

Please check the examination details below before entering your candidate information

Candidate surname	Other names
Centre Number	Candidate Number
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Pearson Edexcel International GCSE

Time 2 hours	<table border="1" style="border-collapse: collapse;"> <tr> <td style="padding: 2px 5px;">Paper reference</td> <td style="padding: 5px;">4PM1/02R</td> </tr> </table>	Paper reference	4PM1/02R
Paper reference	4PM1/02R		
<div style="display: flex; justify-content: space-between; align-items: center;"> <div style="text-align: center;"> <h2 style="margin: 0;">Further Pure Mathematics</h2> <h3 style="margin: 0;">PAPER 2R</h3> </div> <div style="text-align: right;">  </div> </div>			
Calculators may be used.	Total Marks		

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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International GCSE in Further Pure Mathematics Formulae sheet

Mensuration

$$\text{Surface area of sphere} = 4\pi r^2$$

$$\text{Curved surface area of cone} = \pi r \times \text{slant height}$$

$$\text{Volume of sphere} = \frac{4}{3}\pi r^3$$

Series**Arithmetic series**

$$\text{Sum to } n \text{ terms, } S_n = \frac{n}{2}[2a + (n-1)d]$$

Geometric series

$$\text{Sum to } n \text{ terms, } S_n = \frac{a(1-r^n)}{(1-r)}$$

$$\text{Sum to infinity, } S_\infty = \frac{a}{1-r} \quad |r| < 1$$

Binomial series

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$$

Calculus**Quotient rule (differentiation)**

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry**Cosine rule**

$$\text{In triangle } ABC: a^2 = b^2 + c^2 - 2bc \cos A$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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Answer all ELEVEN questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1 (a) Expand $\left(1 + \frac{x}{4}\right)^8$ in ascending powers of x up to and including the term in x^3

Give each coefficient in its simplest terms.

(3)

(b) Use your expansion with a suitable value of x to obtain an approximation, to 4 decimal places, of $(1.035)^8$

(3)

Dotted lines for working.

(Total for Question 1 is 6 marks)



Question 2 continued

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(Total for Question 2 is 6 marks)



Question 3 continued

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(Total for Question 3 is 8 marks)



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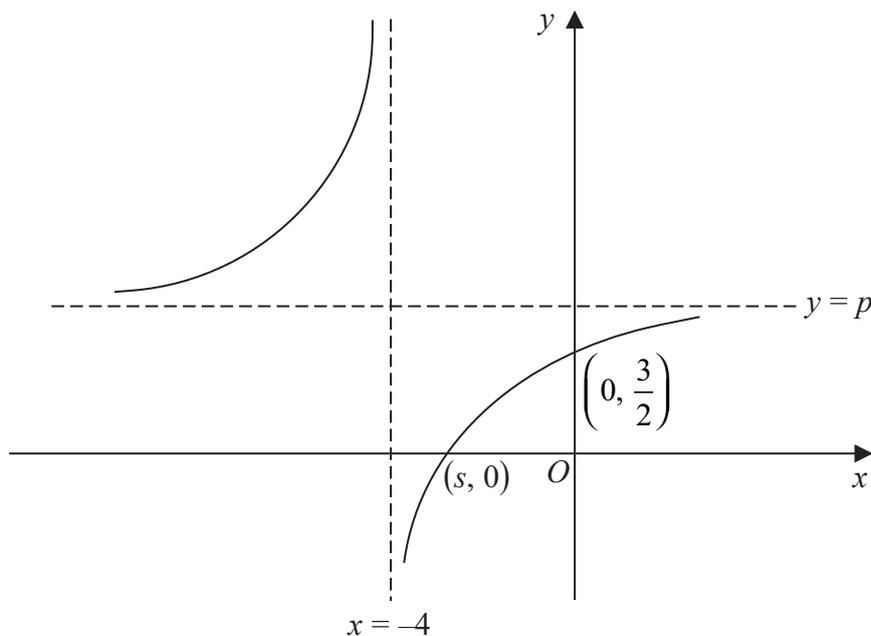


Diagram NOT accurately drawn

Figure 1

Figure 1 shows part of the curve C with equation

$$y = \frac{2x + q}{x + r} \quad x \neq -r$$

where q and r are integers.

The asymptote to C that is parallel to the y -axis has equation $x = -4$

The asymptote to C that is parallel to the x -axis has equation $y = p$

(a) Write down

(i) the value of p

(ii) the value of r

(2)

Given that C crosses the y -axis at the point with coordinates $(0, \frac{3}{2})$

(b) find the value of q

(2)

Given that C crosses the x -axis at the point with coordinates $(s, 0)$

(c) find the value of s

(2)

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Question 4 continued

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(Total for Question 4 is 6 marks)



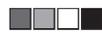
Question 5 continued

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Question 5 continued

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(Total for Question 5 is 11 marks)



Question 6 continued

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(Total for Question 6 is 6 marks)



Question 7 continued

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Question 7 continued

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(Total for Question 7 is 8 marks)



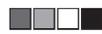
Question 8 continued

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Question 8 continued

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(Total for Question 8 is 14 marks)



Question 9 continued

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Question 9 continued

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(Total for Question 9 is 12 marks)



Question 10 continued

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Question 10 continued

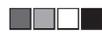
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(Total for Question 10 is 13 marks)



11

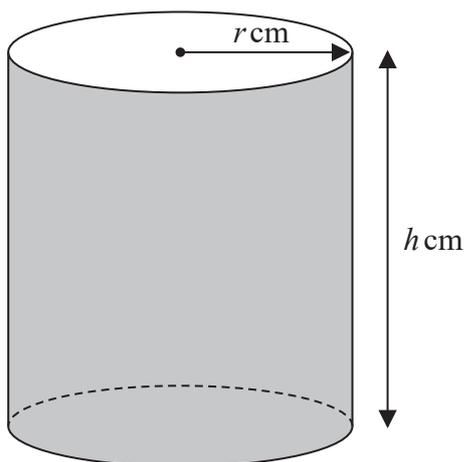


Diagram **NOT** accurately drawn

Figure 4

Figure 4 shows an open container in the shape of a cylinder with radius r cm and height h cm.

Given that the total surface area of the container is 625π cm²

(a) show that

$$h = \frac{625 - r^2}{2r} \tag{3}$$

The volume of the container is V cm³

Given that r can vary,

(b) use calculus to find the value, to 3 significant figures, of r for which V is a maximum.

Justify that this value of r gives a maximum value of V (6)

(c) For the value of r found in part (b), find the corresponding value, to 3 significant figures, of h (1)

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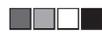
Question 11 continued

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Question 11 continued

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