

Please check the examination details below before entering your candidate information

Candidate surname	Other names
Centre Number	Candidate Number
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Pearson Edexcel International GCSE

Thursday 8 June 2023

Morning (Time: 2 hours)	<div style="display: flex; align-items: center;"> <div style="border: 1px solid black; padding: 2px 5px; font-size: 0.8em;">Paper reference</div> <div style="font-size: 1.5em; font-weight: bold; margin-left: 10px;">4PM1/02R</div> </div>
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Further Pure Mathematics

PAPER 2R

Calculators may be used.	Total Marks
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Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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International GCSE in Further Pure Mathematics Formulae sheet

MensurationSurface area of sphere = $4\pi r^2$ Curved surface area of cone = $\pi r \times$ slant heightVolume of sphere = $\frac{4}{3}\pi r^3$ **Series****Arithmetic series**Sum to n terms, $S_n = \frac{n}{2}[2a + (n-1)d]$ **Geometric series**Sum to n terms, $S_n = \frac{a(1-r^n)}{(1-r)}$ Sum to infinity, $S_\infty = \frac{a}{1-r}$ $|r| < 1$ **Binomial series** $(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots$ for $|x| < 1, n \in \mathbb{Q}$ **Calculus****Quotient rule (differentiation)**

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry**Cosine rule**In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

DO NOT WRITE IN THIS AREA



Answer all ELEVEN questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1 $f(x) = 2x^2 + (k + 8)x + k$

Show that for all values of k , the equation $f(x) = 0$ has distinct real roots.

(4)

Area with horizontal dotted lines for writing the answer to Question 1.

(Total for Question 1 is 4 marks)

DO NOT WRITE IN THIS AREA



P 7 4 2 8 4 A 0 3 3 2

Question 2 continued

Area with horizontal dotted lines for writing answers.

(Total for Question 2 is 6 marks)

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Question 3 continued

Area with horizontal dotted lines for writing answers.

(Total for Question 3 is 10 marks)

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Question 4 continued

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(Total for Question 4 is 6 marks)

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Question 5 continued

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(Total for Question 5 is 7 marks)

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Question 6 continued

A large rectangular area with horizontal dotted lines for writing answers.

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P 7 4 2 8 4 A 0 1 3 3 2

Question 6 continued

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Question 6 continued

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(Total for Question 6 is 10 marks)

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7

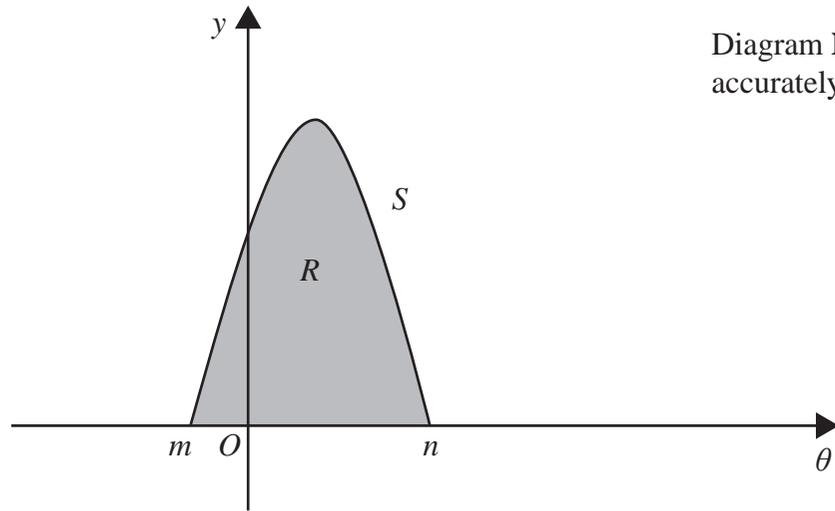


Figure 2

Figure 2 shows part of the curve S with equation $y = (\cos 3 + \sqrt{3} \sin 3)^{\frac{1}{2}}$

where $m \leq \theta \leq n$

The curve S meets the x -axis at the point with coordinates $(m, 0)$ and at the point with coordinates $(n, 0)$

- (a) Find the exact value of m and the exact value of n (3)

The finite region R , shown shaded in Figure 2, is bounded by the curve S , and the x -axis in the region $m \leq \theta \leq n$

The region R is rotated through 2π radians about the theta-axis.

- (b) Use calculus to find the exact volume of the solid generated. (4)

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Question 7 continued

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Question 7 continued

Area with horizontal dotted lines for writing answers.

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Question 7 continued

Handwritten answer area with horizontal dotted lines.

(Total for Question 7 is 7 marks)

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Question 8 continued

A large rectangular area with horizontal dotted lines for writing answers.

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Question 8 continued

Handwriting practice area consisting of 20 horizontal dotted lines for writing.

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Question 8 continued

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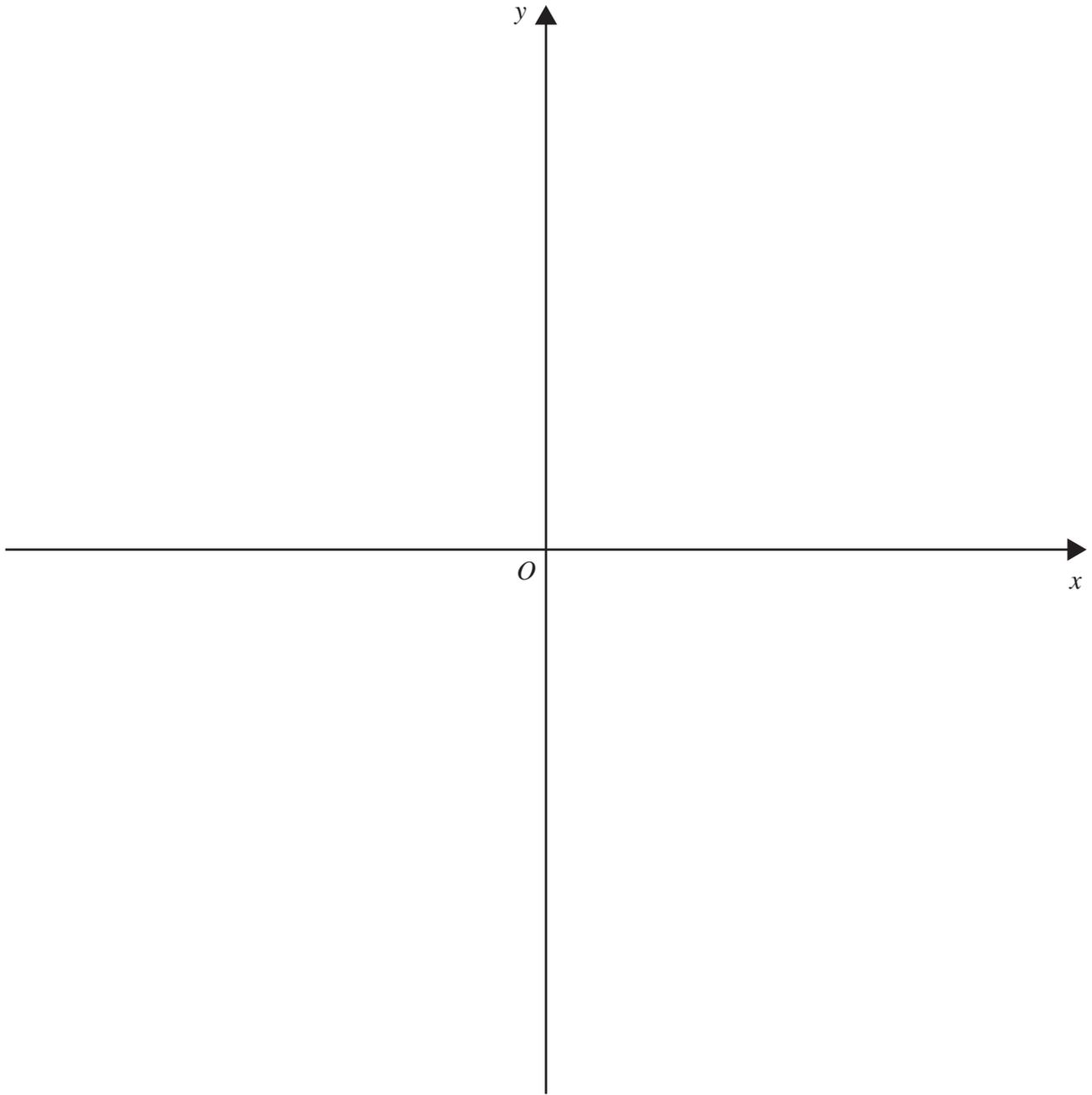
(Total for Question 8 is 16 marks)

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Question 9 continued



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P 7 4 2 8 4 A 0 2 5 3 2

Question 9 continued

Area for writing answers, consisting of multiple horizontal dotted lines.

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Question 9 continued

Handwritten area with horizontal dotted lines for writing.

(Total for Question 9 is 15 marks)

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P 7 4 2 8 4 A 0 2 7 3 2

10 Solve the equation

$$\log_4 x^3 + 8\log_x 64 = 22$$

(7)

Area with horizontal dotted lines for writing the solution.

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Question 10 continued

Handwritten area with horizontal dotted lines for writing.

(Total for Question 10 is 7 marks)

DO NOT WRITE IN THIS AREA



P 7 4 2 8 4 A 0 2 9 3 2

Question 11 continued

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P 7 4 2 8 4 A 0 3 1 3 2



Question 11 continued

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DO NOT WRITE IN THIS AREA

(Total for Question 11 is 12 marks)

TOTAL FOR PAPER IS 100 MARKS

