

Please check the examination details below before entering your candidate information

Candidate surname	Other names
Pearson Edexcel	Centre Number
International GCSE	Candidate Number
Monday 15 June 2020	
Afternoon (Time: 2 hours)	Paper Reference 4PM1/01R
Further Pure Mathematics	
Paper 1R	
	
Calculators may be used.	Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain **NO** credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

International GCSE in Further Pure Mathematics Formulae sheet

MensurationSurface area of sphere = $4\pi r^2$ Curved surface area of cone = $\pi r \times$ slant heightVolume of sphere = $\frac{4}{3}\pi r^3$ **Series****Arithmetic series**Sum to n terms, $S_n = \frac{n}{2}[2a + (n-1)d]$ **Geometric series**Sum to n terms, $S_n = \frac{a(1-r^n)}{(1-r)}$ Sum to infinity, $S_\infty = \frac{a}{1-r}$ $|r| < 1$ **Binomial series** $(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots$ for $|x| < 1, n \in \mathbb{Q}$ **Calculus****Quotient rule (differentiation)**

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry**Cosine rule**In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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Answer all TWELVE questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1 Here is a formula

$$P = 3 + 2 \sin \left(\frac{3\pi t}{8} \right) \quad 0 \leq t \leq 12$$

(a) Find the exact value of P when $t = \frac{10}{3}$ (2)

(b) Find

(i) the largest value of P

(ii) the smallest value of P (2)

(c) Find the least value of t for which $P = 4$ (3)

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Question 1 continued

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(Total for Question 1 is 7 marks)



Question 2 continued

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Question 2 continued

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Question 2 continued

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(Total for Question 2 is 11 marks)



3 The n th term of an arithmetic series is u_n such that

$$u_n = \ln a + (n - 1) \ln b$$

where a and b are positive integers.

Given that $u_2 = \ln 12$ and that $u_5 = \ln 768$

find the value of a and the value of b .

(7)

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Question 3 continued

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(Total for Question 3 is 7 marks)



Question 4 continued

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(Total for Question 4 is 6 marks)



Question 5 continued

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(Total for Question 5 is 8 marks)



Question 6 continued

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Question 6 continued

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(Total for Question 6 is 7 marks)



Question 7 continued

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Question 7 continued

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(Total for Question 7 is 9 marks)



Question 8 continued

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Question 8 continued

Area for writing answers, consisting of multiple horizontal dotted lines.

(Total for Question 8 is 7 marks)



9 Showing your working clearly, use algebra to solve the equations

$$\frac{16^x}{8^y} = \frac{1}{4}$$

$$4^{x-2y} = 16$$

(7)

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Question 9 continued

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(Total for Question 9 is 7 marks)



Question 10 continued

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Question 10 continued

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(Total for Question 10 is 11 marks)



11

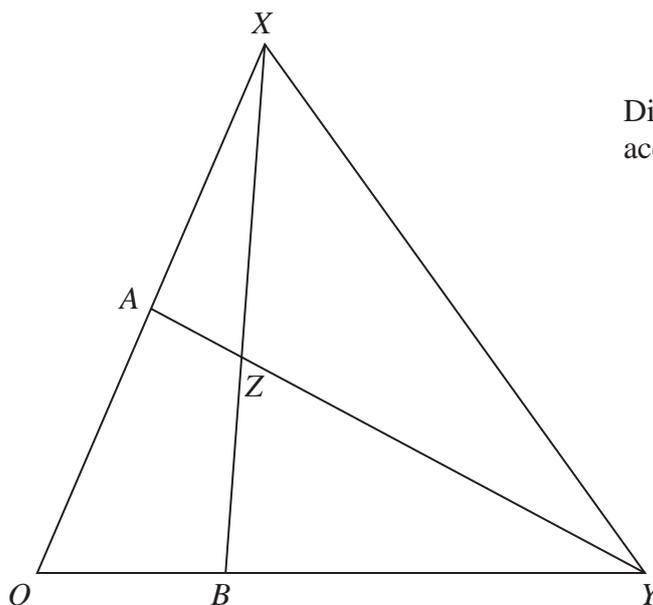


Diagram NOT accurately drawn

Figure 1

Figure 1 shows a triangle OXY

$$\vec{OX} = 2\mathbf{a} \text{ and } \vec{OY} = 3\mathbf{b}$$

A is the midpoint of OX and B is the point on OY such that $OB : BY = 1 : 2$
The lines XB and AY intersect at Z .

(a) Find \vec{AB} as a simplified expression in terms of \mathbf{a} and \mathbf{b} (1)

(b) Using a vector method, find \vec{OZ} as a simplified expression in terms of \mathbf{a} and \mathbf{b} (9)

The point M on XY is such that O, Z and M are collinear.

(c) Find \vec{OM} as a simplified expression in terms of \mathbf{a} and \mathbf{b} (3)

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Question 11 continued

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12

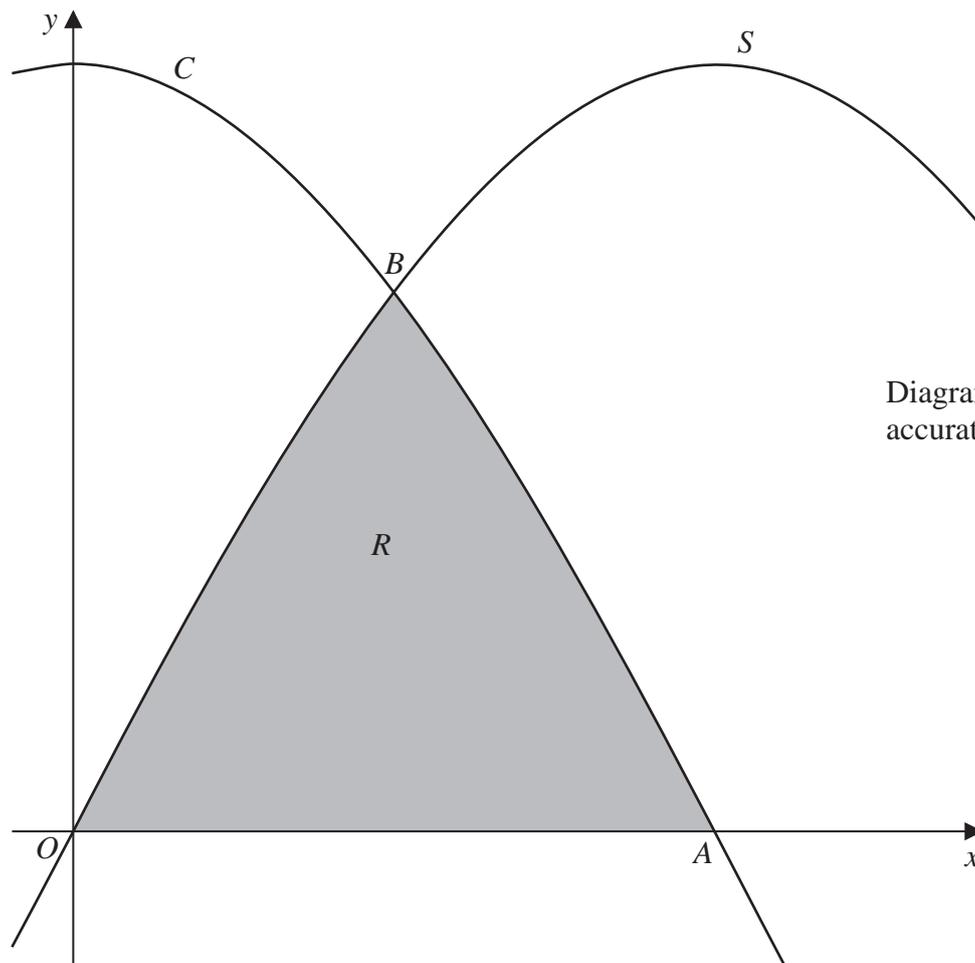


Diagram **NOT** accurately drawn

Figure 2

The region R , shown shaded in Figure 2, is bounded by the x -axis, the curve S with equation $y = 2\sin x$ and the curve C with equation $y = 2\cos x$. As shown in Figure 2, C crosses the x -axis at the point A .

(a) Write down the x coordinate of A . (1)

As shown in Figure 2, C and S intersect at the point B .

(b) Find the x coordinate of B . (2)

(c) Using calculus, find the area of the shaded region R .
Give your answer in the form $a - \sqrt{b}$ where a and b are integers. (4)

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Question 12 continued

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