

Please check the examination details below before entering your candidate information

Candidatesurname	Other names
<b>Pearson Edexcel International GCSE</b>	Centre Number <input style="width: 20px; height: 20px;" type="text"/> <input style="width: 20px; height: 20px;" type="text"/> <input style="width: 20px; height: 20px;" type="text"/> <input style="width: 20px; height: 20px;" type="text"/>
Time 2 hours	Candidate Number <input style="width: 20px; height: 20px;" type="text"/> <input style="width: 20px; height: 20px;" type="text"/> <input style="width: 20px; height: 20px;" type="text"/>
	<b>Paper reference</b> <span style="font-size: 2em; font-weight: bold;">4PM1/01</span>
<b>Further Pure Mathematics PAPER 1</b>	
	
<b>Calculators may be used.</b>	Total Marks   

### Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided – *there may be more space than you need.*
- You must **NOT** write anything on the formulae page. Anything you write on the formulae page will gain NO credit.

### Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets – *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.
- Good luck with your examination.

Turn over ►

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## International GCSE in Further Pure Mathematics Formulae sheet

**Mensuration**Surface area of sphere =  $4\pi r^2$ Curved surface area of cone =  $\pi r \times$  slant heightVolume of sphere =  $\frac{4}{3}\pi r^3$ **Series****Arithmetic series**Sum to  $n$  terms,  $S_n = \frac{n}{2}[2a + (n-1)d]$ **Geometric series**Sum to  $n$  terms,  $S_n = \frac{a(1-r^n)}{(1-r)}$ Sum to infinity,  $S_\infty = \frac{a}{1-r}$   $|r| < 1$ **Binomial series** $(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots$  for  $|x| < 1, n \in \mathbb{Q}$ **Calculus****Quotient rule (differentiation)**

$$\frac{d}{dx} \left( \frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

**Trigonometry****Cosine rule**In triangle  $ABC$ :  $a^2 = b^2 + c^2 - 2bc \cos A$ 

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

**Logarithms**

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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**Question 2 continued**

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**(Total for Question 2 is 6 marks)**





**Question 3 continued**

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**Question 3 continued**

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**(Total for Question 3 is 10 marks)**



4 The  $n$ th term of an arithmetic series is  $u_n$  where

$$u_n = (n + 1) \ln 4$$

Given that the sum of the first  $n$  terms of the series is  $S_n$

show that  $S_n = \ln 2^{(n^2 + an)}$  where  $a$  is an integer whose value is to be found.

(5)

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**Question 4 continued**

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**(Total for Question 4 is 5 marks)**





**Question 5 continued**

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**(Total for Question 5 is 10 marks)**





**Question 6 continued**

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**Question 6 continued**

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**(Total for Question 6 is 10 marks)**





**Question 7 continued**

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**Question 7 continued**

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**(Total for Question 7 is 11 marks)**





**Question 8 continued**

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**Question 8 continued**

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**(Total for Question 8 is 8 marks)**



9 Find an equation of the normal to the curve with equation

$$y = (x^3 - 2x)e^{(1-x)}$$

at the point on the curve with coordinates  $(1, -1)$

(5)

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**Question 9 continued**

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**(Total for Question 9 is 5 marks)**





**Question 10 continued**

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**Question 10 continued**

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**(Total for Question 10 is 14 marks)**



11 (a) Using a formula from page 2, show that  $\cos 2x = 1 - 2 \sin^2 x$  (3)

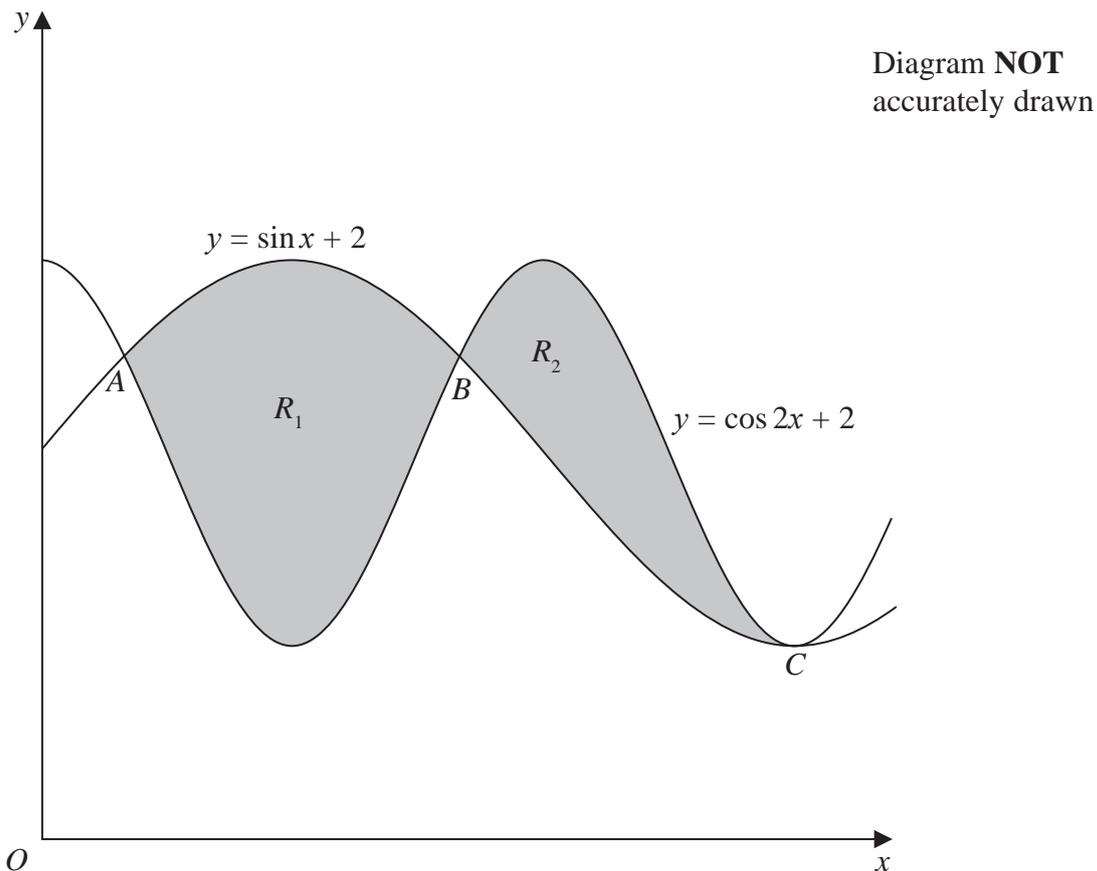


Figure 2

Figure 2 shows a sketch of part of the curves with equations  $y = \sin x + 2$  and  $y = \cos 2x + 2$

The points  $A$ ,  $B$  and  $C$ , shown in Figure 2, are three points that are common to both curves.

(b) Find the coordinates of each of these points. (4)

$R_1$  and  $R_2$ , shown shaded in Figure 2, are two regions enclosed by the two curves.

(c) Use calculus to find, in its simplest form, the ratio (8)

area of  $R_1$  : area of  $R_2$

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**Question 11 continued**

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**Question 11 continued**

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