

Please check the examination details below before entering your candidate information

Candidate surname	Other names
Pearson Edexcel	Centre Number
International GCSE	Candidate Number
Monday 20 January 2020	
Morning (Time: 2 hours)	Paper Reference 4PM1/02R
Further Pure Mathematics Paper 2R	
	
Calculators may be used.	Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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International GCSE in Further Pure Mathematics Formulae sheet

MensurationSurface area of sphere = $4\pi r^2$ Curved surface area of cone = $\pi r \times$ slant heightVolume of sphere = $\frac{4}{3}\pi r^3$ **Series****Arithmetic series**Sum to n terms, $S_n = \frac{n}{2}[2a + (n-1)d]$ **Geometric series**Sum to n terms, $S_n = \frac{a(1-r^n)}{(1-r)}$ Sum to infinity, $S_\infty = \frac{a}{1-r}$ $|r| < 1$ **Binomial series** $(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots$ for $|x| < 1, n \in \mathbb{Q}$ **Calculus****Quotient rule (differentiation)**

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry**Cosine rule**In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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2

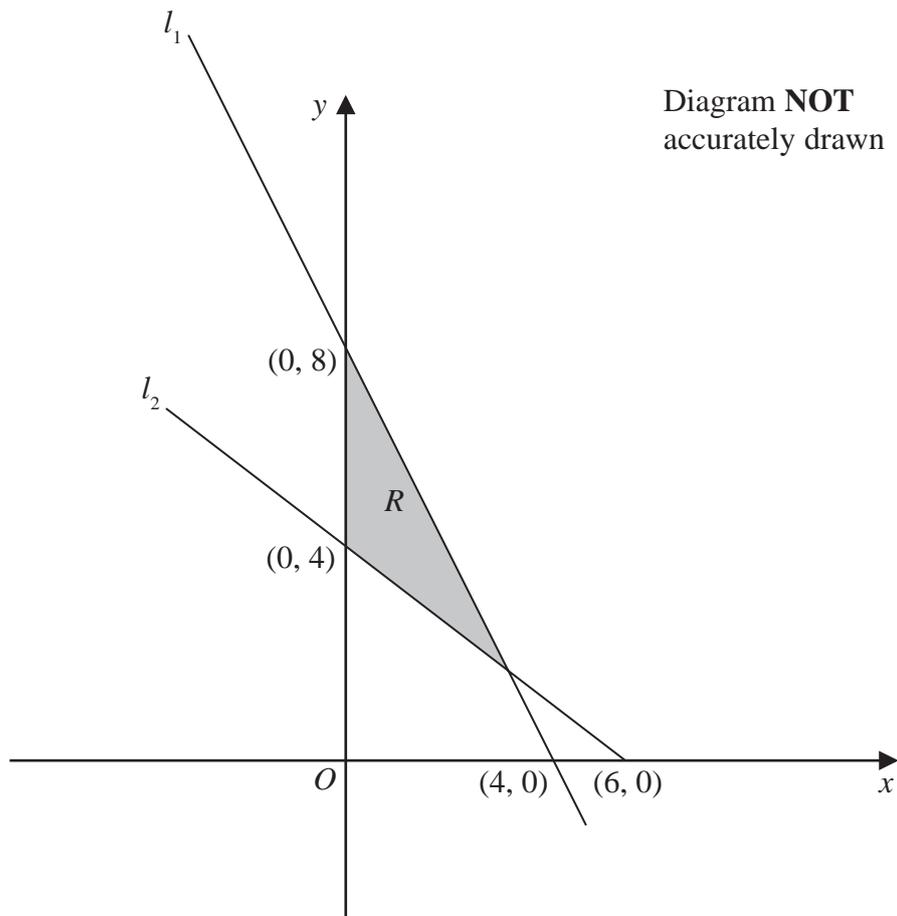


Figure 2

Figure 2 shows the shaded region R bounded by the line l_1 , the line l_2 and the y -axis.

The points with coordinates $(0, 8)$ and $(4, 0)$ lie on l_1

The points with coordinates $(0, 4)$ and $(6, 0)$ lie on l_2

(a) Find, in the form $ax + by = c$, where a , b and c integers, an equation of

(i) l_1

(ii) l_2

(3)

(b) Hence write down three inequalities that define the region R .

(3)

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Question 2 continued

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A large rectangular area with horizontal dotted lines for writing.

(Total for Question 2 is 6 marks)



3 In triangle ABC , $AB = 11$ cm and $BC = 12$ cm.

The area of triangle $ABC = 33$ cm²

Find, in cm to 3 significant figures, the two possible lengths of AC .

(5)

Handwriting practice area consisting of 20 horizontal dotted lines.

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Question 3 continued

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(Total for Question 3 is 5 marks)



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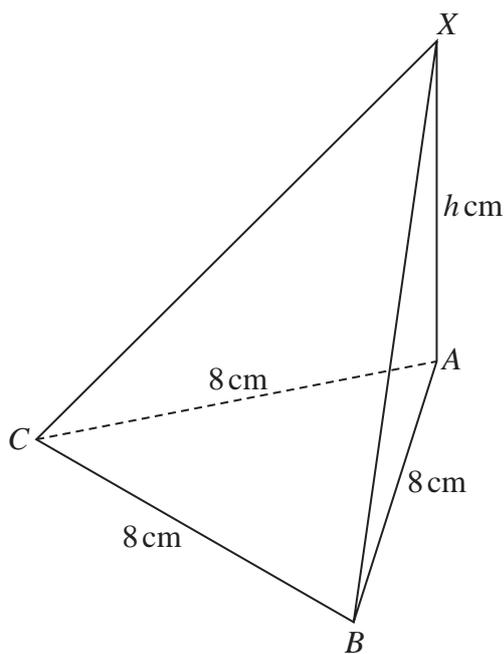


Diagram **NOT** accurately drawn

Figure 3

Figure 3 shows a triangular pyramid $ABCX$.
 The base ABC of the pyramid is an equilateral triangle where $AB = BC = CA = 8$ cm.
 The vertex X of the pyramid is such that AX is perpendicular to the base of the pyramid and $AX = h$ cm.

The volume of the pyramid is $48\sqrt{3}$ cm³

- (a) Show that $h = 9$ (3)
- (b) Find, in degrees to one decimal place, the size of angle BXC . (3)
- (c) Find, in degrees to one decimal place, the size of the angle between the plane BCX and the base ABC of the pyramid. (3)

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Question 4 continued

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A large rectangular area with rounded corners, containing numerous horizontal dotted lines for writing.



Question 4 continued

A large rectangular area with a rounded border, containing 25 horizontal dotted lines for writing.

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Question 4 continued

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(Total for Question 4 is 9 marks)



Question 5 continued

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A large rectangular area with rounded corners, containing numerous horizontal dotted lines for writing.



Question 5 continued

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A large rectangular area with horizontal dotted lines for writing.

(Total for Question 5 is 12 marks)



Question 6 continued

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A large rectangular area with rounded corners, containing numerous horizontal dotted lines for writing.



Question 6 continued

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Area with horizontal dotted lines for writing.

(Total for Question 6 is 6 marks)



Question 7 continued

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Area for writing answers, consisting of multiple horizontal dotted lines.



Question 7 continued

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Area with horizontal dotted lines for writing.

(Total for Question 7 is 13 marks)



Question 8 continued

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A large rectangular area with horizontal dotted lines for writing, intended for the answer to Question 8.



Question 8 continued

A large rectangular area with a rounded border, containing 25 horizontal dotted lines for writing.

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Question 8 continued

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Area with horizontal dotted lines for writing answers.

(Total for Question 8 is 10 marks)



Question 9 continued

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A large rectangular area with horizontal dotted lines for writing.



Question 9 continued

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Area with horizontal dotted lines for writing answers.

(Total for Question 9 is 10 marks)



Question 10 continued

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Question 10 continued

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Area with horizontal dotted lines for writing.

(Total for Question 10 is 12 marks)



Question 11 continued

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Area for writing answers, consisting of multiple horizontal dotted lines.



Question 11 continued

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A large rectangular area with horizontal dotted lines for writing, intended for the answer to Question 11.



