

Please check the examination details below before entering your candidate information

Candidate surname	Other names
Centre Number	Candidate Number
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Pearson Edexcel International GCSE

Friday 26 May 2023

Afternoon (Time: 2 hours)	Paper reference	4PM1/01R
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Further Pure Mathematics

PAPER 1R



Calculators may be used.	Total Marks
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Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

International GCSE in Further Pure Mathematics Formulae sheet

Mensuration

Surface area of sphere $= 4\pi r^2$

Curved surface area of cone $= \pi r \times \text{slant height}$

Volume of sphere $= \frac{4}{3}\pi r^3$

Series**Arithmetic series**

Sum to n terms, $S_n = \frac{n}{2}[2a + (n-1)d]$

Geometric series

Sum to n terms, $S_n = \frac{a(1-r^n)}{(1-r)}$

Sum to infinity, $S_\infty = \frac{a}{1-r} \quad |r| < 1$

Binomial series

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$$

Calculus**Quotient rule (differentiation)**

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry**Cosine rule**

In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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Question 2 continued

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(Total for Question 2 is 8 marks)



Question 3 continued

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(Total for Question 3 is 9 marks)

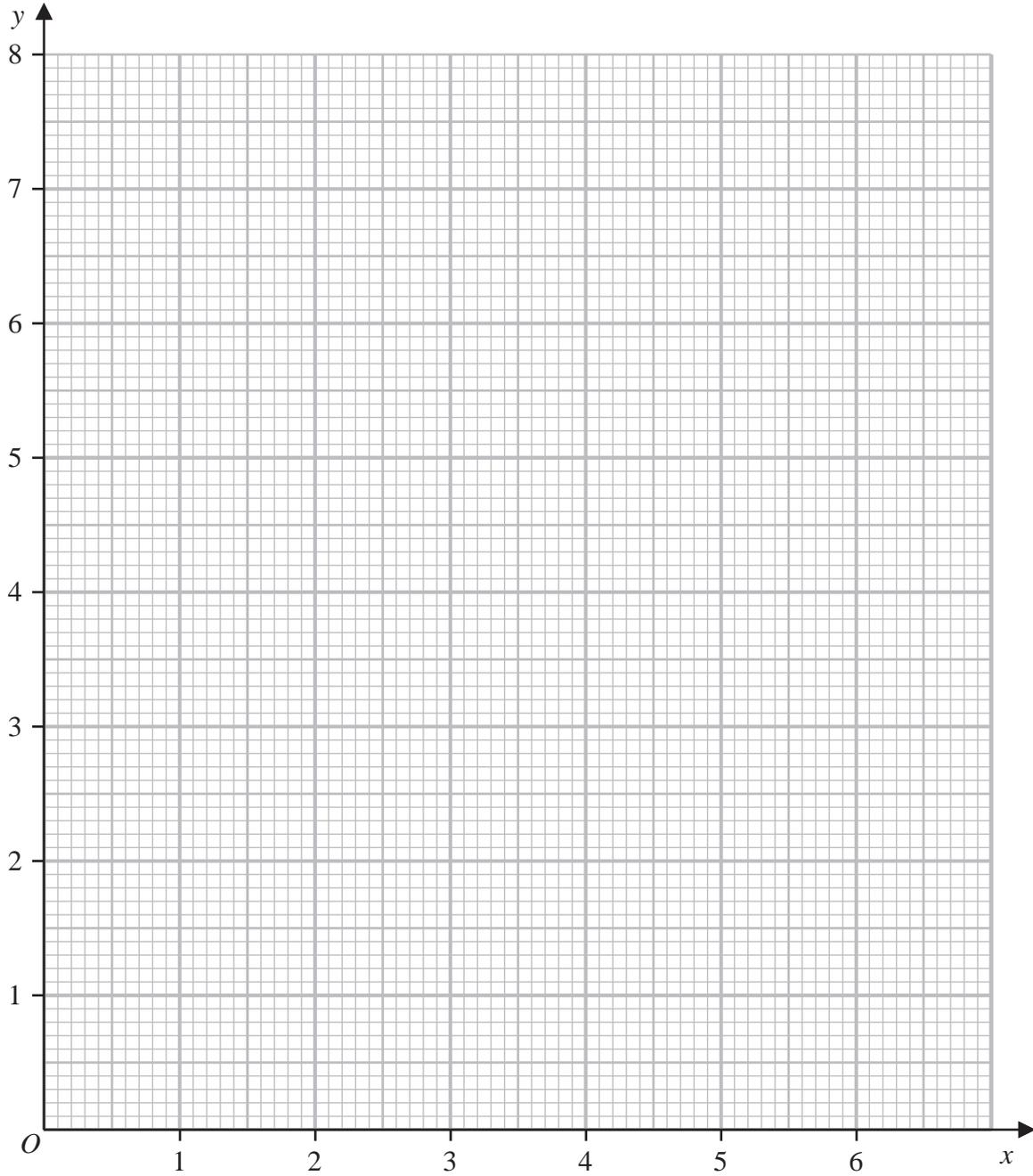


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Question 4 continued



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Turn over for a spare grid if you need to redraw your graph.



Question 4 continued

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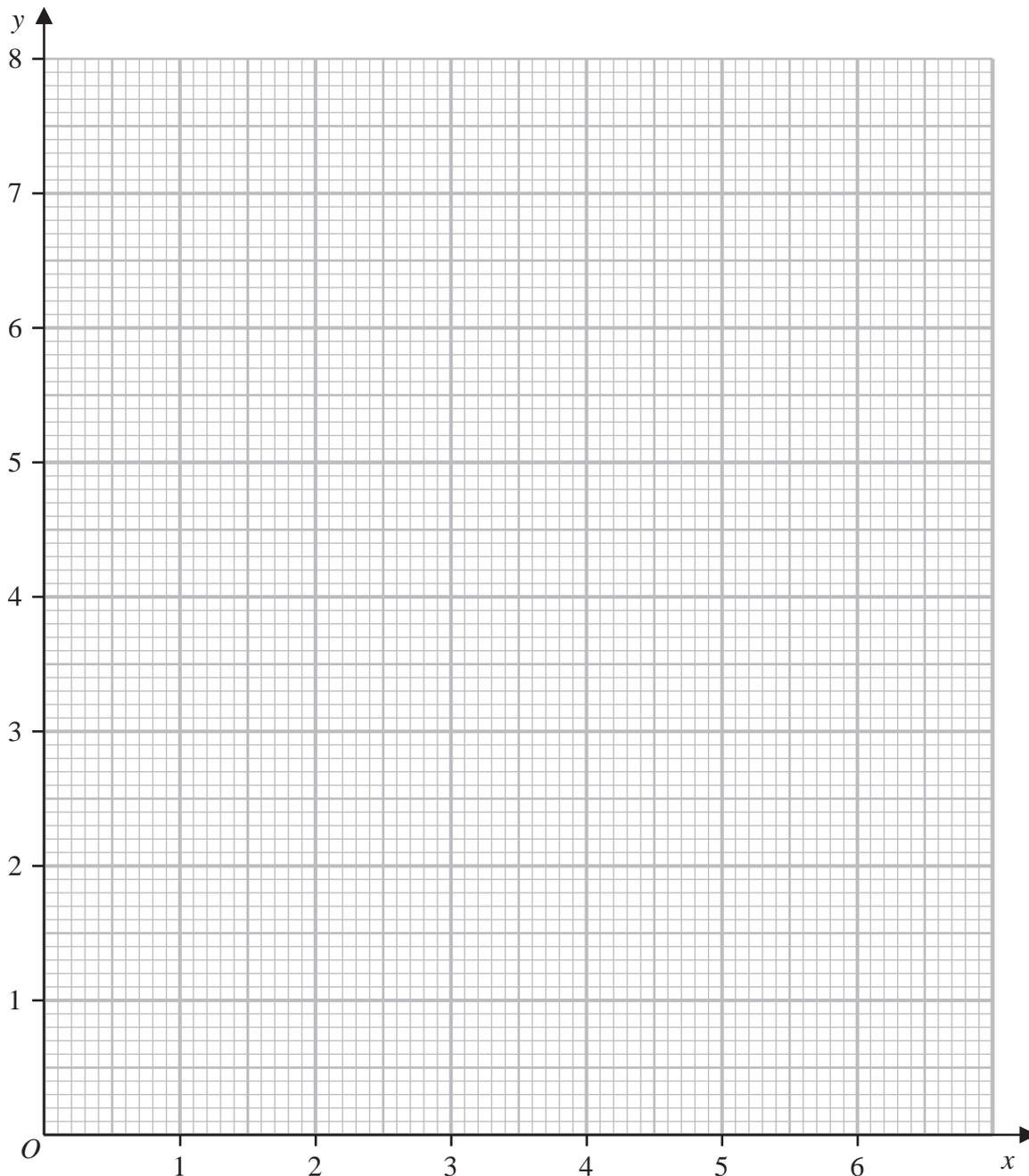
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Question 4 continued

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(Total for Question 4 is 9 marks)



5 $f(x) = 2x^3 + ax^2 - 14x + b$ where a and b are constants.

When $f(x)$ is divided by $(x - 4)$ the remainder is 39

Given that $(x - 1)$ is a factor of $f(x)$

(a) show that $a = -3$ and find the value of b (5)

(b) Hence factorise $f(x)$ completely. (4)

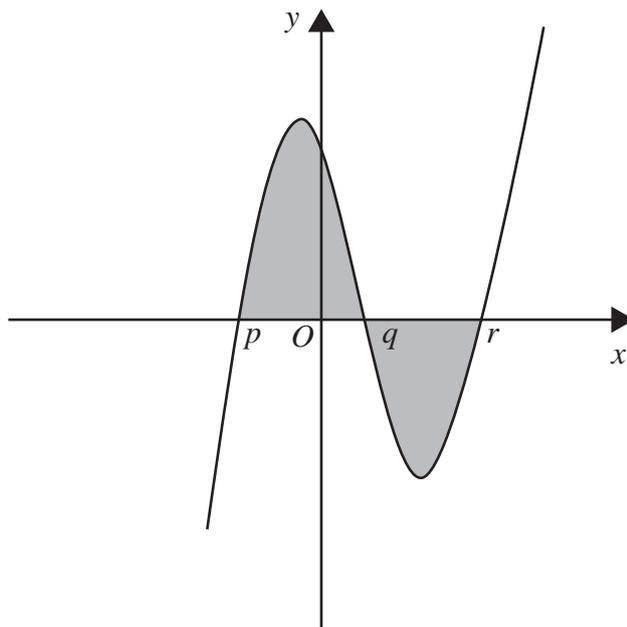


Diagram NOT accurately drawn

Figure 3

Figure 3 shows part of the curve C with equation $y = f(x)$

Given that C crosses the x -axis at the points with coordinates $(p, 0)$, $(q, 0)$ and $(r, 0)$

(c) write down the value of p , the value of q and the value of r (3)

The region shown shaded in Figure 3 is bounded by the curve and the x -axis.

(d) Use algebraic integration to find the exact area of the shaded region. (4)

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Question 5 continued

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Question 5 continued

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(Total for Question 5 is 16 marks)



Question 6 continued

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Question 6 continued

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(Total for Question 6 is 11 marks)



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Question 7 continued

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(Total for Question 7 is 8 marks)



Question 8 continued

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Question 8 continued

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Handwriting practice area consisting of 25 horizontal dotted lines for writing answers.

(Total for Question 8 is 10 marks)



Question 9 continued

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Question 9 continued

Handwriting practice area consisting of 25 horizontal dotted lines for writing answers.

(Total for Question 9 is 14 marks)



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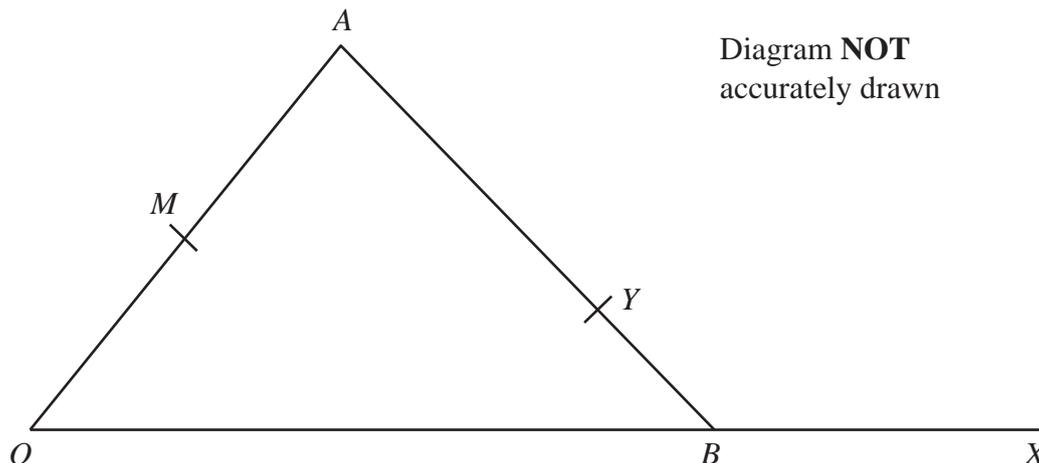


Figure 5

In Figure 5, $\vec{OA} = 2\mathbf{a}$, $\vec{OB} = 4\mathbf{b}$ and M is the midpoint of OA .

The point Y lies on AB such that $AY : YB = 3 : 1$

The point X lies on OB produced.

(a) Find as simplified expressions in terms of \mathbf{a} and \mathbf{b}

- (i) \vec{AB} (ii) \vec{MY} (3)

The points M , Y and X are collinear.

(b) Find the ratio $OB : OX$ (5)

(c) Find the ratio of (Area ΔYBX) : (Area ΔOAX) (3)

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Question 10 continued

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