

Please check the examination details below before entering your candidate information

Candidate surname	Other names
Centre Number	Candidate Number
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Pearson Edexcel International GCSE

Thursday 8 June 2023

Morning (Time: 2 hours)	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="padding: 5px; font-weight: bold; font-size: 0.8em;">Paper reference</td> <td style="padding: 5px; font-weight: bold; font-size: 1.5em;">4PM1/02</td> </tr> </table>	Paper reference	4PM1/02
Paper reference	4PM1/02		

Further Pure Mathematics

PAPER 2



Calculators may be used.	Total Marks
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**Instructions**

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.  
Anything you write on the formulae page will gain NO credit.

**Information**

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

**Advice**

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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## International GCSE in Further Pure Mathematics Formulae sheet

**Mensuration**

$$\text{Surface area of sphere} = 4\pi r^2$$

$$\text{Curved surface area of cone} = \pi r \times \text{slant height}$$

$$\text{Volume of sphere} = \frac{4}{3}\pi r^3$$

**Series****Arithmetic series**

$$\text{Sum to } n \text{ terms, } S_n = \frac{n}{2}[2a + (n-1)d]$$

**Geometric series**

$$\text{Sum to } n \text{ terms, } S_n = \frac{a(1-r^n)}{(1-r)}$$

$$\text{Sum to infinity, } S_\infty = \frac{a}{1-r} \quad |r| < 1$$

**Binomial series**

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$$

**Calculus****Quotient rule (differentiation)**

$$\frac{d}{dx} \left( \frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

**Trigonometry****Cosine rule**

$$\text{In triangle } ABC: a^2 = b^2 + c^2 - 2bc \cos A$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

**Logarithms**

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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**Question 2 continued**

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A large rectangular area with horizontal dotted lines for writing answers.

**(Total for Question 2 is 6 marks)**





**Question 3 continued**

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Area for writing answers, consisting of multiple horizontal dotted lines.

**(Total for Question 3 is 6 marks)**





**Question 4 continued**

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A large rectangular area with rounded corners, containing numerous horizontal dotted lines for writing.





**Question 4 continued**

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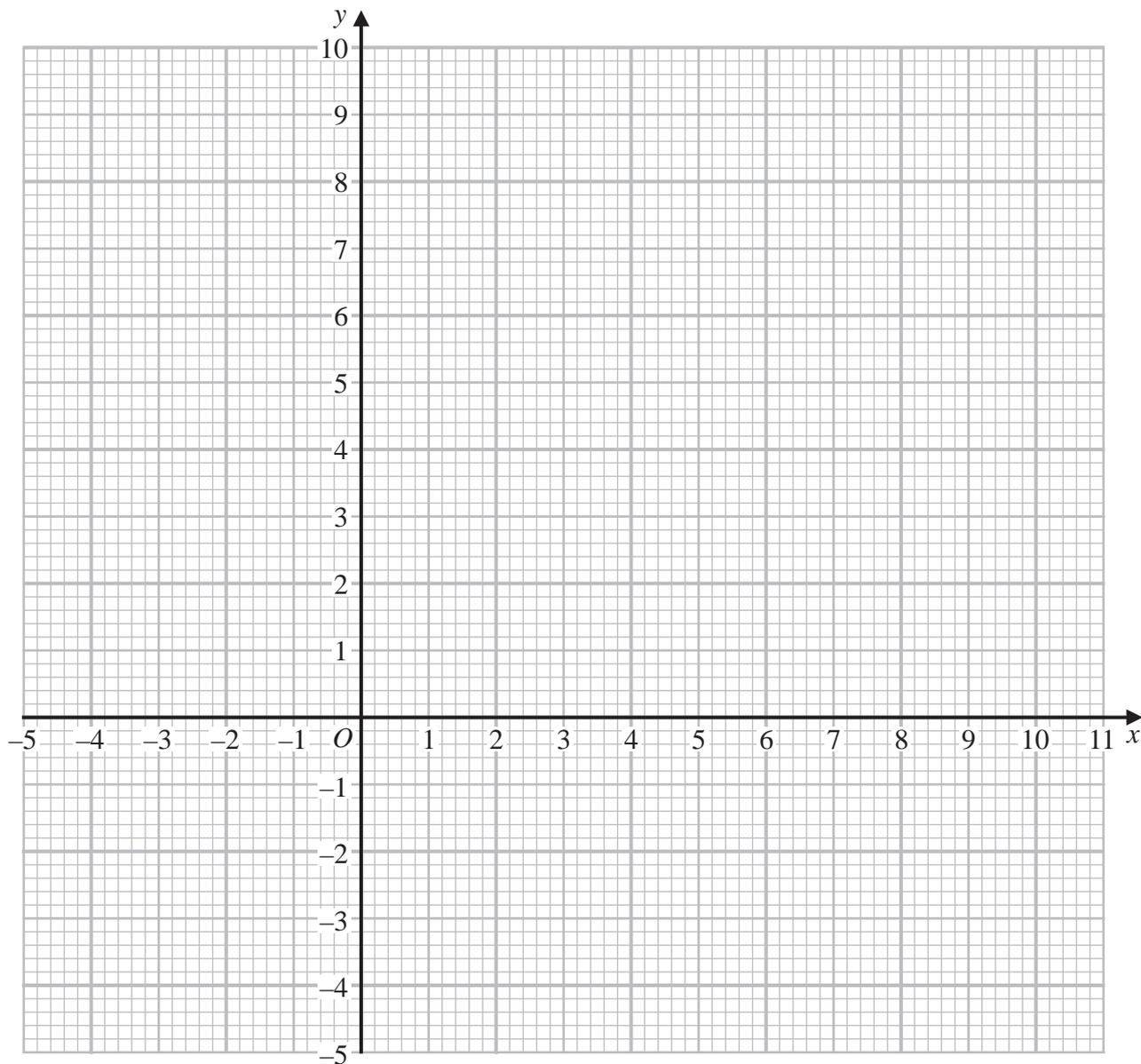
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**(Total for Question 4 is 8 marks)**





**Question 5 continued**



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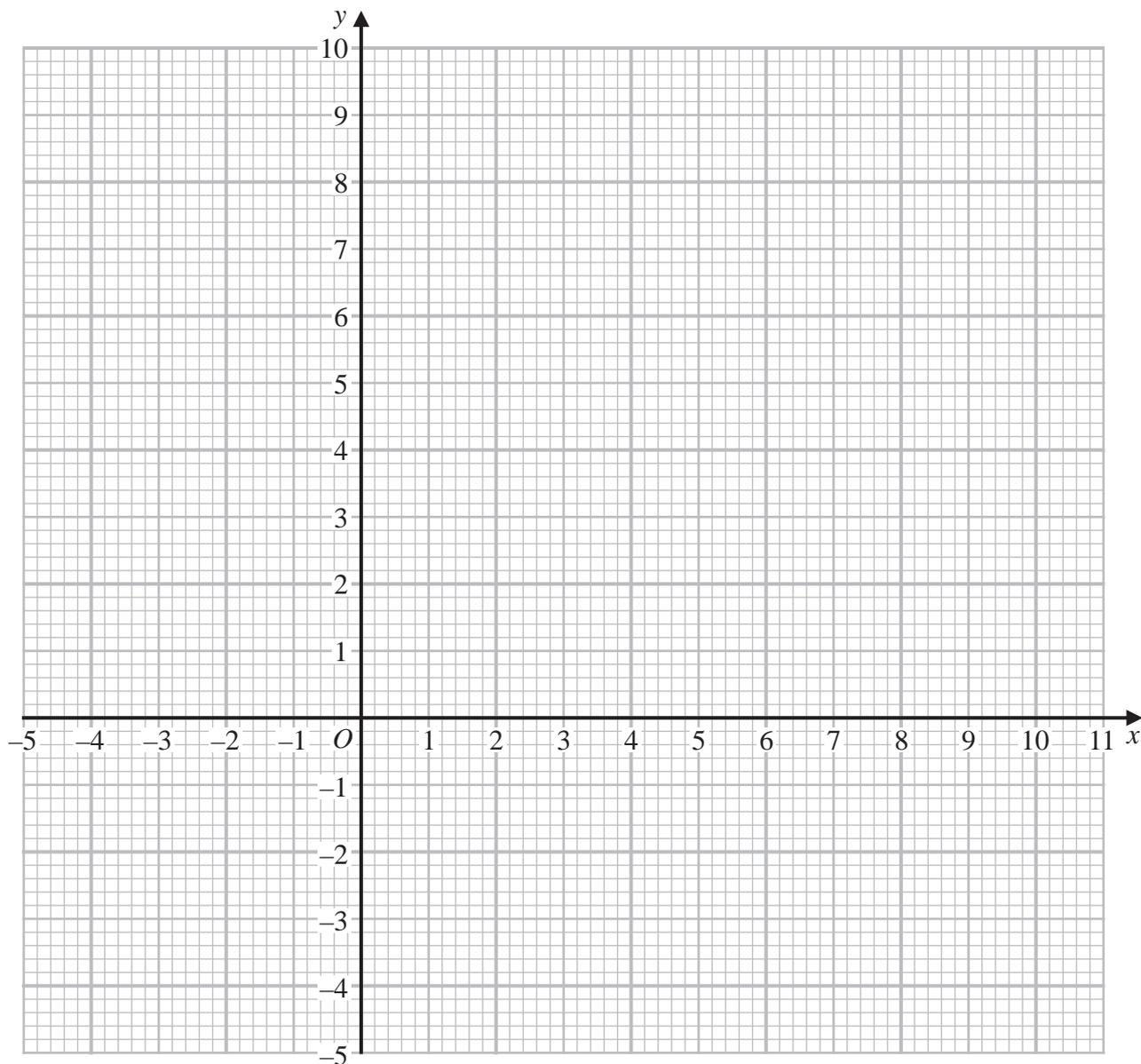
**Turn over for a spare grid if you need to redraw your graph.**





**Question 5 continued**

**Only use this grid if you need to redraw your graph.**



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**(Total for Question 5 is 7 marks)**



6

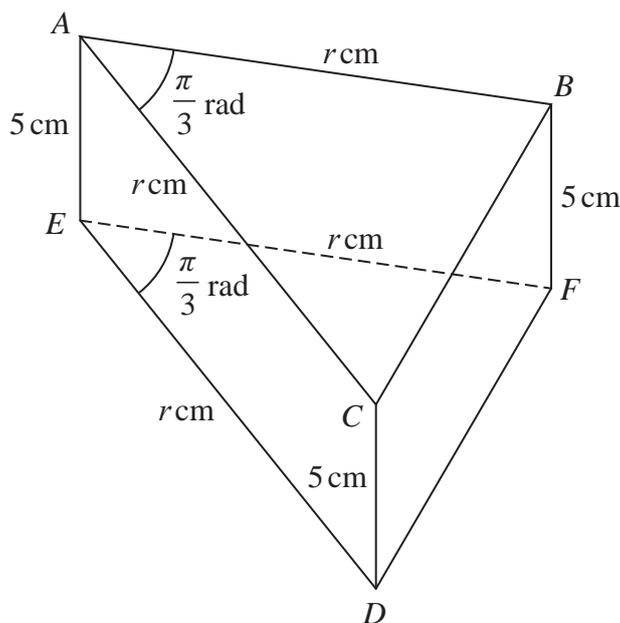


Diagram NOT accurately drawn

Figure 3

Figure 3 shows a right triangular prism  $ABCDEF$ . A cross section  $ABC$  of the prism is a triangle in which  $AB = AC = r$  cm and  $\angle CAB = \frac{\pi}{3}$  radians.

In the prism

$$AE = BF = CD = 5 \text{ cm} \quad ED = EF = r \text{ cm and } \angle DEF = \frac{\pi}{3} \text{ radians}$$

- (a) Show that the volume of the prism is  $\frac{5\sqrt{3}}{4} r^2 \text{ cm}^3$  (1)

The volume of the prism is increasing in such a way that the size of  $\angle CAB$  and the size of  $\angle DEF$  remain constant and the length of  $AE$ , the length of  $BF$  and the length of  $CD$  remain constant.

The lengths of  $AB$ ,  $AC$ ,  $ED$  and  $EF$  are each increasing at a constant rate of  $0.2 \text{ cm/s}$

- (b) Find the exact rate of increase, in  $\text{cm}^3/\text{s}$ , of the volume of the prism when the area of the rectangular face  $BCDF$  is  $60 \text{ cm}^2$  (5)

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**Question 6 continued**

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**Question 6 continued**

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**(Total for Question 6 is 6 marks)**



7 (a) Expand  $\left(1 + \frac{x}{3}\right)^{-3}$  in ascending powers of  $x$  up to and including the term in  $x^3$   
Where appropriate express each coefficient as an exact fraction in its lowest terms. (3)

(b) Write down the range of values of  $x$  for which your expression is valid. (1)

(c) Express  $(3 + x)^{-3}$  in the form  $P(1 + Qx)^{-3}$  where  $P$  and  $Q$  are rational numbers whose values should be stated. (2)

$$f(x) = \frac{(1 + 4x)}{(3 + x)^3}$$

(d) Obtain a series expansion for  $f(x)$  in ascending powers of  $x$  up to and including the term in  $x^2$  (2)

(e) Hence, using algebraic integration, obtain an estimate of  $\int_0^{0.2} f(x) dx$   
Give your answer to 5 significant figures. (3)

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**Question 7 continued**

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**Question 7 continued**

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**(Total for Question 7 is 11 marks)**





**Question 8 continued**

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**Question 8 continued**

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**(Total for Question 8 is 17 marks)**





**Question 9 continued**

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**(Total for Question 9 is 6 marks)**





**Question 10 continued**

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**Question 10 continued**

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**(Total for Question 10 is 16 marks)**





### Question 11 continued

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