b)	$2x\sin x - x = 1 \Rightarrow 2x\sin x = x+1 \Rightarrow 3x\sin x = \frac{3}{2}(x+1)$ $x = -0.5$, $x = 1.2$, $x = 2.3$ (allow 2.4)	5	M1 A1 M1 dep A1 A1
			Total 8 Marks

Question		Working	Mark	Notes
6.	(a)(i)	$\alpha\beta = -\frac{3}{2}$	4	B1
	(a)(ii)	$\left(\alpha + \frac{1}{\beta}\right)\left(\beta + \frac{1}{\alpha}\right)$		
		$= \alpha\beta + 2 + \frac{1}{\alpha\beta}$ $\;or\;$ $\frac{(\alpha\beta+1)^2}{\alpha\beta}$ $\;or\;$ $\frac{-\frac{1}{2}}{\beta} \times \frac{-\frac{1}{2}}{\alpha}$		M1
		$= -\frac{3}{2} + 2 - \frac{2}{3}$ $\;or\;$ $\frac{(-\frac{1}{2})^2}{-\frac{3}{2}}$		M1 dep
		$= -\frac{1}{6}$		A1 cao
	(b)(i)	$\alpha + \beta = -\frac{p}{2}$	4	B1
	(b)(ii)	$\left(\alpha + \frac{1}{\beta}\right) + \left(\beta + \frac{1}{\alpha}\right)$		
		$= (\alpha + \beta) + \frac{\alpha + \beta}{\alpha\beta}$ $\;or\;$ $\frac{(\alpha + \beta)(\alpha\beta + 1)}{\alpha\beta}$ $\;or\;$ $-\frac{1}{2}\left(\frac{\alpha + \beta}{\alpha\beta}\right)$		M1
		$= -\frac{p}{2} + \frac{-\frac{p}{2}}{-\frac{3}{2}}$ $\;or\;$ $\frac{-\frac{p}{2}(-\frac{3}{2}+1)}{-\frac{3}{2}}$ $\;or\;$ $-\frac{1}{2}\left(\frac{-\frac{p}{2}}{-\frac{3}{2}}\right)$		M1
		$= -\frac{p}{6}$		A1
	(c)	$-\frac{p}{6} = 2\left(-\frac{1}{6}\right) \Rightarrow p = 2$	1	B1 ft
	(d)	$x^2 - \left(-\frac{2}{6}\right)x + \left(-\frac{1}{6}\right) = 0$	2	M1
		$\Rightarrow 6x^2 + 2x - 1 = 0$		A1 cao
				Total 11 Marks

Question		Working	Mark	Notes
7.	(a)	$t_{15} = -14 + (15-1)4 = -14 + 56 = 42$	2	M1 A1
	(b)	$S_{25} = \frac{25}{2}\left(2 \times -14 + (25-1)4\right)$ $= \frac{25}{2}(-28 + 96) = \frac{25}{2} \times 68 = 850$	3	M1 A1 A1 cao

| (c) | If first of 9 terms is a then the last term is a + 8 × 4
or sum is $\frac{9}{2}(2a+(9-1)4)$

$\Rightarrow \frac{9}{2}(a+a+32)=1422$
$\Rightarrow 2a+32=316 \Rightarrow a=142$

OR

$S_{r+8}-S_{r-1} \quad (=1422)$
$\frac{r+8}{2}(-28+4(r+7))-\frac{r-1}{2}(-28+4(r-2)) \quad (=1422)$
$(r+8)(4r)-(r-1)(4r-36)=2844$
$4r^2+32r-4r^2+36r+4r-36=2844$

$72r=2880 \Rightarrow r=40$

$t_{40}=-14+39\times4=142$

OR

$S_{r+9}-S_r \quad (=1422)$
$\frac{r+9}{2}(-28+4(r+8))-\frac{r}{2}(-28+4(r-1)) \quad (=1422)$
$(r+9)(4r+4)-(r)(4r-32)=2844$
$4r^2+36r+4r+36-4r^2+32r=2844$

$72r=2808 \Rightarrow r=39$

$t_{39+1}=-14+39\times4=142$

OR | 5 | M1

M1 A1
M1 A1   cao

OR

M1   Either of the required sums

M1

A1

M1 A1

OR

M1   Either of the required sums

M1

A1

M1 A1

OR |

7.	(c)	**OR**		**OR**
		$A+(A+d)+\cdots(A+8d)=1422$	M1	
		$9A+\frac{1}{2}(d+8d)8=1422$	M1 A1	M1 for equation in A and d
				A1 for a correct equation with a single term in A
		$9A+144=1422 \Rightarrow 9A=1278$	M1	
		$A=142$	A1	
				Total 10 Marks

Question	Working	Mark	Notes
8. (a)	$(1-2x)^5 = 1+5(-2x)+10(-2x)^2+10(-2x)^3+5(-2x)^4+(-2x)^5$ $\text{OR} = 1+5(-2x)+\frac{5.4}{2!}(-2x)^2+\frac{5.4.3}{3!}(-2x)^3+\frac{5.4.3.2}{4!}(-2x)^4+(-2x)^5$ $= 1-10x+40x^2-80x^3+80x^4-32x^5$	3	M1 A1 A1 A1 for 3 correct terms A2 for all terms correct
(b)	$(1+2x)^{-5} = 1+\frac{-5}{1}(2x)+\frac{-5\times-6}{1\times2}(2x)^2+\frac{-5\times-6\times-7}{1\times2\times3}(2x)^3\cdots$ $= 1-10x+60x^2-280x^3\cdots$	3	M1 A1 A1
(c)	Valid when $\lvert2x\rvert<1 \Rightarrow \lvert x\rvert<\frac{1}{2}$ or $-\frac{1}{2}<x<\frac{1}{2}$	1	B1
(d)	$\left(\dfrac{1-2x}{1+2x}\right)^5 = (1-10x+40x^2\cdots)(1-10x+60x^2\cdots)$ $= 1-10x+60x^2-10x+100x^2+40x^2\cdots$ $= 1-20x+200x^2\cdots$	3	M1 M1 A1 cao
(e)	$\dfrac{dy}{dx} = -20+400x\cdots$ when $x=0$, gradient $=-20$	2	M1 A1 cso
			Total 12 Marks

Question		Working	Mark	Notes
9.	(a)	$DE^2 = 13^2 - 5^2, \Rightarrow DE = 12$ $BE^2 = 10^2 - 5^2$ or $BE = 10\sin 60°$ or $10\cos 30°$ or $5\tan 60°$ $BE = \sqrt{75}$ (cm) or $BE = 5\sqrt{3}$ (cm)	4	M1 A1 M1 A1 oe
	(b)	$(5\sqrt{3})^2 = 13^2 + 12^2 - 2\times 13\times 12\cos BDE$ $\cos BDE = \dfrac{13^2 + 12^2 - (5\sqrt{3})^2}{2\times 13\times 12}\ \left(=\dfrac{238}{312}\right)$ $\angle BDE = 40.3°$	3	M1 oe, ft A1 cao A1
	(c)	$\dfrac{5\sqrt{3}}{\sin 40.3°} = \dfrac{12}{\sin DBE}$ or $12^2 = 13^2 + 75 - 2\times 13\times \sqrt{75}\cos B$ $\sin DBE = \dfrac{12\sin 40.3°}{5\sqrt{3}}\ (=0.8960)\ or\ \cos B = \dfrac{100}{26\sqrt{75}}\ (=0.4441)$ $\angle DBE = 63.6°$	3	M1 A1 ft A1 cao
	(d)	$\angle DEB = 180° - 40.3° - 63.6°$ $\angle DEB = 76.1°$	2	M1 or complete method using sin or cos rule A1 cao
	(e)	$h = 13\sin 63.6°$ or $h = 12\sin 76.1° = 11.648$ base area $= \frac{1}{2}\times 10^2 \times \sin 60° = 25\sqrt{3}\ (=43.30)$ $V = \frac{1}{3}\times 25\sqrt{3}\times 11.648 = 168\ \left(\text{cm}^3\right)$	3	M1 M1 A1 cao
				Total 15 Marks

Question		Working	Mark	Notes
10.	(a)	$\dfrac{dy}{dx} = 27x^2 - 36x - 8$ At P (0, 24), gradient $= -8$ Equation of PQ is $y = -8x + 24$	4	M1 A1 M1 dep A1 cao
	(b)	At Q, $9x^3 - 18x^2 - 8x + 24 = -8x + 24$ $\Rightarrow 9x^3 - 18x^2 = 0$ $\Rightarrow 9x^2(x-2) = 0$ $\Rightarrow x = 2$ ($x = 0$ at P) $y = 9 \times 2^3 - 18 \times 2^2 - 8 \times 2 + 24 = 8$ so Q (2, 8)	5	M1 A1 M1 A1 A1
	(c)	Since $PQRS$ is a parallelogram, RS is parallel to QP so gradient of RS is -8 $\Rightarrow 27x^2 - 36x - 8 = -8$ $\Rightarrow 9x(3x - 4) = 0$ $\Rightarrow x = \frac{4}{3}$ ($x = 0$ at P) $y = 9\left(\frac{4}{3}\right)^3 - 18\left(\frac{4}{3}\right)^2 - 8\left(\frac{4}{3}\right) + 24 = \frac{8}{3}$ so $R\left(\frac{4}{3}, \frac{8}{3}\right)$	4	 M1 M1 A1 A1
	(d)	x coord $= \frac{4}{3} + (0 - 2)$ y coord $= \frac{8}{3} + (24 - 16)$ $S\left(-\frac{2}{3}, 18\frac{2}{3}\right)$	2	M1 A1 cao
	(e)	If $x = -\frac{2}{3}$, $y = 9\left(\frac{-2}{3}\right)^3 - 18\left(\frac{-2}{3}\right)^2 - 8\left(\frac{-2}{3}\right) + 24$ $= -\frac{8}{3} - 8 + \frac{16}{3} + 24 = \frac{8}{3} + 16 = 18\frac{2}{3}$ $\Rightarrow S\left(-\frac{2}{3}, 18\frac{2}{3}\right)$ lies on C.	2	 M1 A1 cso
				Total 17 Marks